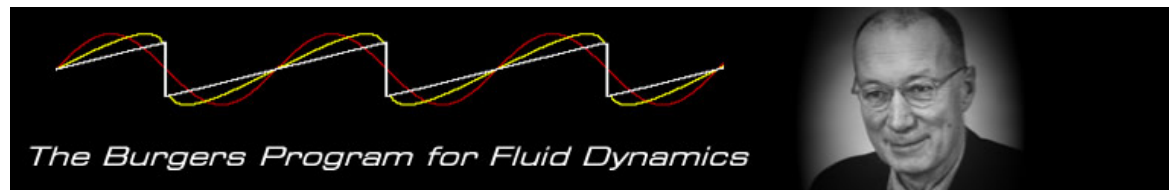


Highlights of Fifty Years of Turbulent Boundary Layer Research

Turbulence Colloquium Marseille 2011



James Wallace



Landmarks of Turbulent Boundary Layer Research

Pre – 1961

Development of Hot-wire anemometry & measurement of statistical properties.

1960s

Visualization identifying organized (coherent) structures related to turbulence production.

1970s

Conditional sampling and averaging methods (quadrant analysis, VITA, etc.) developed to quantify properties and effects of organized structures.

1980s

First DNS of turbulent channel and boundary layer flows providing full spatial field properties and access to 3D structural information. First experimental measurements of velocity gradient tensor based properties: vorticity, dissipation rate, etc.

1990s

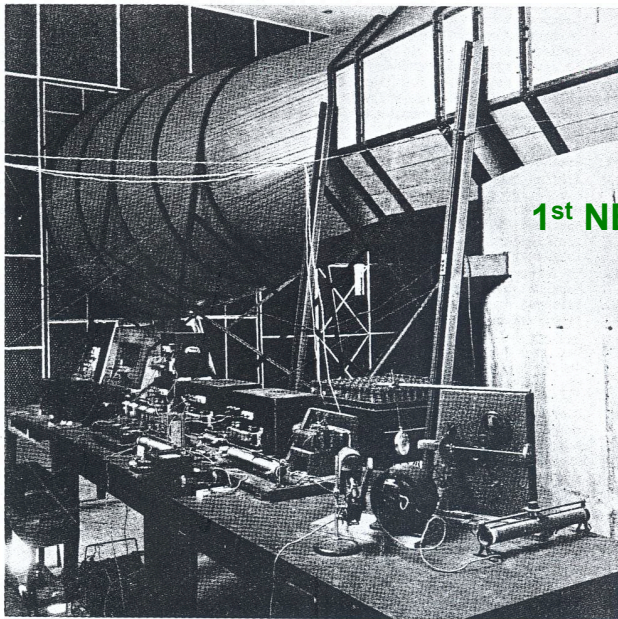
Development of better methods to identify vortices. Implementation of planar PIV providing new insights to flow structure. Development of field sites for experiments in the ASL at very high Reynolds numbers. Development of high Reynolds number laboratory facilities.

2000s

DNS at significantly higher Reynolds numbers and supersonic Mach numbers. Use of stereo-, tomographic- & holographic-PIV to provide additional insight about flow structure.

2010s

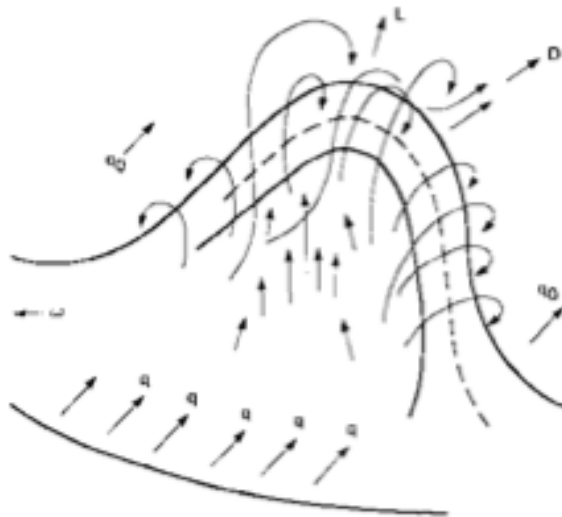
DNS for much higher Reynolds numbers and hypersonic flow ($Re_\theta \sim 11,000$ & Mach ~ 12).



1st NBS hot-wire apparatus

Figure 1. General View of First NBS Hot-Wire Apparatus (Dryden and Kueth, reference [5])

Dryden & Kueth (1929) NACA TR 320



“horseshoe” structure of wall bounded turbulence

Theodorsen (1952) 2nd Midwestern. Conf. on Fl. Mech.

Pre - 1961

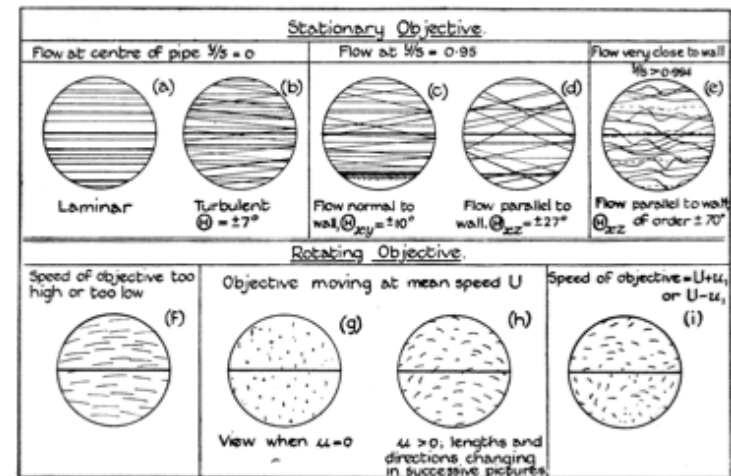
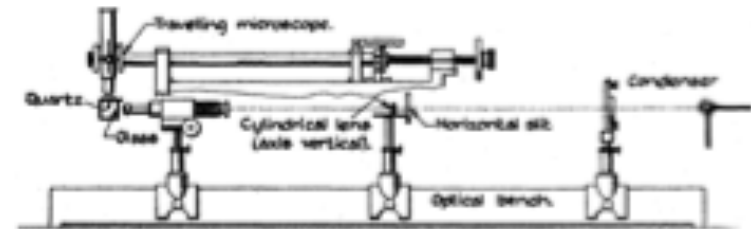


FIG. 2 (a)-(e).—Sketches of Paths of Particles as observed in the Ultramicroscope.

Fage & Townend (1932) Proc. Roy. Soc. Lond. A 135

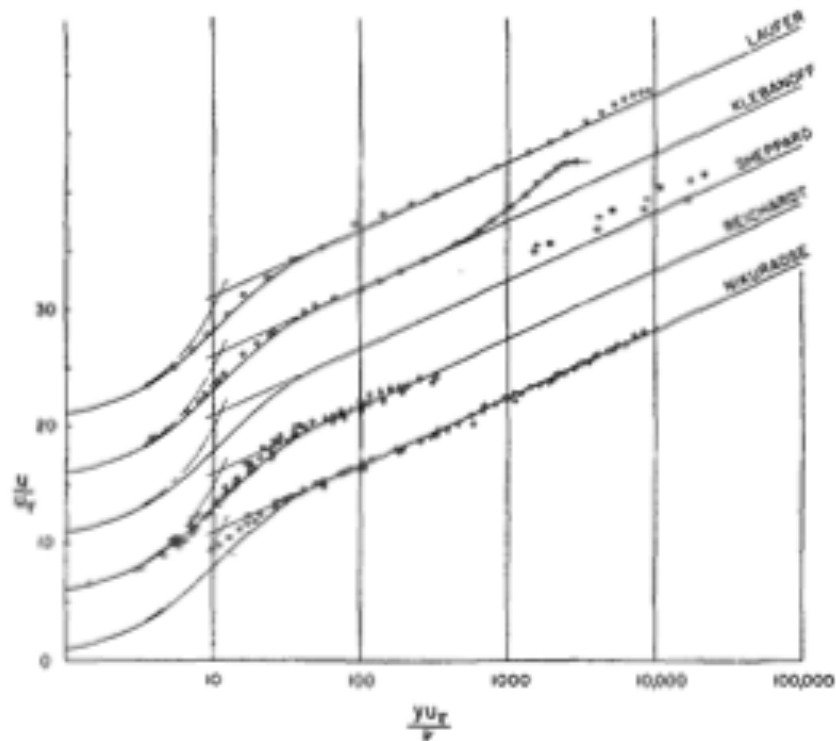


Figure 1. The law of the wall.

$$\frac{u}{u_\tau} = \frac{1}{\kappa} \ln\left(\frac{y u_\tau}{\nu}\right) + c$$

Millikan (1938) 5th Int. Appl. Mech. Congress

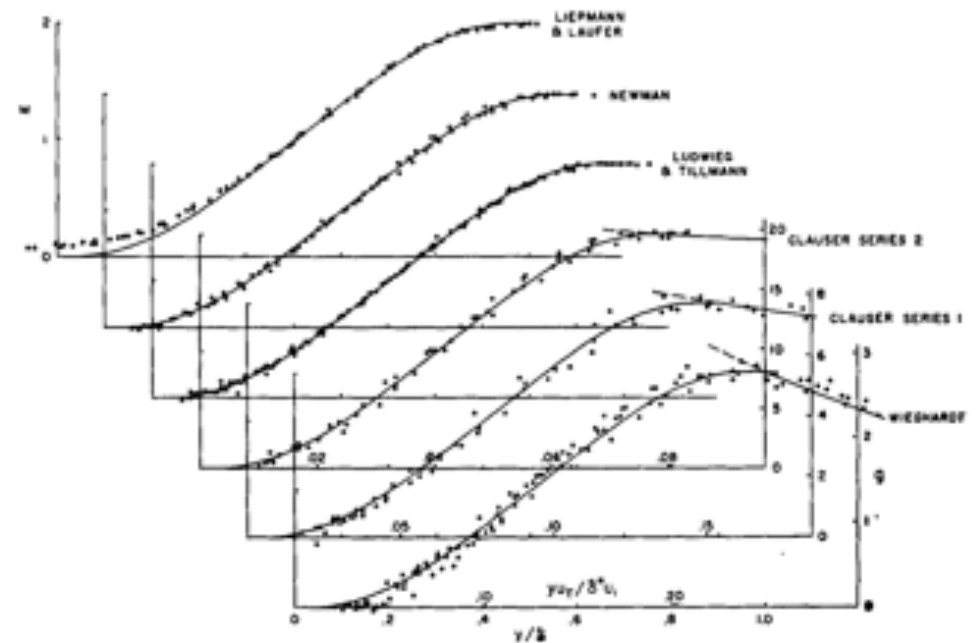


Figure 2. The law of the wake.

$$\frac{u}{u_\tau} = f\left(\frac{y u_\tau}{\nu}\right) + \frac{\Pi}{\kappa} \ln\left(\frac{y}{\delta}\right)$$

Coles (1956) JFM 1

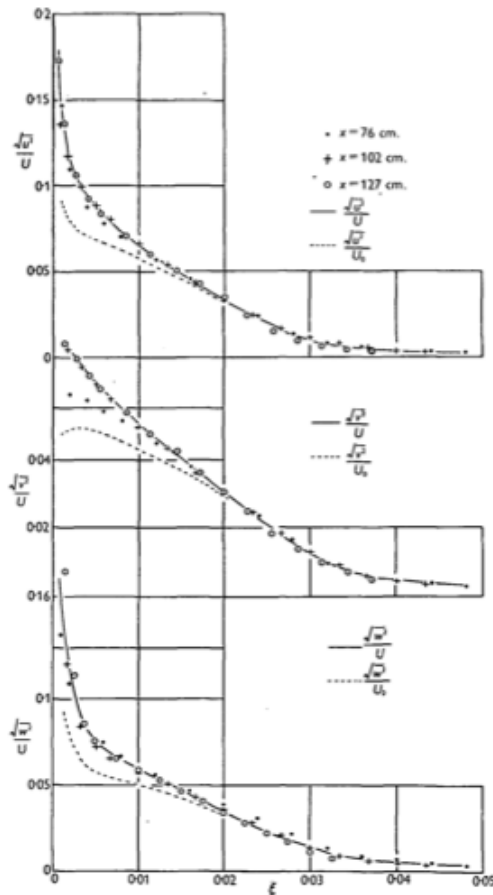


Fig. 3. Turbulent intensities.

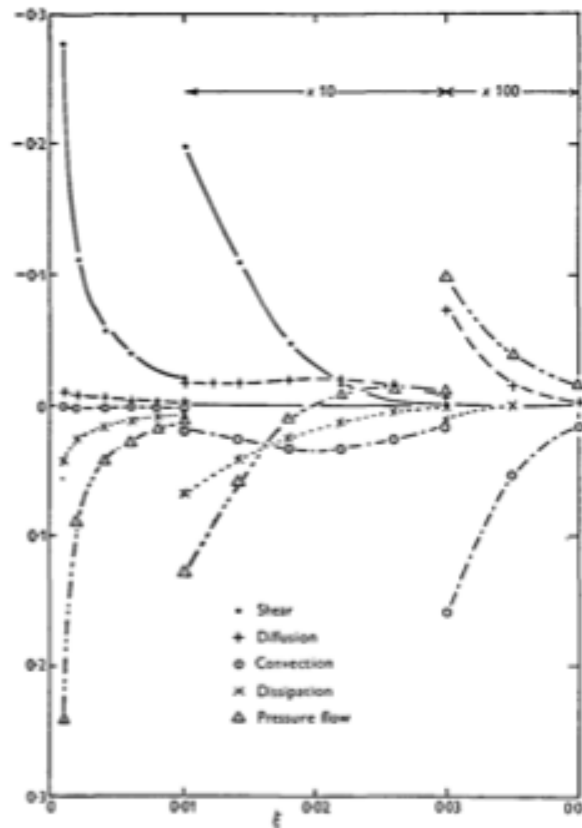


Fig. 7. Total energy balance.

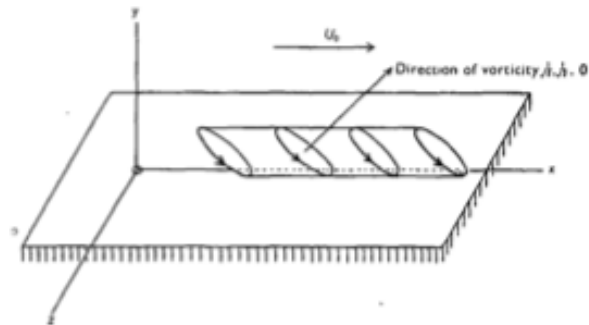


Fig. 12. Eddy structure.

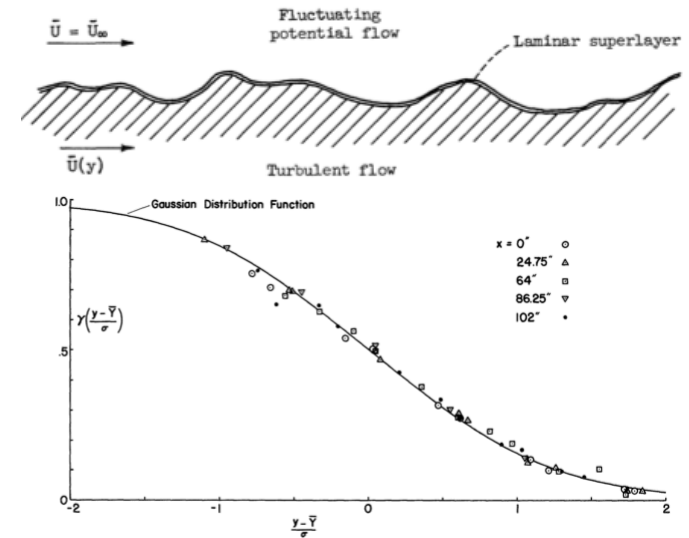


Figure 20.- Intermittency distributions for several x-stations in boundary layer.

Corrsin & Kistler (1954) NACA TN 3133

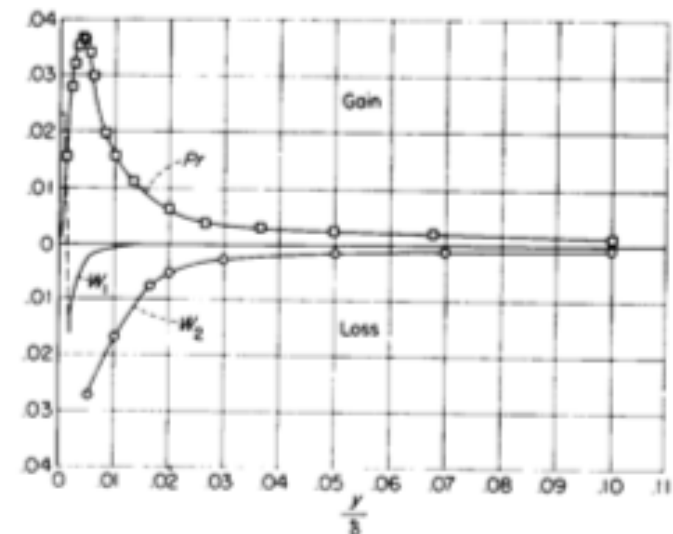


FIGURE 23. -Production and dissipation in region near wall.

Townsend (1951) Math. Proc. Cambridge Phi. Soc. 47

Klebanoff (1955) NACA Rep. 1247

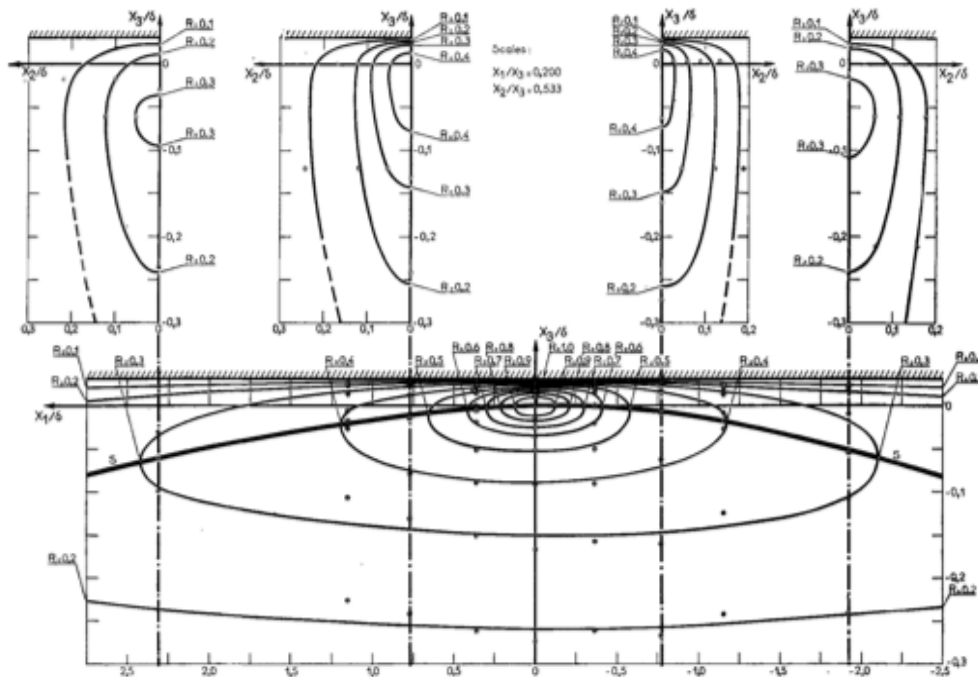


Figure 7. Space-time isocorrelation surfaces with optimum delay in the boundary layer on a flat plate; $\delta = 33$ mm, $R_s = 27900$, $y'/\delta = 0.03$

Grant (1958) JFM 4

Favre, Gaviglio & Dumas (1958) JFM 3

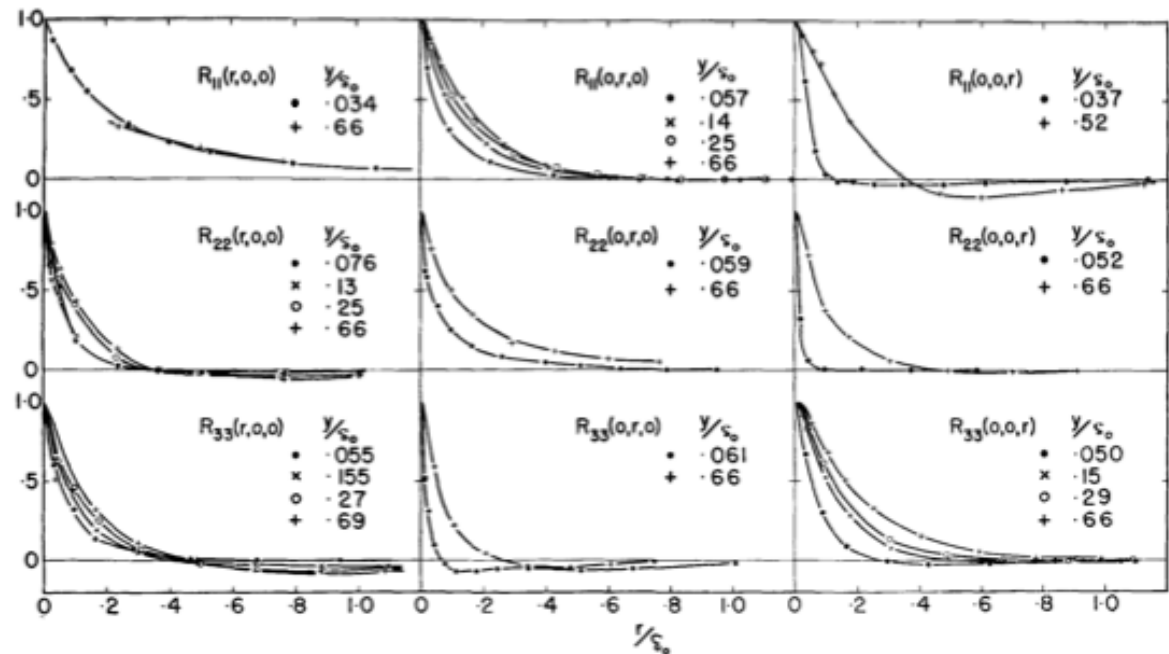


Figure 21. The nine correlations in the boundary layer.

1961 – 1970: Visualization & Measurement

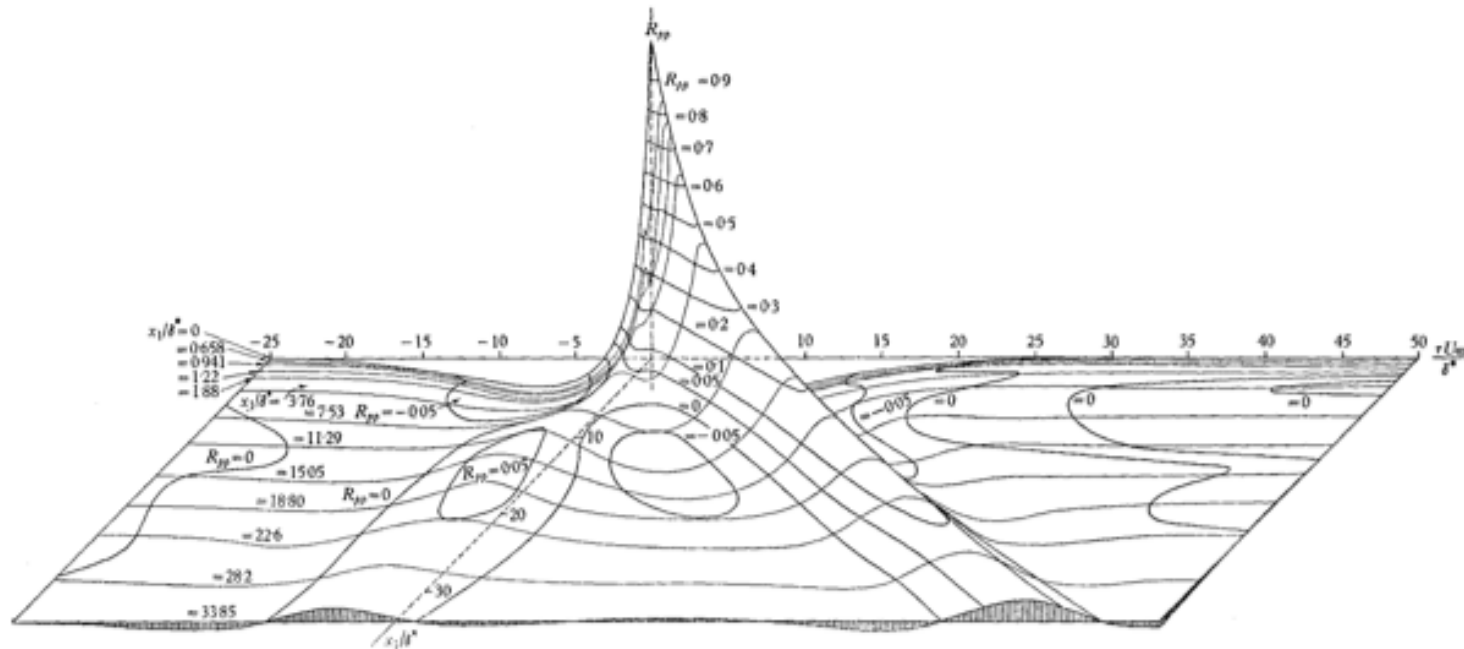


FIGURE 6. Longitudinal space-time correlation of the wall pressure displayed in three dimensions using the data of figure 5.

Willmarth & Wooldridge (1962) JFM 14

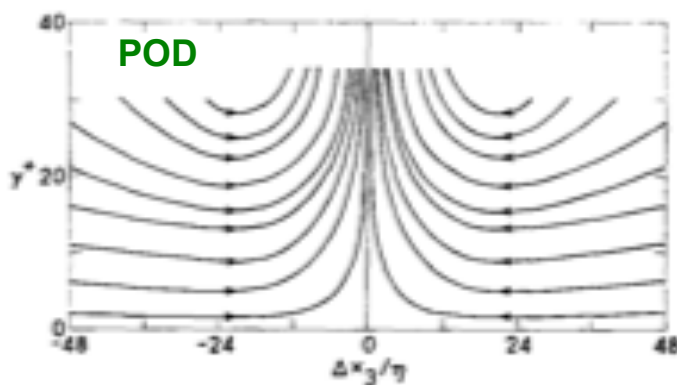


FIG. 11. Streamlines of the large eddy structure in a plane normal to the mean flow.

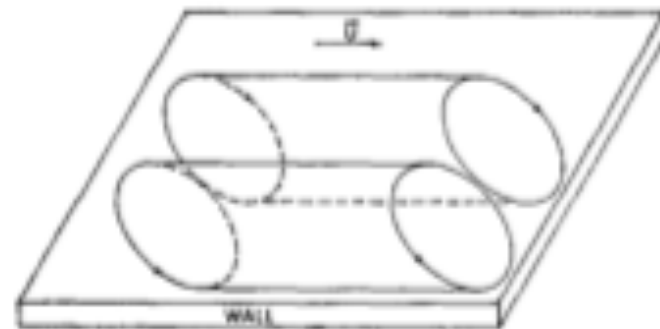
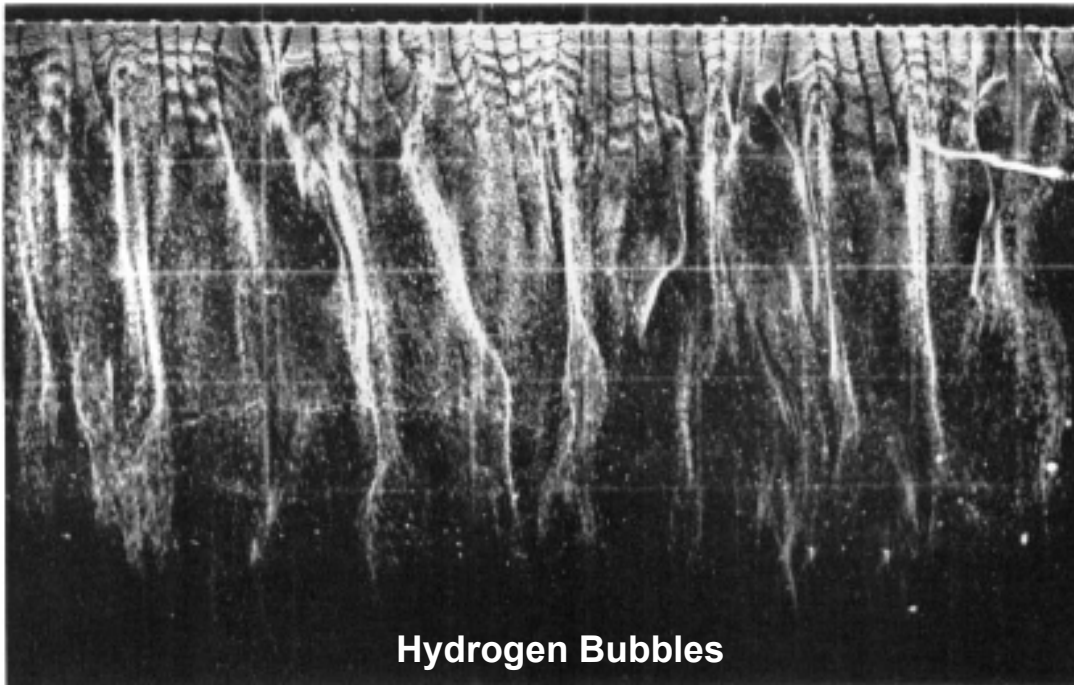


FIG. 12. Composite representation of the large eddy pairs.

Bakewell & Lumley (1967) Phys. Fl. 10



Hydrogen Bubbles

FIGURE 10b. $y^+ = 4.3$.

FIGURE 10. Photographs of the structure of a flat plate turbulent boundary layer.

Kline, Reynolds, Schraub & Runstadler (1967) JFM 30

**View Multi-media Fluid Mechanics
videos 4192, 4497 & 4766 in the
Media Library**

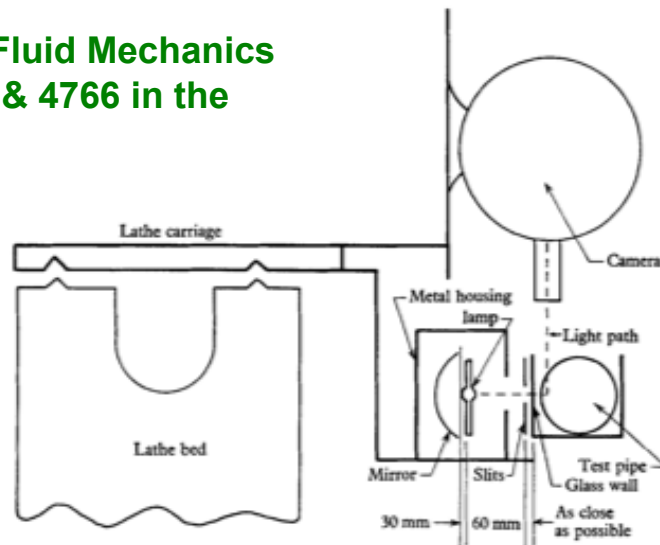


FIGURE 2. Optical system.

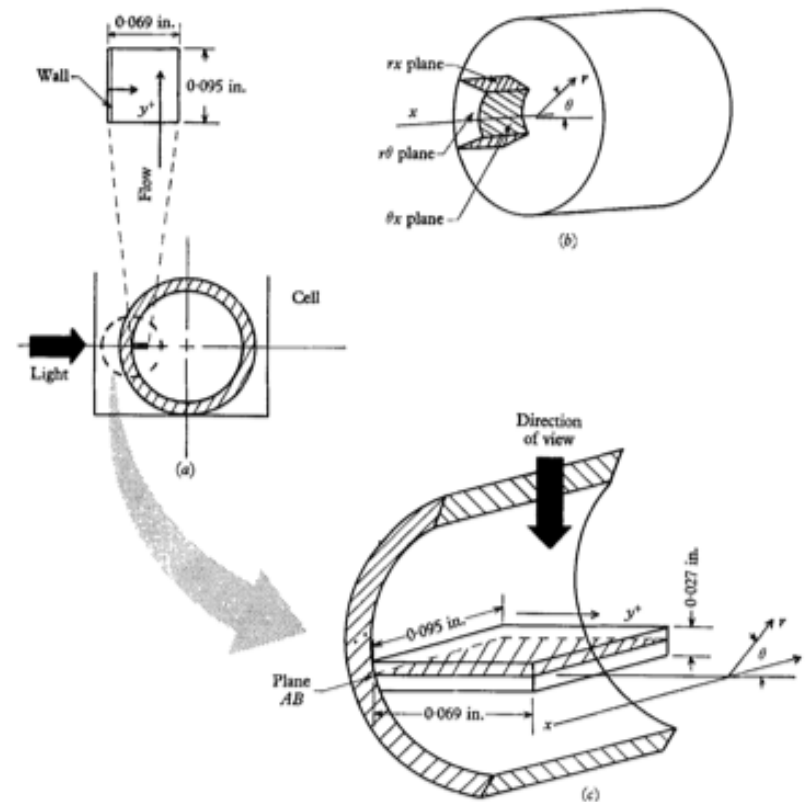


FIGURE 3. Wall view (dimensions for $\times 4.3$).

Corino & Brodkey (1969) JFM 37

1970 – 1986: Conditional Processing of Measurements & Further Visualization

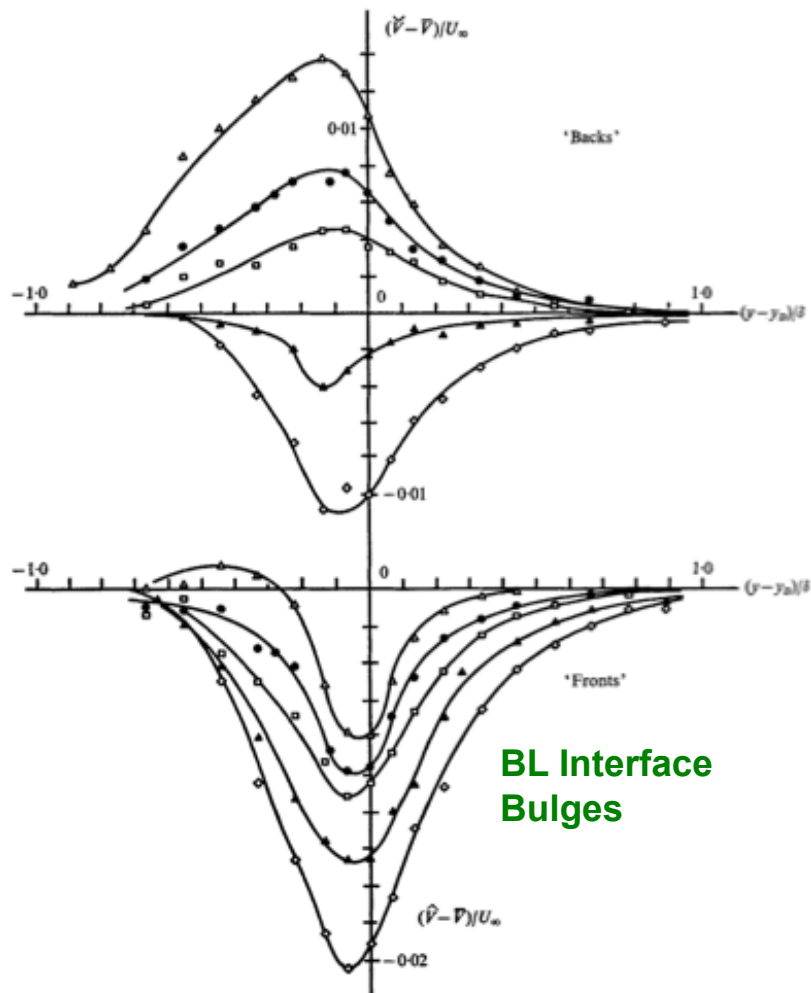


FIGURE 9. Point averages of the normal velocity component as a function of the distance from the interface. $\gamma(y_0)$: Δ , 0.1; $\bullet$, 0.3; $\square$, 0.5; $\blacktriangle$, 0.7; $\diamond$, 0.9.

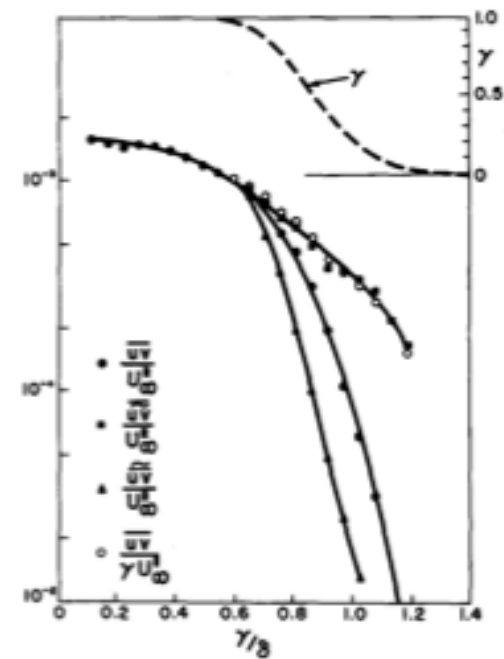


FIG. 1. Conditional averages of the Reynolds stress.

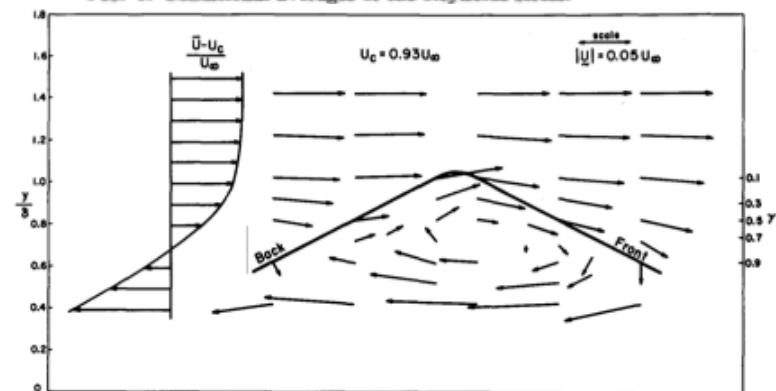


FIG. 3. Composite velocity distribution in the outer region of the boundary layer.

Kovasznay, Kibens & Blackwelder (1970) JFM 41

Blackwelder & Kovasznay (1972) Phys. Fl. 15

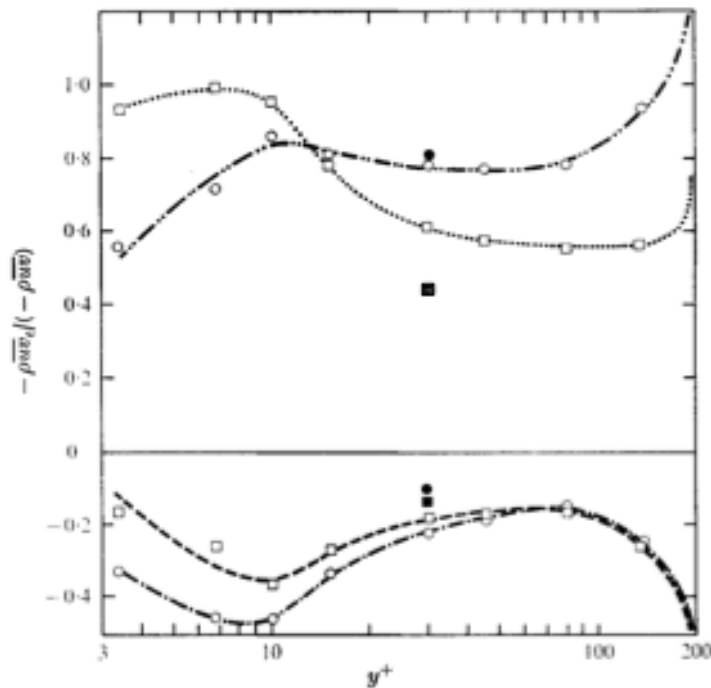


FIGURE 1. The classified Reynolds stresses normalized with the local average Reynolds stress. ●, ■, results of Willmarth & Lu (1972). ·····, sweep; —·—·, ejection; —·—·, i_o , outward interaction; —·—·, i_w , wallward interaction.

Wallace, Eckelmann & Brodkey (1972) JFM 54
 Brodkey, Wallace & Eckelmann (1974) JFM 63
 Wallace & Brodkey (1977) Phys. Fl. 20

Quadrant Analysis

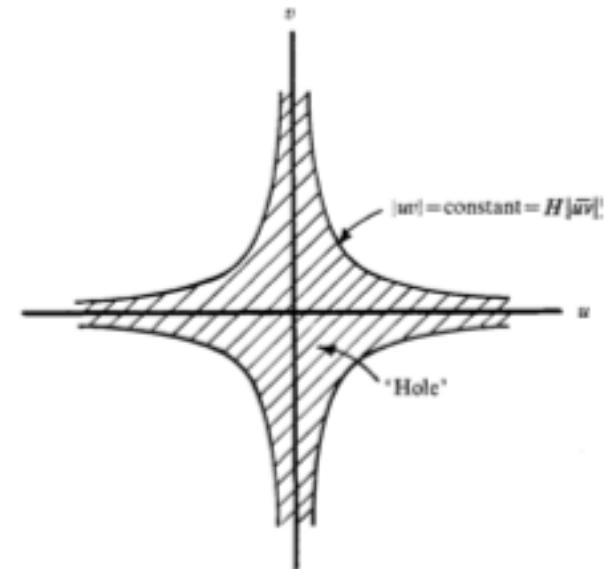


FIGURE 15. Sketch of 'hole' region in uv plane.

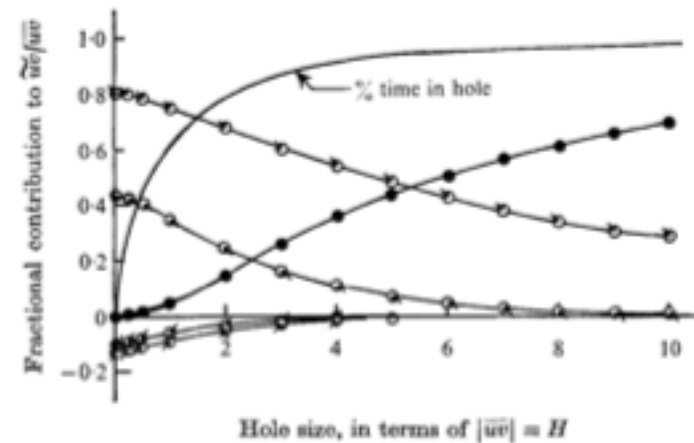
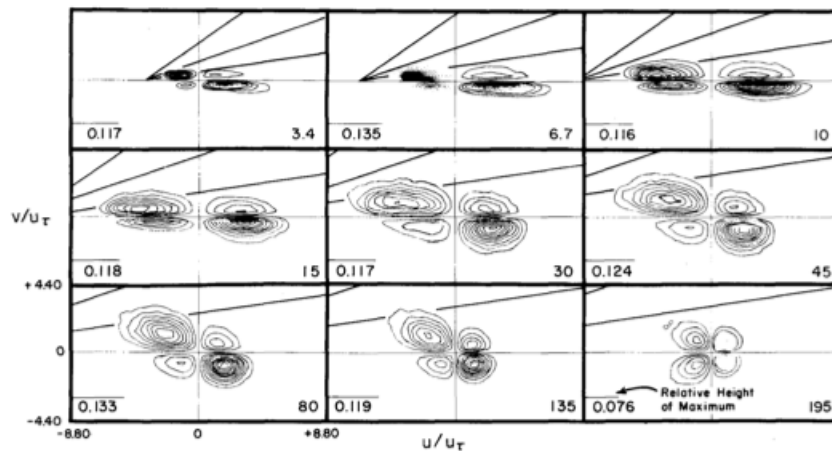


FIGURE 16. Contributions to Reynolds stress from truncated quadrants of u, v plane and percentage time spent in 'hole' as a function of 'hole' size. uv measured at $y^+ = 30$ in low-speed boundary layer; $U_\infty = 19.7$ ft/s. Open circles indicate $|uv| > \text{hole size}$: ○, $u > 0, v > 0$; ◐, $u < 0, v > 0$; ◑, $u < 0, v < 0$; ◒, $u > 0, v < 0$. ●, 'hole', $|uv| < \text{hole size}$.



Willmarth & Lu (1972) JFM 55
 Lu & Willmarth (1973) JFM 60

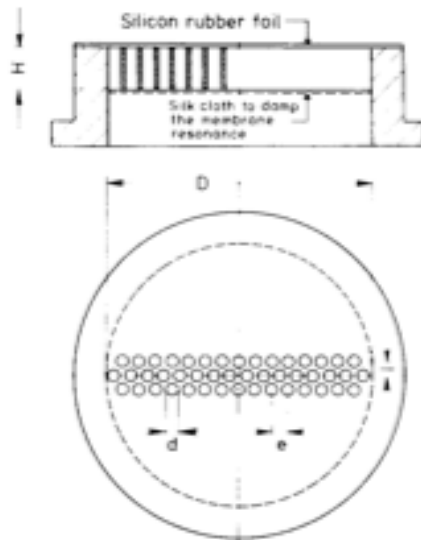


FIG. 1. Pressure transducer ($D = 97$ mm, $H = 6$ mm, $d = 2.5$ mm, $e = 3$ mm, $t = 2.6$ mm).

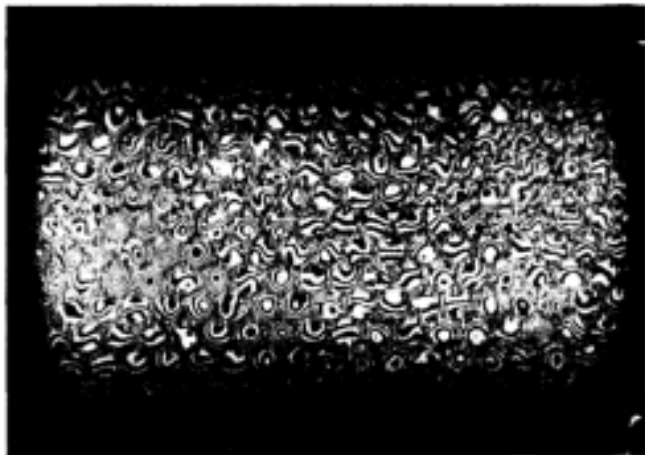


FIG. 9. Interference fringe pattern of one frame of a film taken with $U_\infty = 8.5$ m/sec and a frame rate of 7000 frames per second.

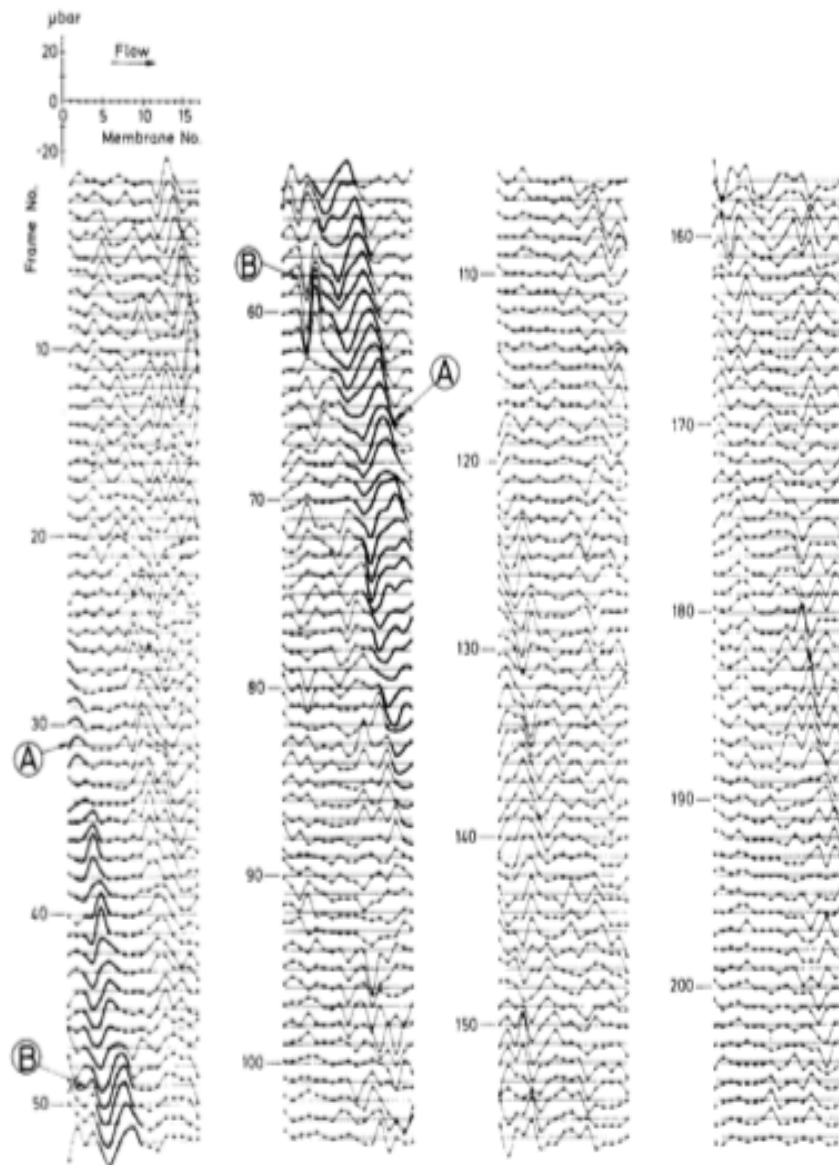


FIG. 11. Sequence of consecutive pressure distributions along one row of 17 membranes lying in flow direction one behind the other. (Flow from left to right, flow velocity $U_\infty = 8.5$ m/sec, time between consecutive maps $\Delta t = 0.14$ msec.)

Patterns ~
1100 Δx , 1.6 δ

Emmerling (1973) MPI für Strömungsforschung Bericht No. 9

Dinkelacker, Hessel, Meier & Schewe (1977) Phys. Fl. 20

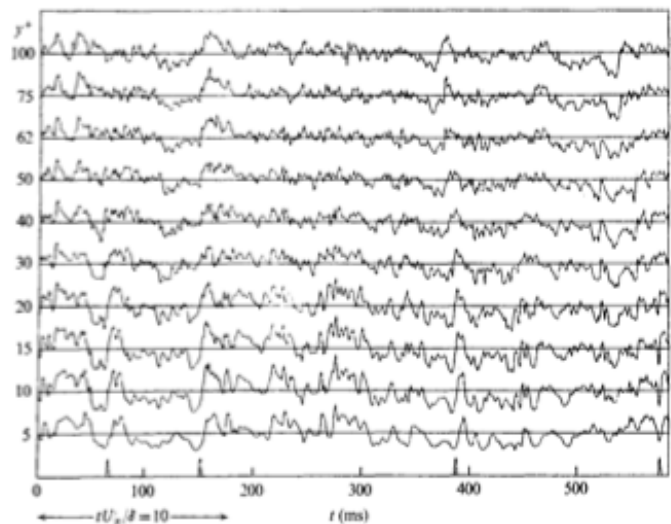


FIGURE 7. Instantaneous streamwise velocities as a function of the normal direction. The detector function obtained at $y^+ = 15$ is shown between the tick marks.

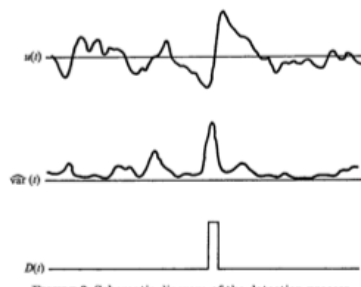


FIGURE 3. Schematic diagram of the detection process.

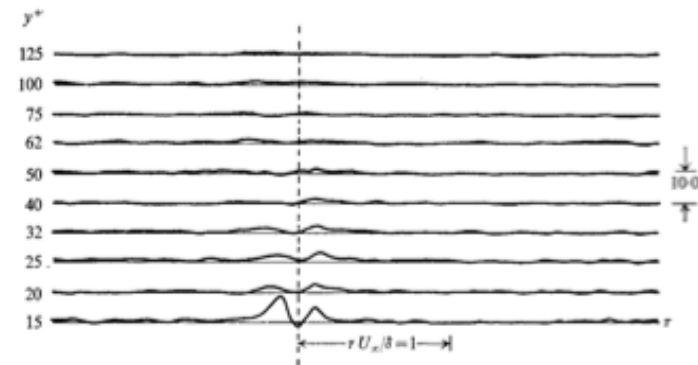


FIGURE 14. The conditional averages of the Reynolds shear stress at $\Delta x = 0$, $Re = 2550$.

VITA Conditional Sampling

Blackwelder & Kaplan (1976) JFM 76

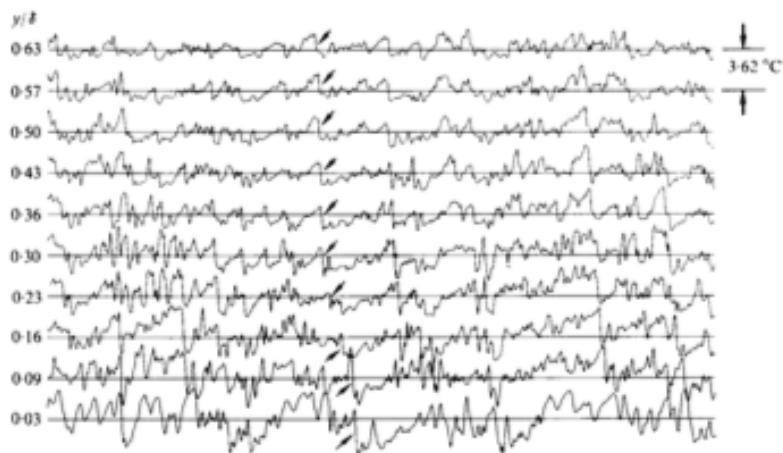


FIGURE 12. Simultaneous temperature signals from the ten-wire rake in the turbulent region. The horizontal time span is $18.7 U_\infty \Delta t / \delta$. One particular temperature front is denoted by the arrows.

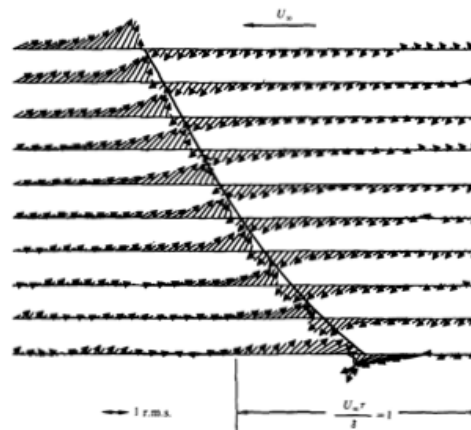


FIGURE 18. Composite picture of the velocity field associated with the internal front. The velocity components are normalized with their local fluctuation levels. The velocity magnitude and time scale are given at the bottom of the figure. For clarity only every other velocity vector has an arrowhead.

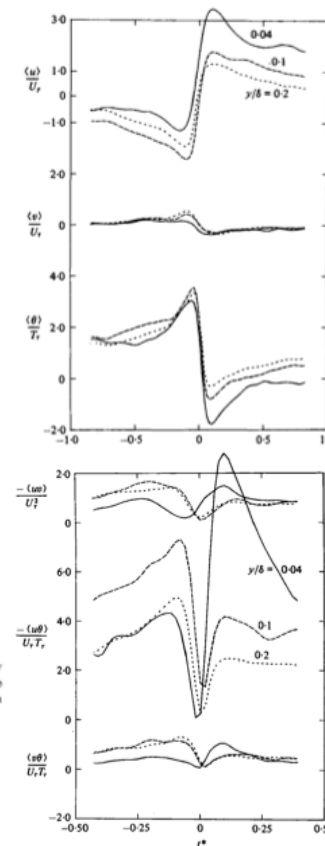


FIGURE 4. Conditional averages of products uw , wv , $v\theta$ in the inner layer

Chen & Blackwelder (1978) JFM 89

Antonia, Rajagopalan, Subramanian & Chambers (1977) JFM 121

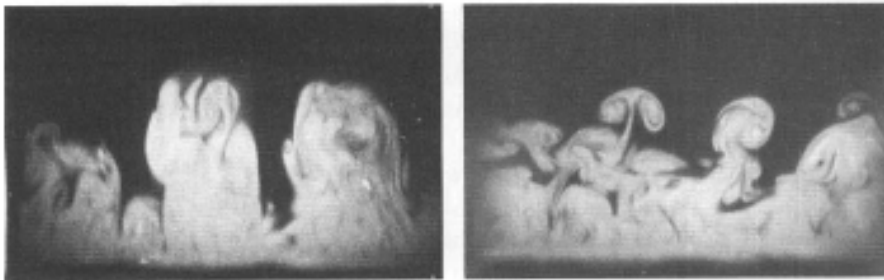


FIGURE 21. Comparison between views with transverse light plane inclined

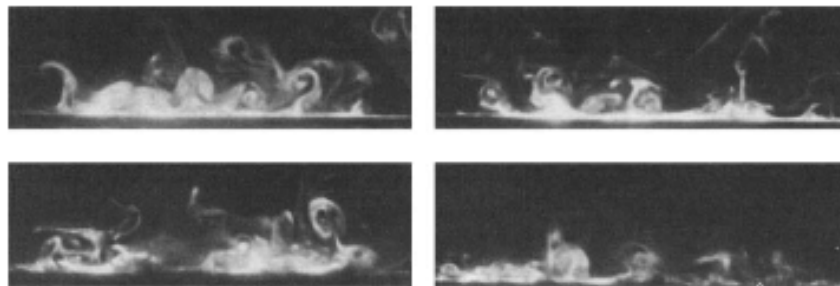
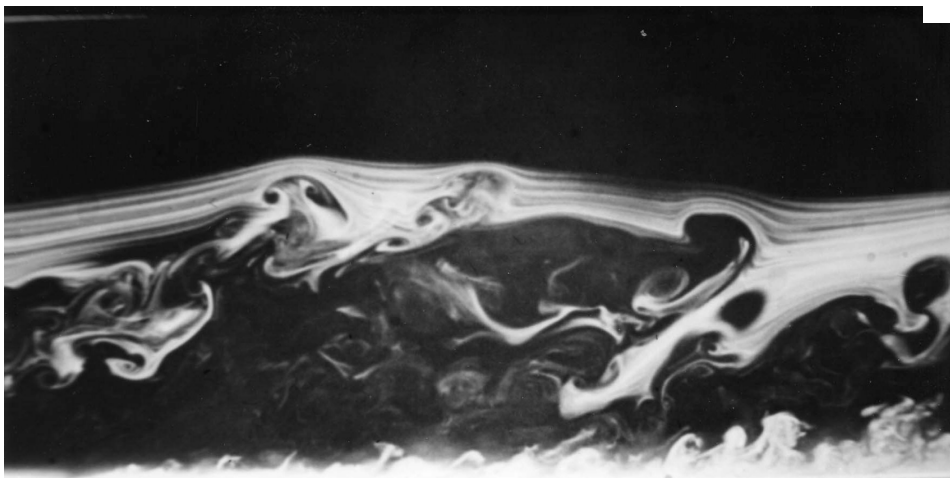


FIGURE 26. Examples of longitudinal vortices and vortex pairs in near-wall region.

Head & Bandyopadhyay (1981) JFM 107



Balint, Ayrault & Wallace (1981)

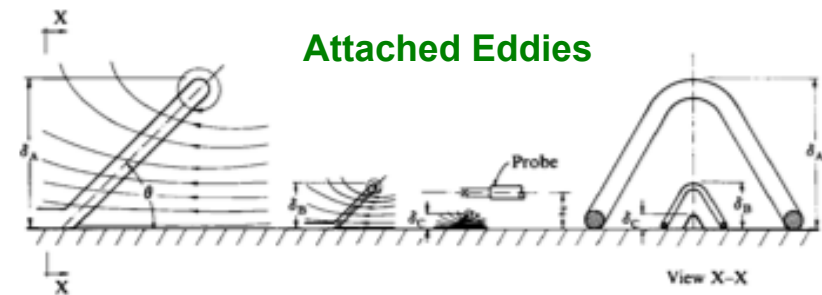
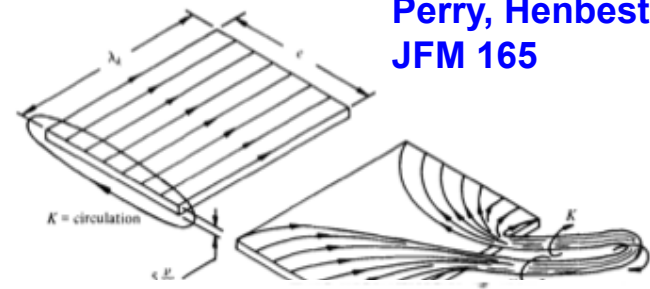


FIGURE 1. A sketch of three attached eddies of varying scales together with the instantaneous streamline pattern generated by each.

Attached Eddies

Townsend (1970, 1976)
Perry, Henbest & Chong (1986)
JFM 165



Perry & Chong (1982) JFM 119

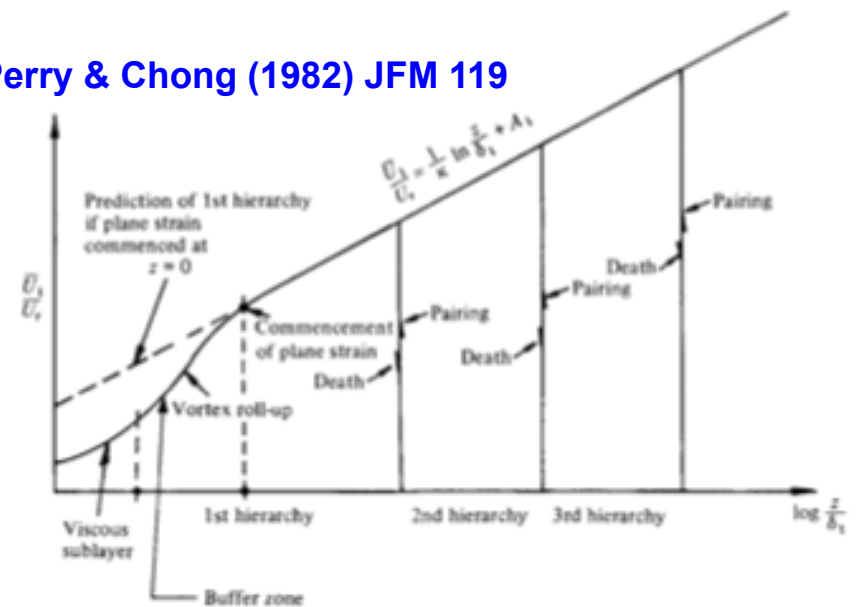


FIGURE 18. Mean-velocity profile interpreted in terms of quantum-jump model. A_1 is a universal constant.

1986 – 2011: DNS, Multi-Sensor Hot-Wire Probes & PIV Measurement

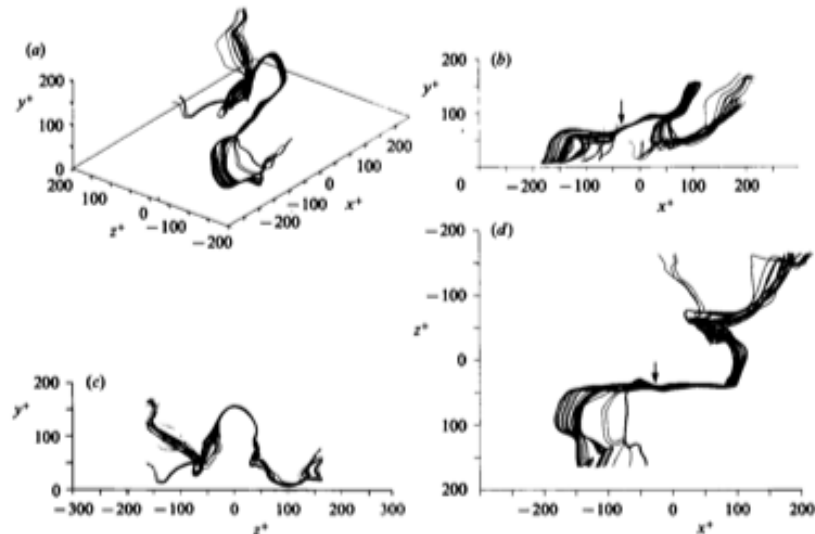


FIGURE 15. Vortex lines of an instantaneous vortical structure detected by QD-2: (a) oblique view; (b) side view; (c) end view; (d) top view.

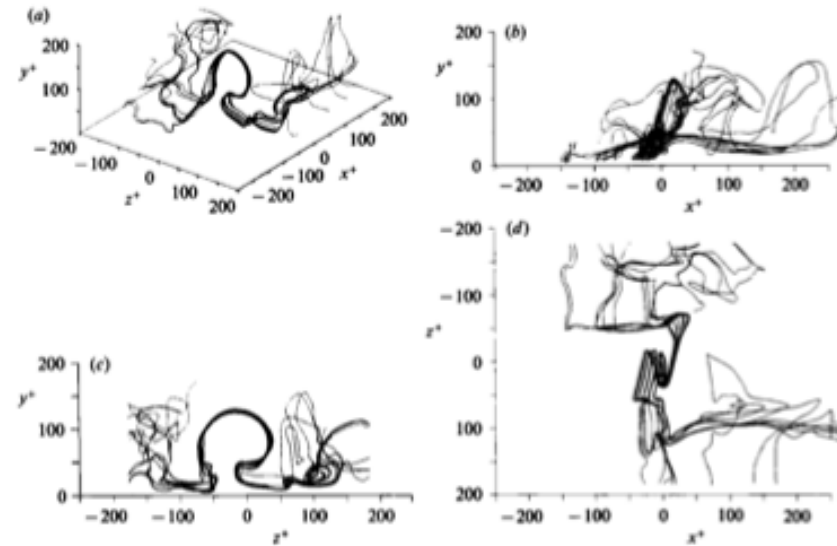


FIGURE 14. Vortex lines of an instantaneous vortical structure detected by QD-2: (a) oblique view; (b) side view; (c) end view; (d) top view.

Kim & Moin (1986) JFM 162

DNS $R_\tau = 180$

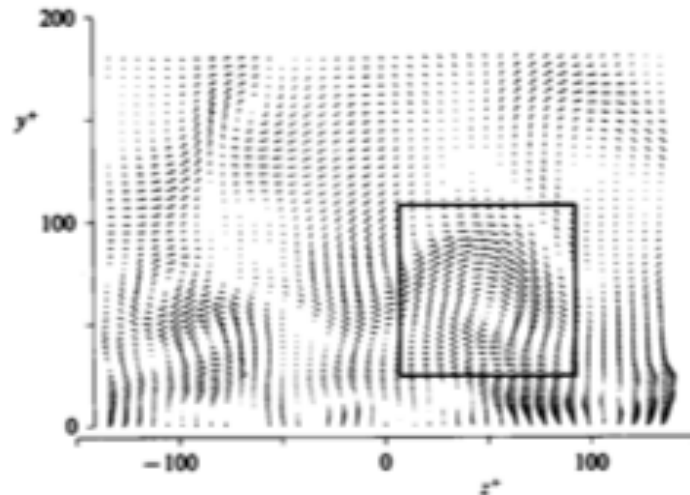
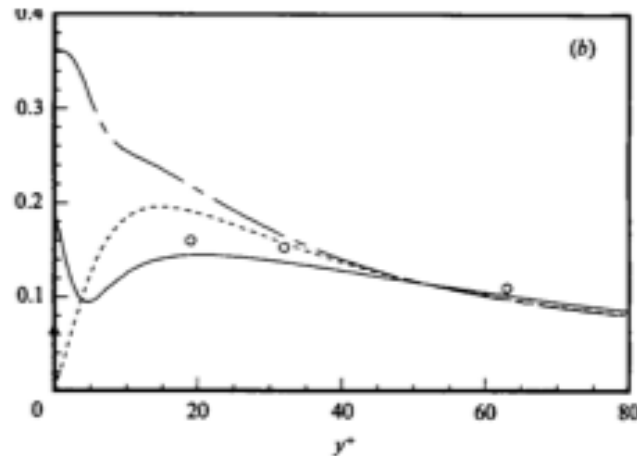


FIGURE 18. Velocity vectors in a (y, z) -plane. The streamwise location is indicated in figure 15(b), and the direction of the mean flow is into the figure.



Kim, Moin
& Moser (1987)
JFM 177

FIGURE 14. Root-mean-square vorticity fluctuations normalized by the mean shear. (a) In global coordinates: —, $\omega_x v/u_\tau^2$; ---, $\omega_y v/u_\tau^2$; - · - · -, $\omega_z v/u_\tau^2$; (b) in wall coordinates: $\circ$, ω_x from Kastrinakis & Eckelmann (1983), $\triangle$, ω_x at the wall from Kreplin & Eckelmann (1979).

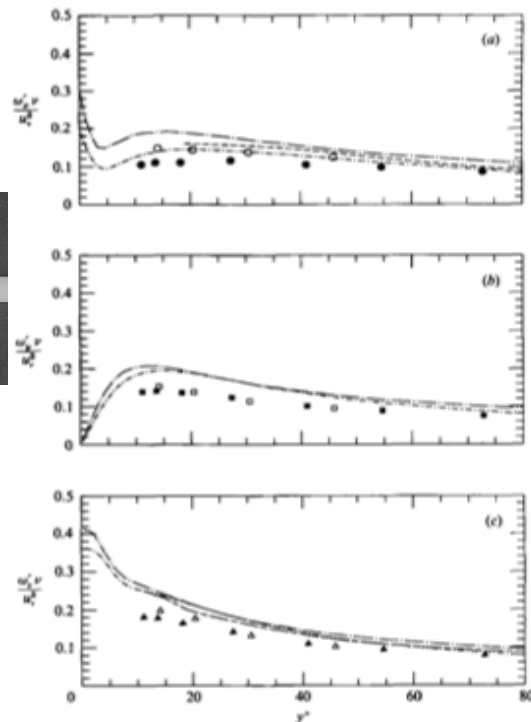
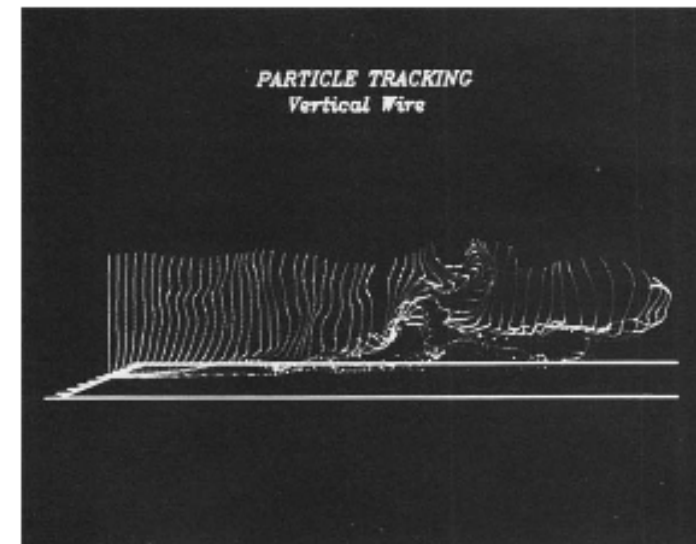
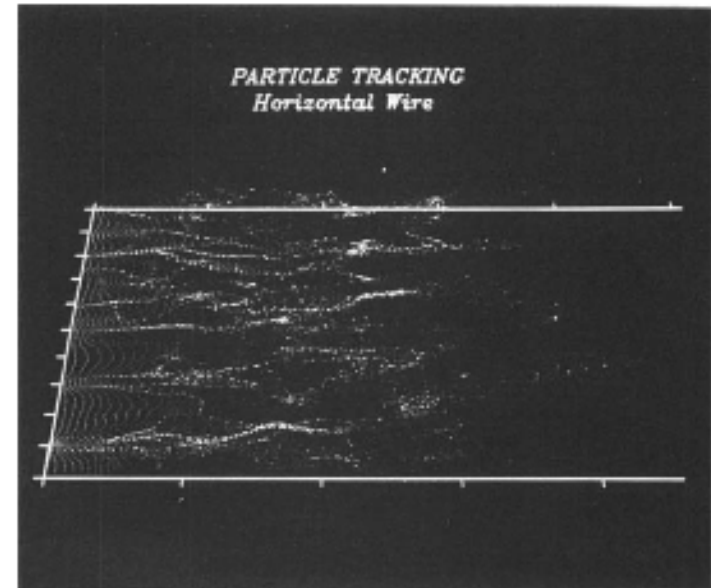


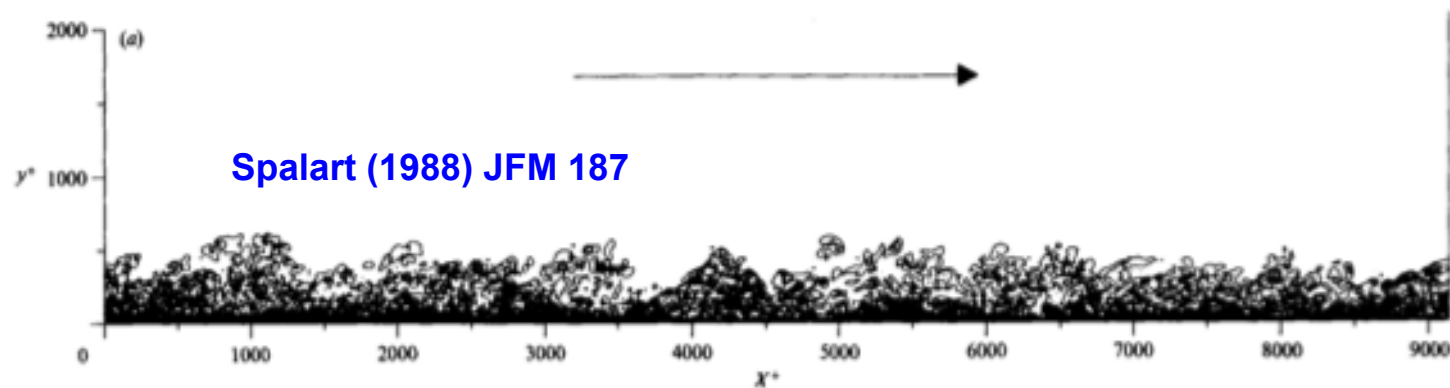
FIGURE 12. Measured r.m.s. fluctuating vorticity components normalized with inner scaling u_τ and v_τ and compared to other measured and simulated values. Symbols given in table 2.

Balint, Vukoslavčević & Wallace (1987),
(1991) JFM 228



(c)

FIGURE 25. Flow structures visualized by fluid markers: (a) particles are generated along a line parallel to the z -axis at $y^+ \approx 10$ (oblique top view); (b) particles are initially distributed uniformly on a plane parallel to the wall at $y^+ \approx 10$ (top view); (c) particles are generated along a line parallel to the y -axis (side view).



Spalart (1988) JFM 187

FIGURE 19. Vorticity contours, $R_\tau = 1410$. (a) streamwise plane; (b) spanwise plane; (c) downstream plane, at 45° ; (d) upstream plane, at 45° . Contour levels: $|\omega| (\partial v / u_\tau^2)^{1/2} = 1, 2, 3, \dots$

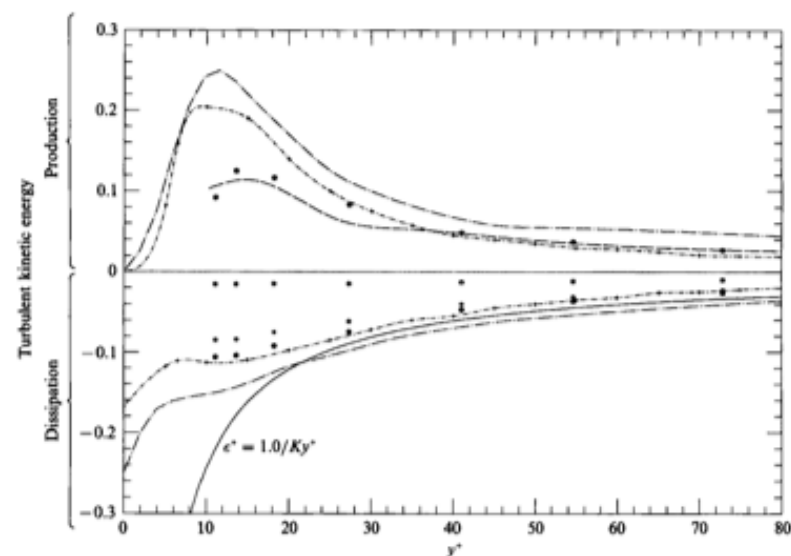
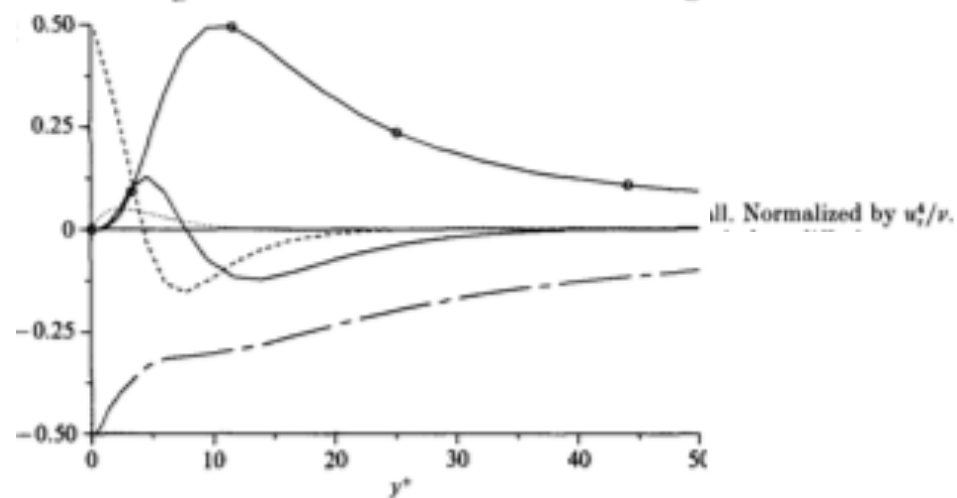
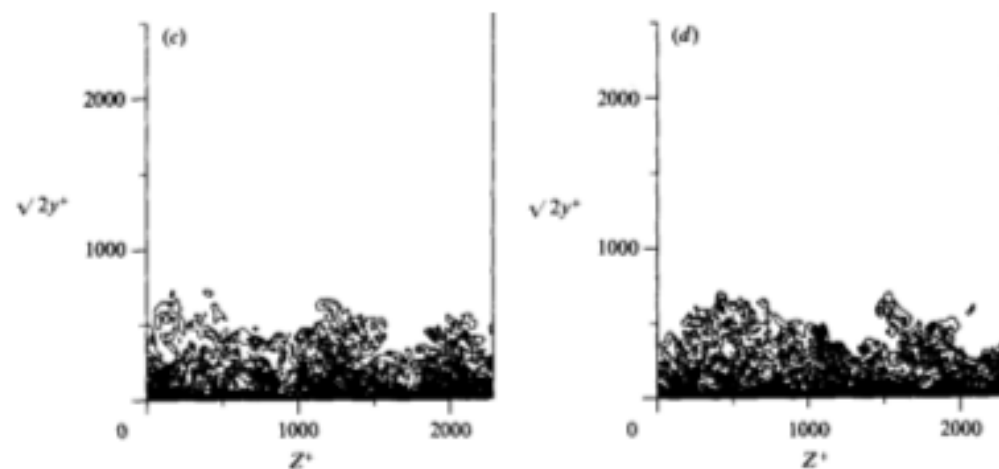


FIGURE 10. Measured turbulent kinetic energy production and dissipation rates normalized with inner scaling u_τ and ν and compared to other measured and simulated values. Symbols given in table 2 except for $\bullet$, dissipation neglecting cross-product velocity gradient correlations and $\oplus$, dissipation assuming isotropy.

Balint, Vukoslavčević & Wallace (1987),
(1991) JFM 228

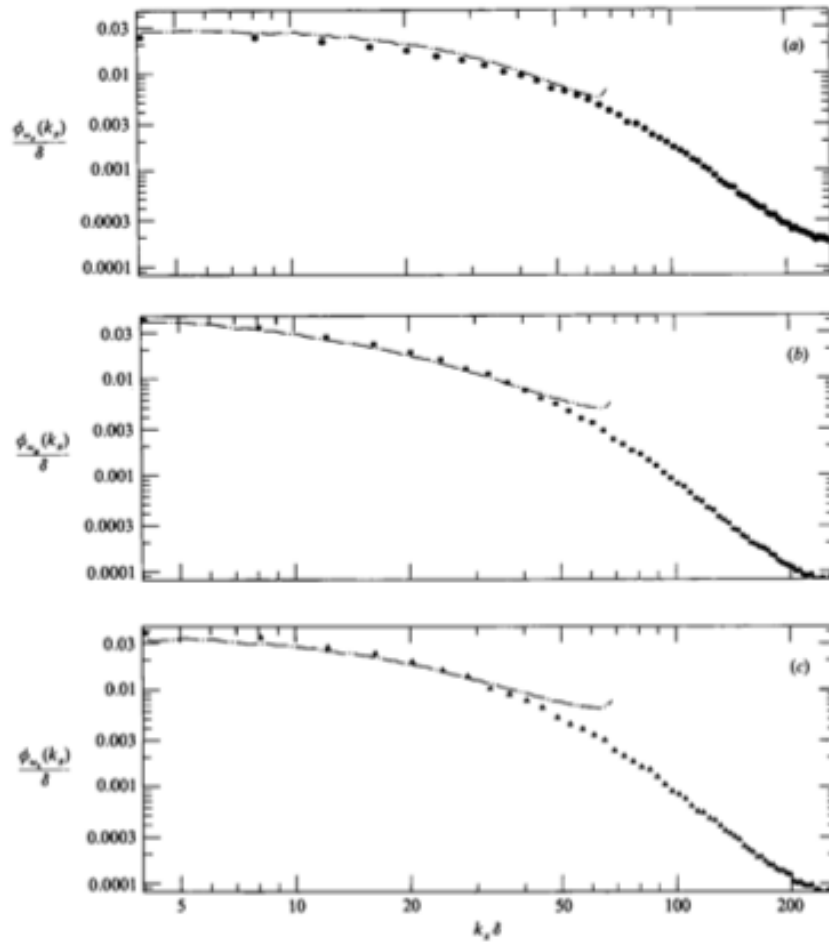


FIGURE 19. Measured one-dimensional fluctuating vorticity component spectra at $y^* = 18$ compared to direct numerical simulations of P. R. Spalart (1990, private communication) at $y^* = 15$.

Balint, Vukoslavčević & Wallace (1991) JFM 228
 Spalart (1988) JFM 187

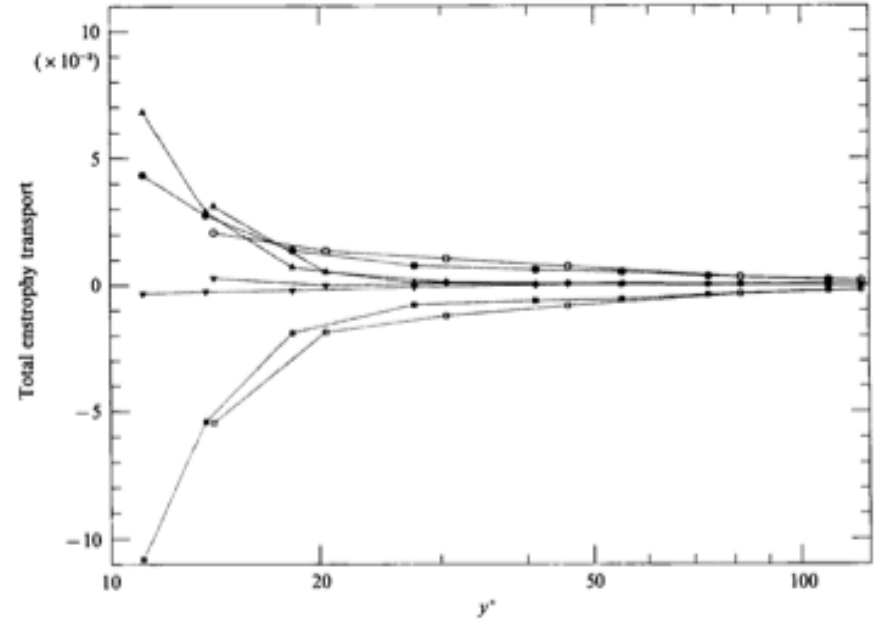


FIGURE 21. Measured terms in equation (7) for the transport of total enstrophy normalized with inner scaling u_i and ν . Closed symbols, present measurements; open symbols, Balint *et al.* (1990): (∇ , ∇), advection (term (7) I); ($\bullet$, $\circ$), rotation and stretching/compression (term (7) II); ($\blacktriangle$, $\triangle$), viscous diffusion (term (7) III); ($\blacksquare$, $\square$), viscous dissipation (term (7) IV).

$$\underbrace{U_j \frac{\partial}{\partial x_j} (\frac{1}{2} \Omega_i \Omega_i)}_I = \underbrace{\Omega_i \Omega_j \frac{\partial U_i}{\partial x_j}}_{II} + \underbrace{\nu \frac{\partial^2 (\frac{1}{2} \Omega_i \Omega_i)}{\partial x_j \partial x_j}}_{III} - \underbrace{\nu \left(\frac{\partial \Omega_i}{\partial x_j} \frac{\partial \Omega_i}{\partial x_j} \right)}_{IV},$$

- I: the rate of advection of total enstrophy;
- II: the rate of rotation and stretching/compression of total enstrophy by the velocity gradient field;
- III: the rate of viscous diffusion of total enstrophy; and
- IV: the rate of viscous dissipation of total enstrophy.

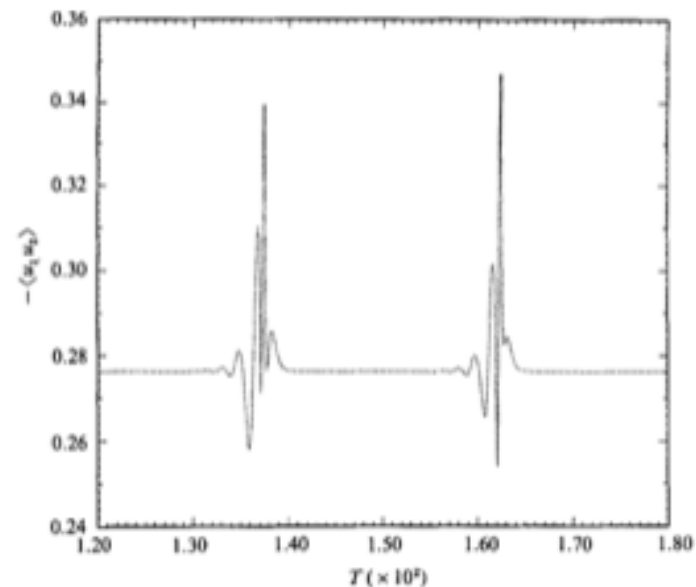


FIGURE 21. The Reynolds stress $\langle u_1 u_2 \rangle$ at $y^+ = 35$ vs. time for Heisenberg parameter showing two bursts.

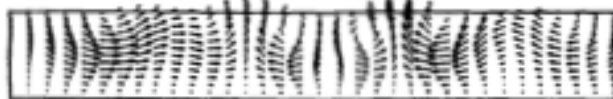


FIGURE 20. Vector representation of u_2, u_3 in a (x_2, x_3) -plane

Aubry, Holmes, Lumley & Stone (1988) JFM 192

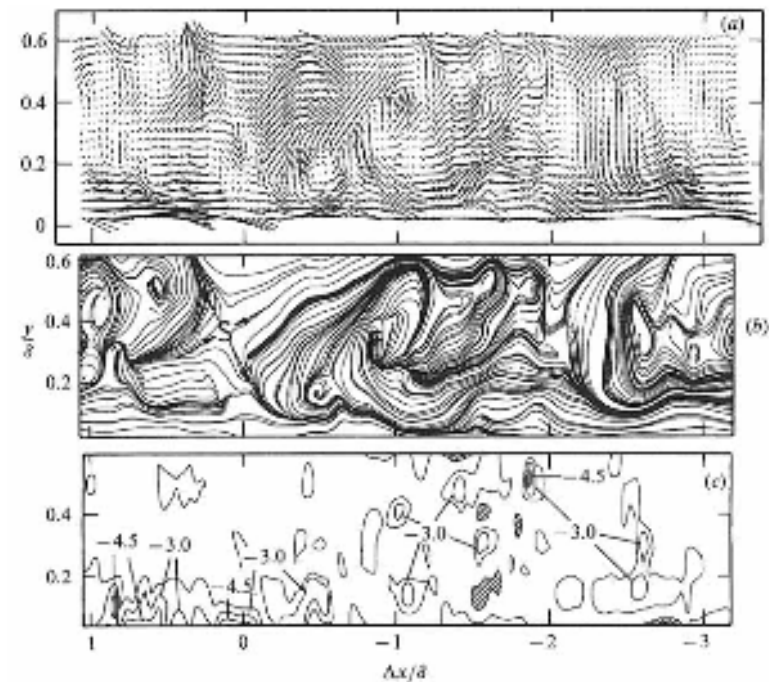


FIGURE 3. (a) Instantaneous velocity vectors, (b) sectional streamlines and (c) contours of approximate spanwise vorticity $\omega_s \delta / U_1$ calculated from the vectors in (a). The information is viewed in a frame of reference which translates to the left with $U_c = 0.8U_1$. $Re = 1360$. Note: hatched contours have a value of $+1.5$. Unlabelled contours have a value of -1.5 .

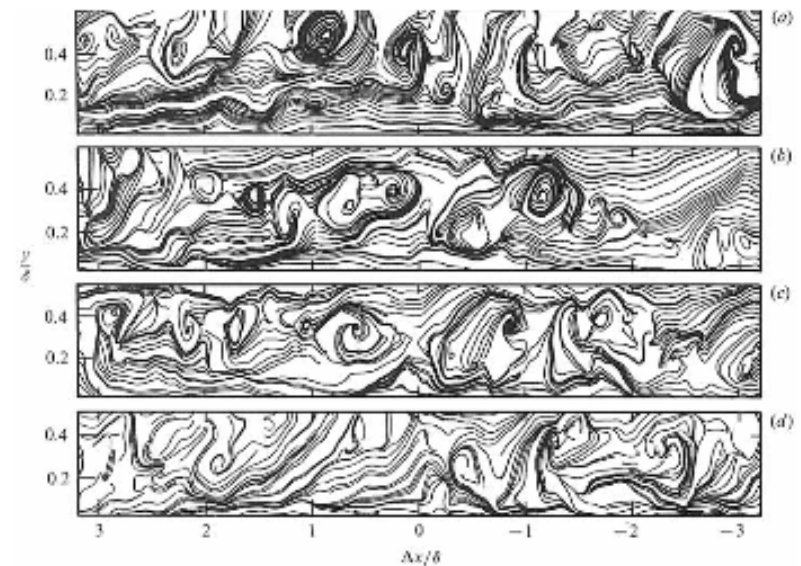


FIGURE 5. Instantaneous sectional streamlines in a frame of reference translating to the left with a velocity $U_c = 0.8U_1$ for different Reynolds numbers. (a) $Re = 1360$; (b) 2180; (c) 6030; (d) 9630.

Antonia, Bisset & Browne (1990) JFM 213

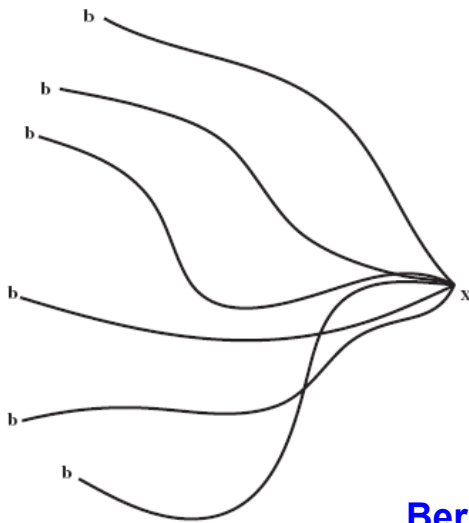


Fig. 6.2 Ensemble of paths arriving at x.

Bernard & Handler (1990) JFM 220

$$\overline{u_a u_a} = \overline{u_b u_a} + \overline{v_a (\overline{U_b} - \overline{U_a})} - \int_{-\tau}^0 \frac{1}{\rho} v(0) \frac{\partial p}{\partial x}(s) ds + \int_{-\tau}^0 \nu v(0) \nabla^2 U(s) ds.$$

Lagrangian decomposition of Reynolds stress

$$\overline{u_a u_a} = \overline{u_b u_a} + \overline{v_a (\overline{U_b} - \overline{U_a})} + \overline{v_a (\overline{U_a} - \overline{U_b})}$$

displacement transport acceleration transport

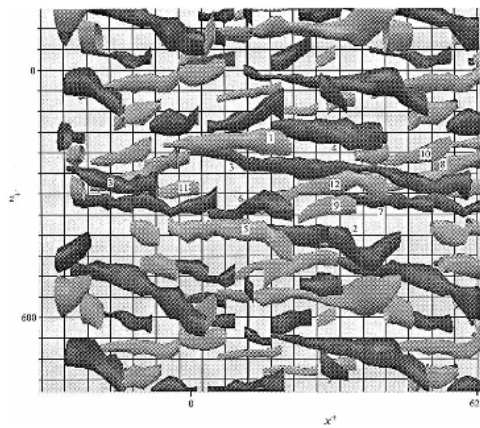


FIGURE 5. Plan view of complete set of vortices visualized using approximate core dimensions. Dark structures have negative streamwise vorticity, light structures have positive streamwise vorticity.

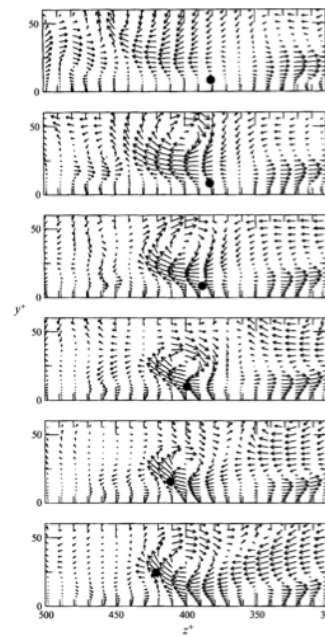


FIGURE 20. Ejection event in figure 19 viewed from end-on velocity vector plot.

FIGURE 5. Quadrant breakdown of the p.d.f. of particle displacement at $y^* = 12.0$: (a) Q1; (b) Q2; (c) Q3; (d) Q4; (e) total.

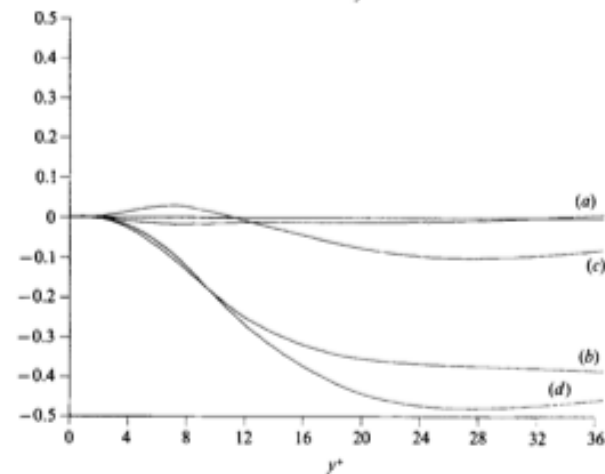
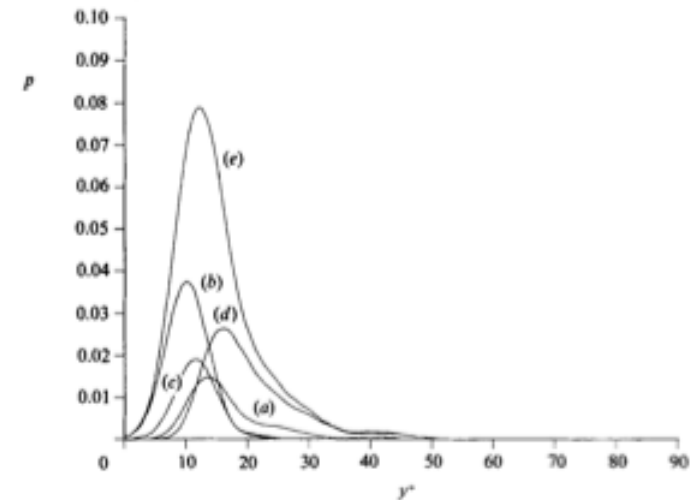


FIGURE 15. Spatial dependence of terms in Reynolds stress decomposition (7): (a) $\overline{u_b u_a}$; (b) $\overline{v_a (\overline{U_b} - \overline{U_a})}$; (c) $\overline{v_a (\overline{U_a} - \overline{U_b})}$; (d) $\overline{v_a v_a}$.

Bernard, Handler & Thomas (1993) JFM 253

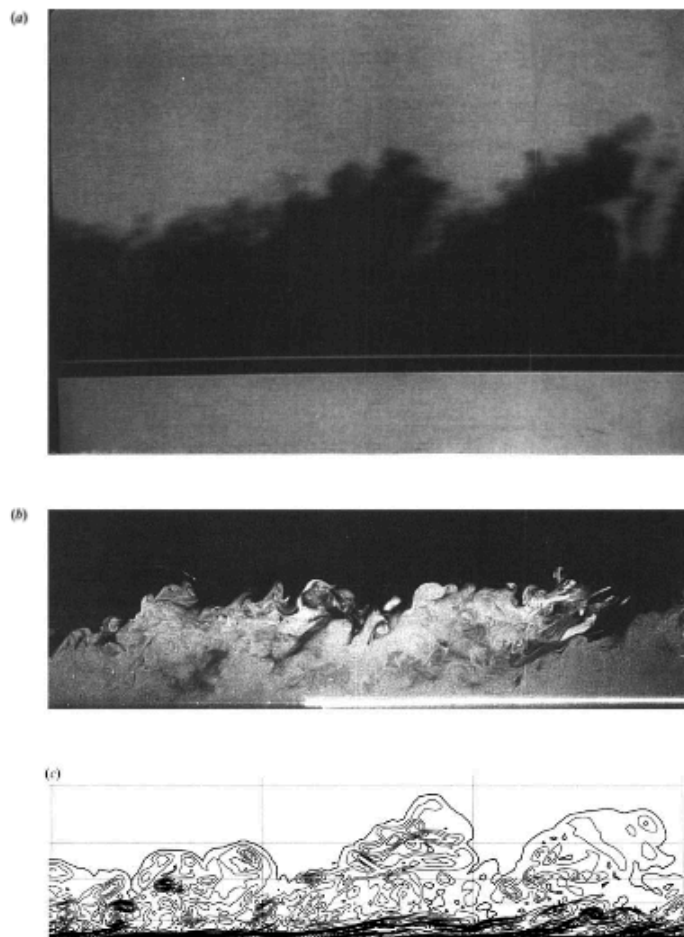


FIGURE 20. (a) Streamwise cross-section of a supersonic boundary layer with $Re_\delta = 25000$, obtained using Rayleigh scattering; Smith (1989). (b) Streamwise cross-section of a subsonic boundary layer with $Re_\delta = 4000$, obtained using oil droplet visualization; Falco (1977). (c) Streamwise cross-section of a computer-generated subsonic boundary layer with $Re_\delta = 670$, showing iso-vorticity contours. The flow is a direct Navier-Stokes turbulence simulation; Robinson (1989).

Spina, Donovan & Smits (1991) JFM 293

FIGURE 12. Ensemble-averaged $(\rho u)'$, v' , and $(\rho u)'v'$ signatures based upon the positive VITA technique (detection on $(\rho u)'$). —, $y/\delta = 0.2$; ·····, $y/\delta = 0.5$; ---, $y/\delta = 0.8$.

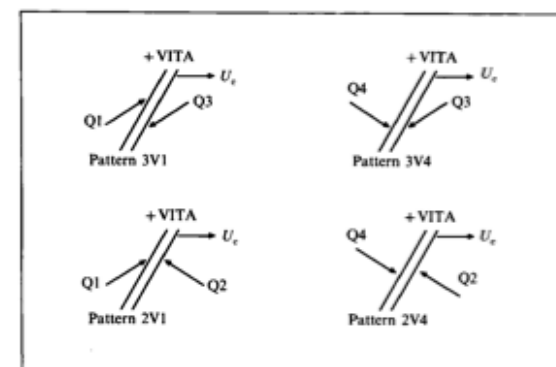
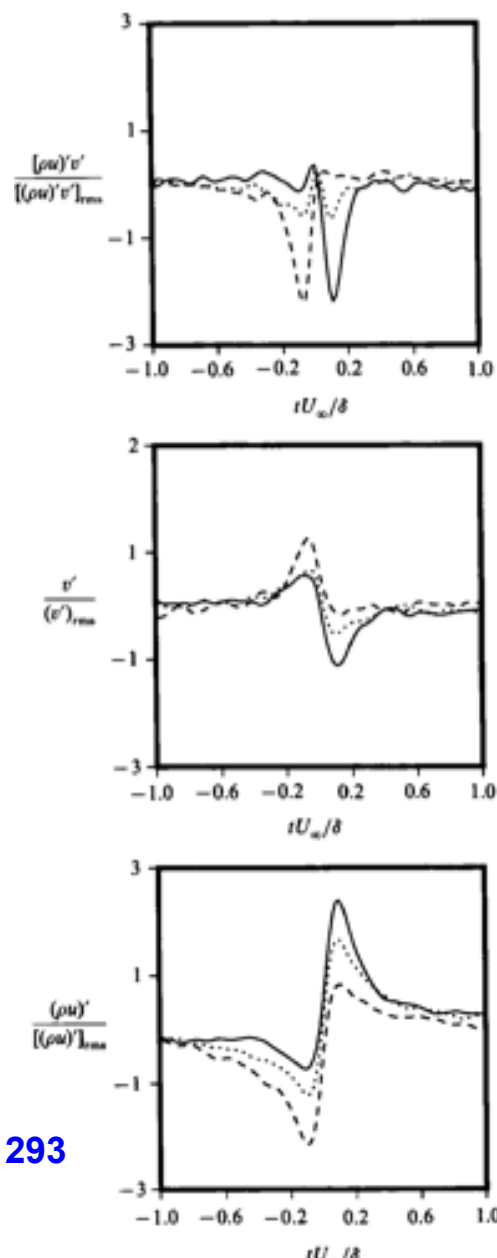


FIGURE 17. Schematic of the four possible triple event patterns showing the spatial location of the shear stress events relative to the +VITA event.

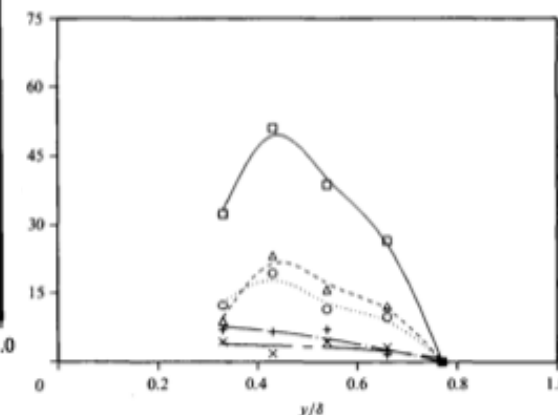
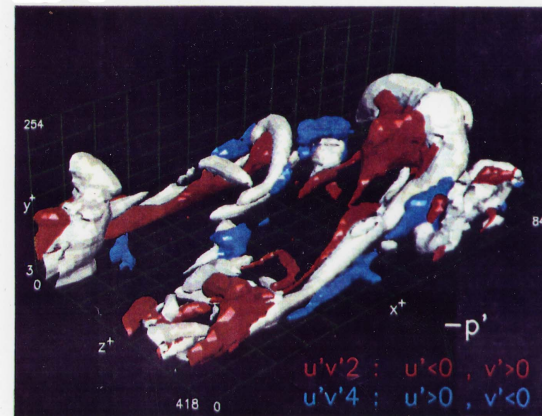
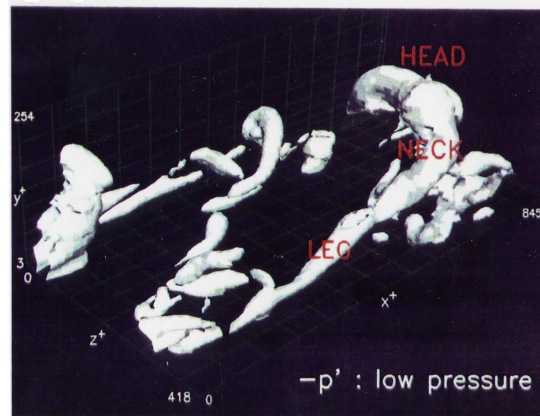
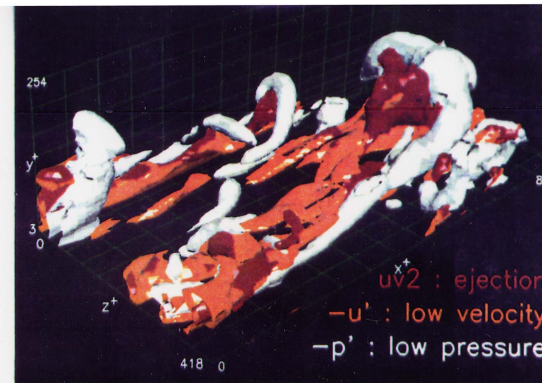
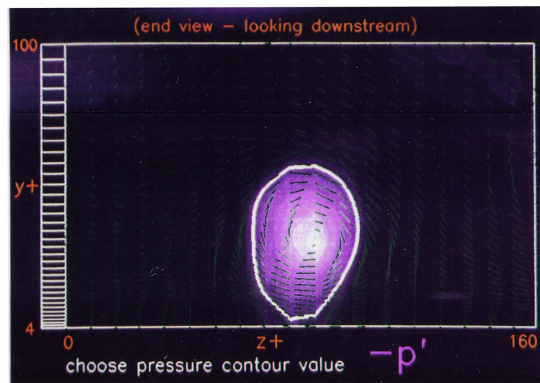
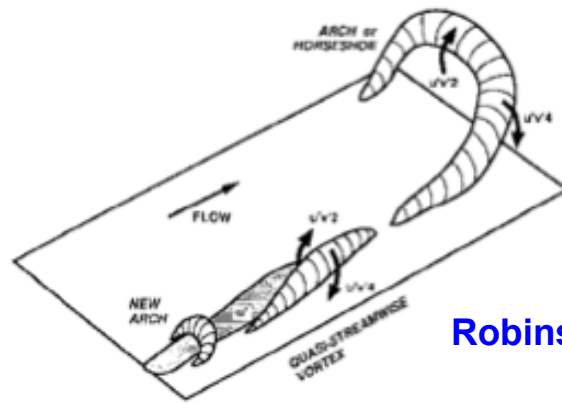


FIGURE 18. Percentage of +VITA events occurring in each of the triple event patterns defined by thresholding the shear stress. □—, Combined; ○·····, 2V4; △---, 2V1; +---, 3V4; ×---, 3V1.



Robinson (1990)



Robinson (1991) Ann. Rev. Fl. Mech. 23

Figure 13b Conceptual model of the kinematical relationships between (1) ejection/sweep motions and quasi-streamwise vortices in the near-wall region and (2) ejection/sweep motions and arch-shaped vortical structures in the outer region. Model proposed for low-Reynolds-number boundary layers (from Robinson 1990).

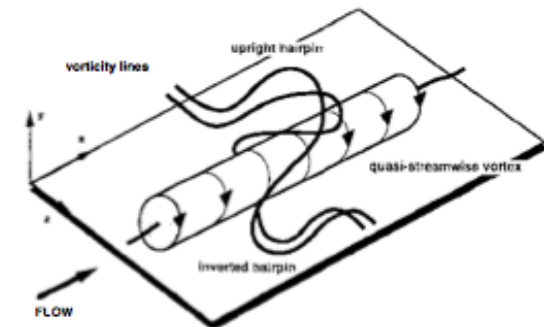


Figure 4 Vorticity lines traced from either side of a quasi-streamwise vortex in a boundary layer, showing upright- and inverted-hairpin shapes.

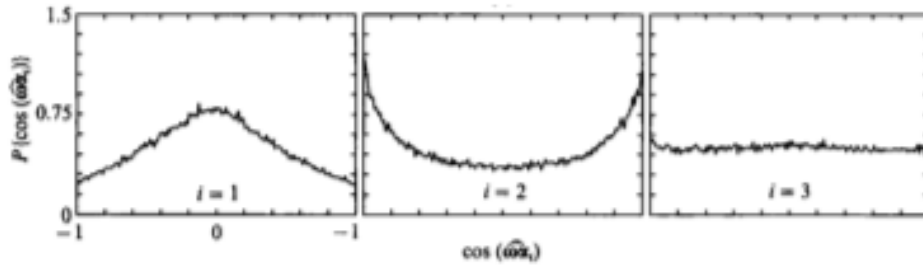
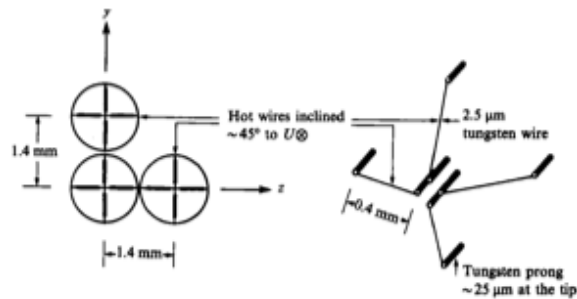
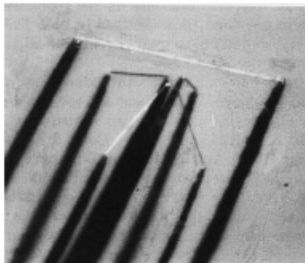


FIGURE 12. Probability density functions of cosine of the angle between vorticity vector and eigenvectors of the rate-of-strain tensor; $\alpha_1 < \alpha_2 < \alpha_3$; $x/M = 30$. (a) Grid flow, (b) boundary layer, $u/\bar{u} = 0.2$.



Tsinober, Kit and Dracos (1992) JFM 242

The exact Reynolds stress transport equation can be written

$$D_i \overline{u_i u_j} = \mu_{ij} + P_{ij} - \frac{\overline{u_i u_j}}{k} \epsilon - \partial_k \overline{u_k u_i u_j} - \frac{2}{3\rho} \delta_{ij} \partial_k \overline{u_k p} + \nu \nabla^2$$

where

$$P_{ij} = -\overline{u_i u_k} \partial_k U_j - \overline{u_j u_k} \partial_k U_i$$

is the rate of turbulence production by mean velocity gradients,

$$\mu_{ij} = -\frac{1}{\rho} \overline{u_i} \partial_j p - \frac{1}{\rho} \overline{u_j} \partial_i p + \frac{2}{3\rho} \delta_{ij} \partial_k \overline{u_k p} - \epsilon_{ij} + \frac{\overline{u_i u_j}}{k} \epsilon$$

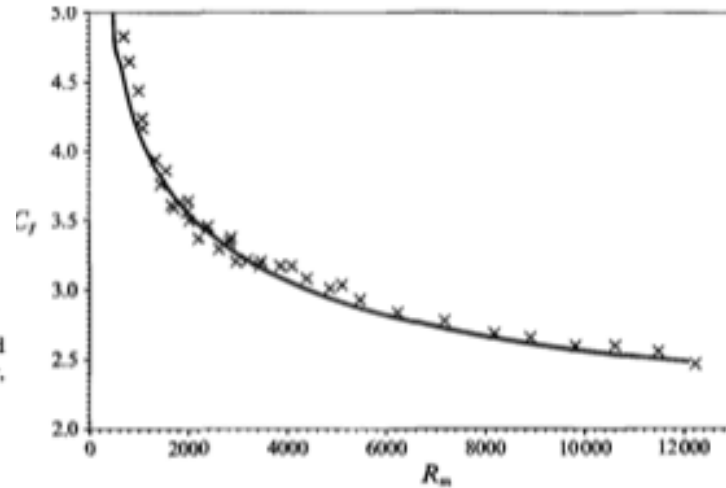


FIGURE 3. Friction coefficient in a zero-pressure-gradient boundary layer versus momentum-thickness Reynolds number. Experimental data is from Coles & Hirst; solid line is present model.

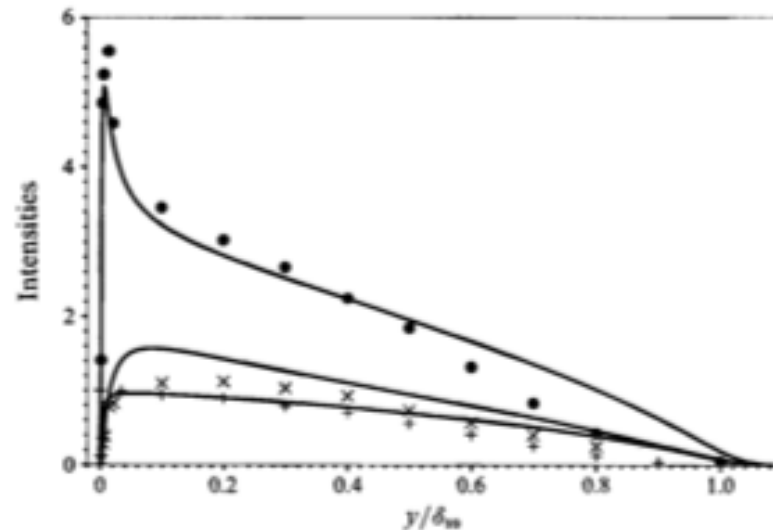


FIGURE 4. Profiles of k (●), ϵ (×) and $-\partial p/\partial x$ (+) at $R_m = 7150$ in a zero-pressure-gradient boundary layer. Experimental data were transcribed from Klebanoff.

Tensorially consistent near wall 2nd order closure model
without ad hoc damping functions

Durbin (1993) JFM 249

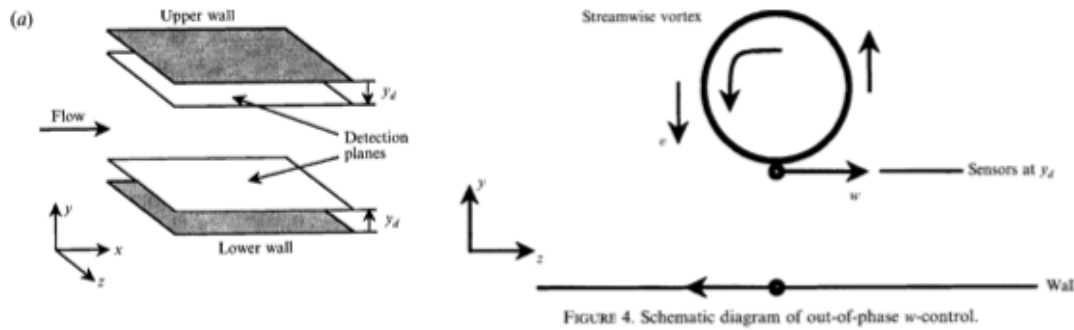


FIGURE 4. Schematic diagram of out-of-phase w -control.

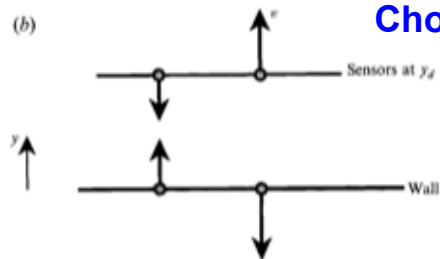


FIGURE 1. (a) Three-dimensional view of detection planes (b) schematic diagram of out-of-phase v -control.

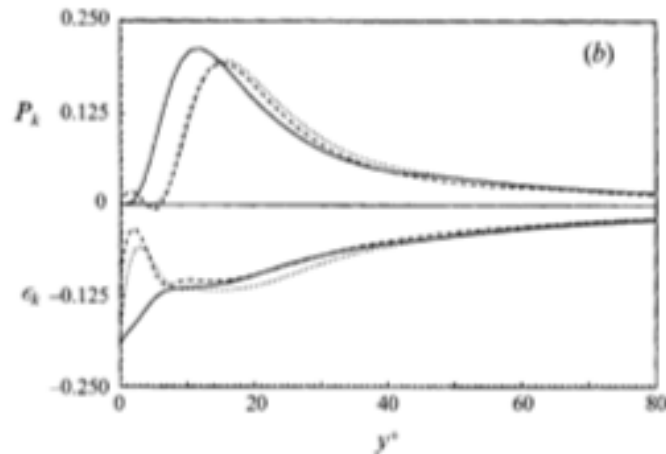


FIGURE 10. Production (P_k) and dissipation (ϵ_k) of the turbulence kinetic energy: —, no control; ---, v -control; ·····, w -control. (a) In global coordinates; (b) in wall coordinates. In coordinates, values are non-dimensionalized by the actual wall-shear velocity.

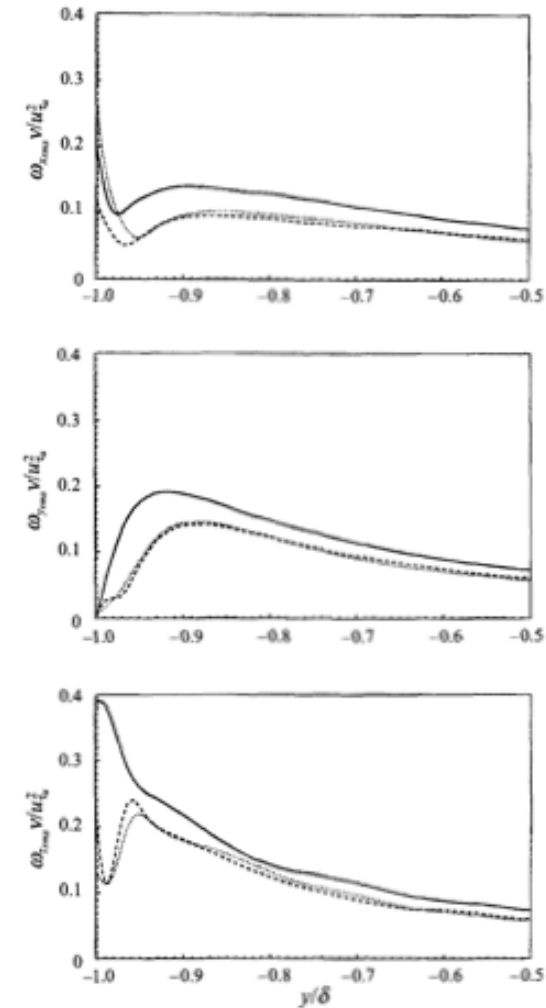


FIGURE 14. Root-mean square vorticity fluctuations normalized by the wall-shear velocity in global coordinates: —, no control; ---, v -control; ·····, w -control. Note that $y/\delta = -1$ corresponds to the lower location.

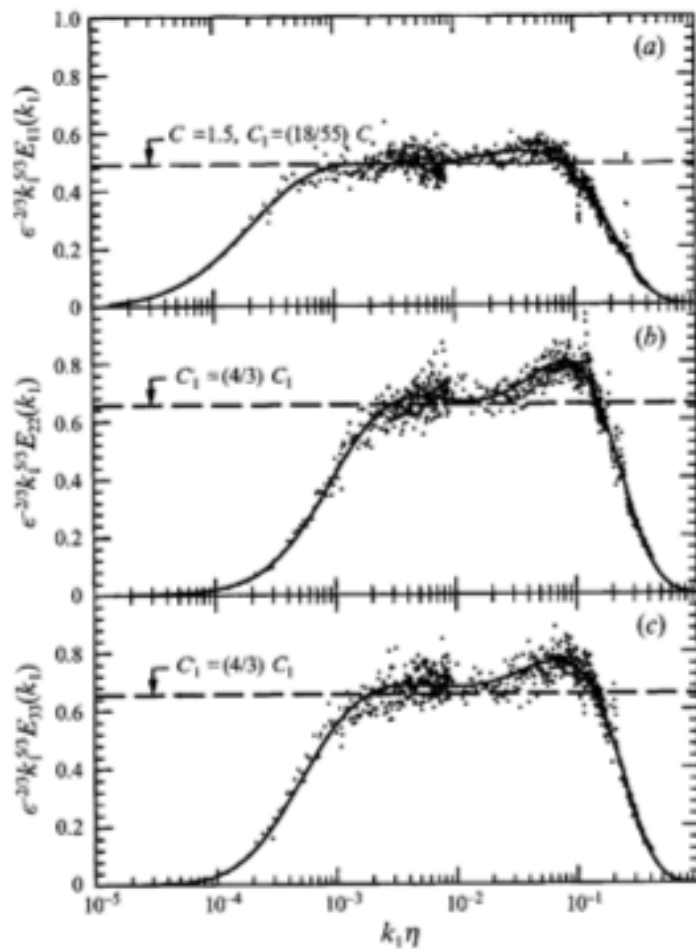


FIGURE 13. Compensated longitudinal and transverse spectra measured at mid-layer for the high-speed case ($y = 400$ mm, $y^+ \approx 62000$, $R_\tau \approx 1450$). Only the data for wavenumber range $k_i \eta < 0.25$ can be accepted. Solid lines are the ninth-order, least-square, log-log polynomial fits to the spectral data. (a) u_x -spectrum; (b) u_y -spectrum; (c) u_z -spectrum.

$$E_{u_y}(k_x) = E_{u_z}(k_x) = \frac{1}{4} \int_{k_x}^{\infty} \frac{E(k)}{k} (k^2 + k_x^2) dk$$

Wallace & Ong (2008) Phys. Fl. 20

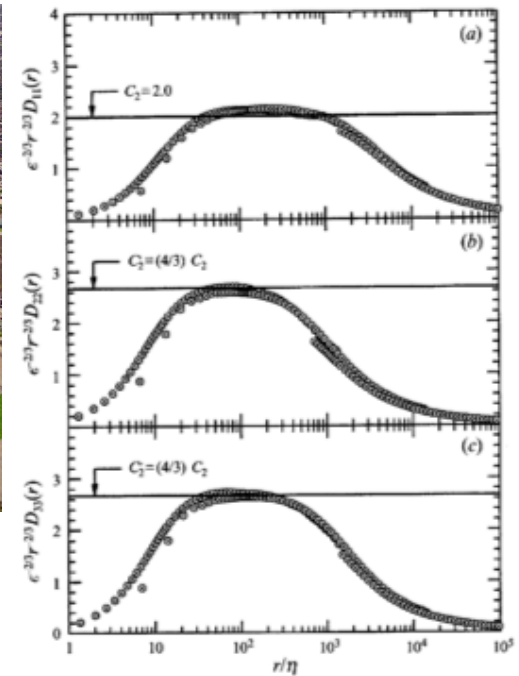
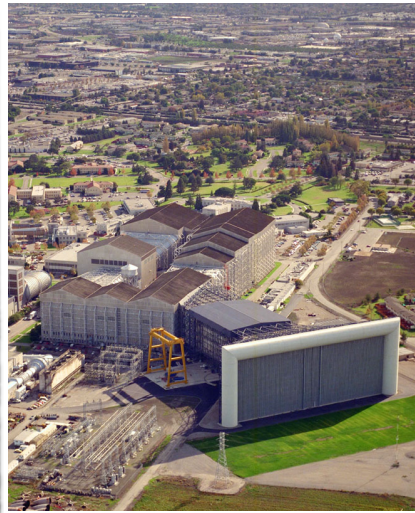


FIGURE 17. Compensated second-order structure functions for longitudinal and transverse velocity fluctuations measured at mid-layer for the low-speed case ($y = 515$ mm, $y^+ \approx 16200$, $R_\tau \approx 600$). Dissipation is from the third-order structure function. (a) u_x -structure function; (b) u_y -structure function; (c) u_z -structure function.

Saddoughi & Veeravalli (1994) JFM 268

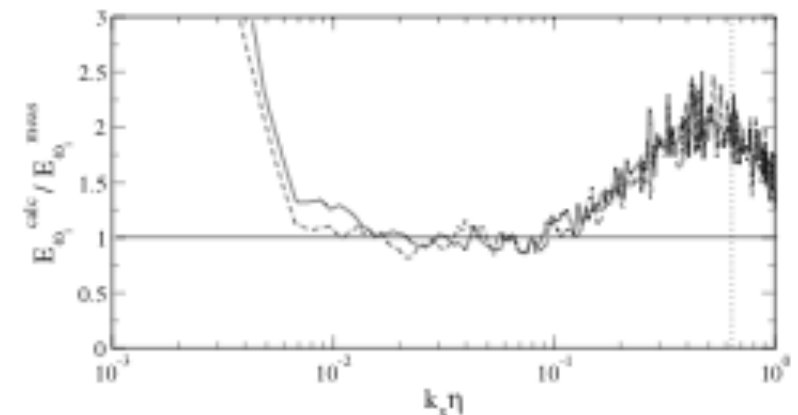


FIG. 6. Distributions of the ratios of wall normal and spanwise vorticity spectra calculated from Eq. (21) to their measured values: (—) $i=y$; (---) $i=z$.

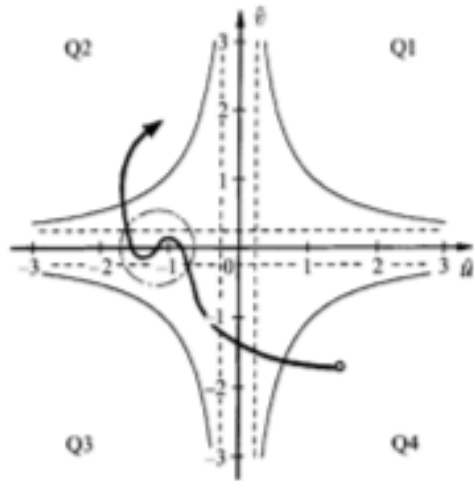


FIGURE 3. Trajectory analysis technique (TRAT) based on quadrant-sequences on the (u, v) -plane. —, $H = 1.07$; ---, $h = 0.25$.

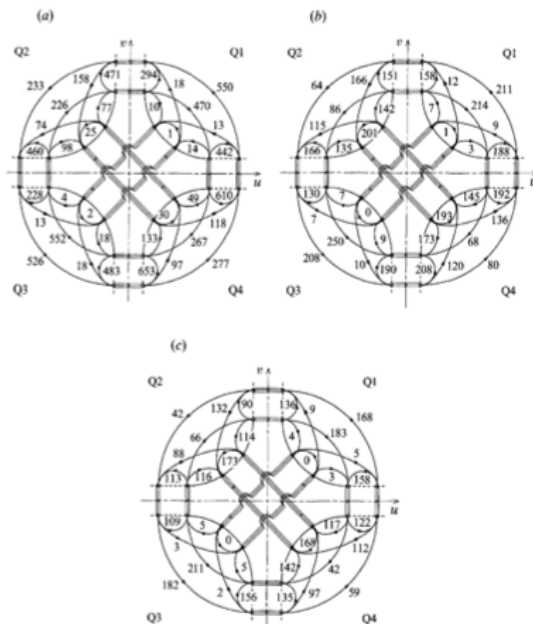


FIGURE 5. Trajectories of turbulent motions in the near-wall region ($y^+ = 18.5$). (a) $(h, H) = (0, 0)$, $N_{\text{total}} = 7712$; (b) $(h, H) = (0.25, 0)$, $N_{\text{total}} = 4155$; (c) $(h, H) = (0.25, 1.07)$, $N_{\text{total}} = 3267$.

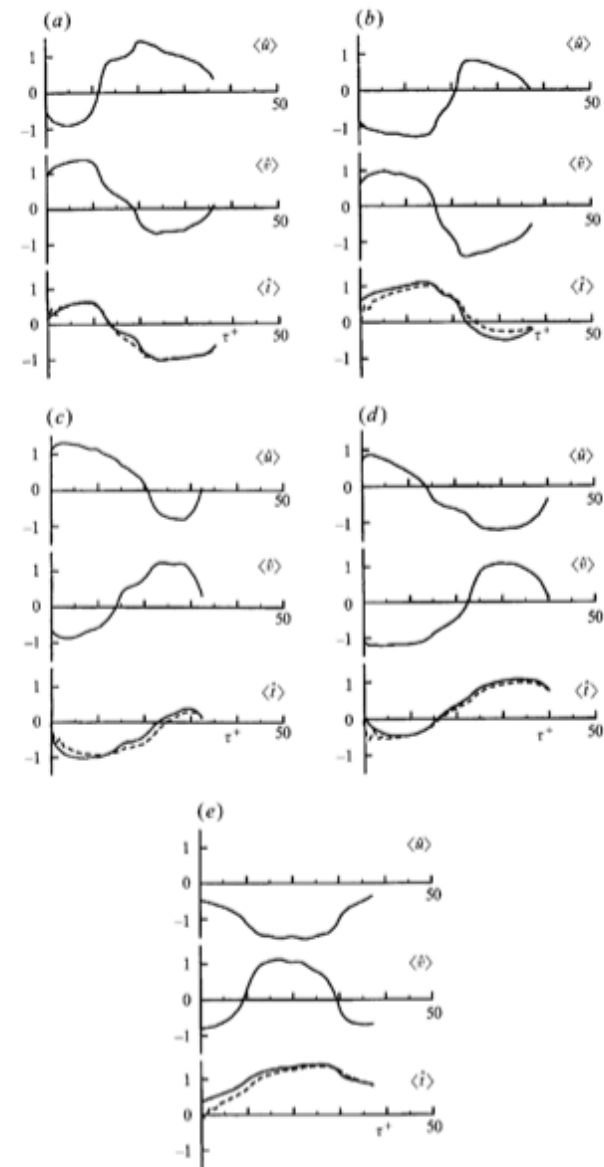


FIGURE 13. Predictions of near-wall temperature fluctuations associated with the key flow patterns using the autoregressive (AR) model: —, measurements; ---, AR model prediction. (a) Q2-Q1-Q4; (b) Q2-Q3-Q4; (c) Q4-Q1-Q2; (d) Q4-Q3-Q2; (e) Q3-Q2-Q3.

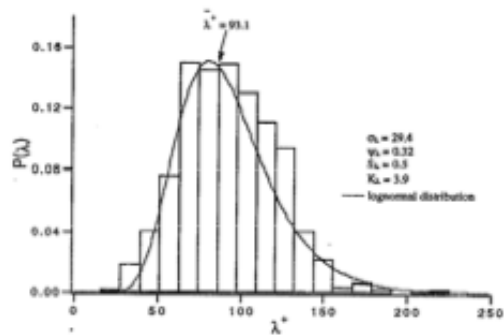
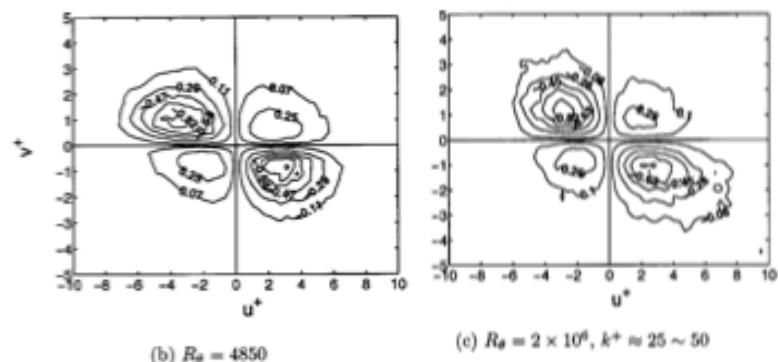


FIG. 4. Probability density histogram of spanwise streak spacing at $R_\theta = 1.5 \times 10^6$, with a sample size of 1072. The symbols σ_λ , ϕ_λ , S_λ , and K_λ define the standard deviation, coefficient of variation (σ_λ/λ^+), skewness, and kurtosis, respectively. The dotted line describes a lognormal distribution using λ^+ and ϕ_λ , as suggested by Smith and Metzler.²

Klewicki, Metzger, Keiner & Thurlow (1995) Phys. Fl. 7



Priyadarshana & Klewicki (2004) Phys. Fl. 16

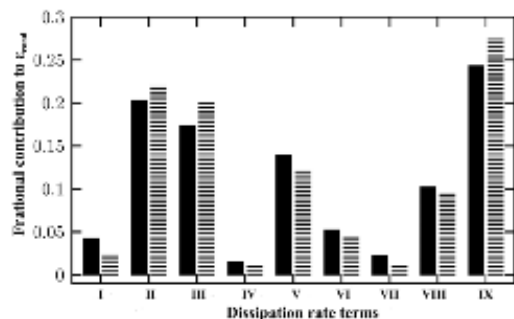


Fig. 14. Average fractional contribution of each of the nine squared velocity gradients [Roman numeral subscripted terms in (8)] to ε_{cmf} during periods of high ε at $R_\theta \sim 10^6$ and $y^+ = 45$. Solid bars are based on all values exceeding the ε threshold; hashed bars also require that ε exceed the threshold for at least 1.33 ms.

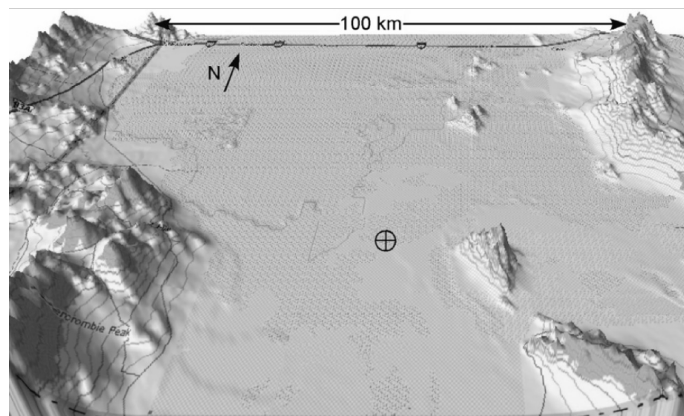


FIG. 3. Inner normalized plot of rms streamwise velocity vs position above the surface.

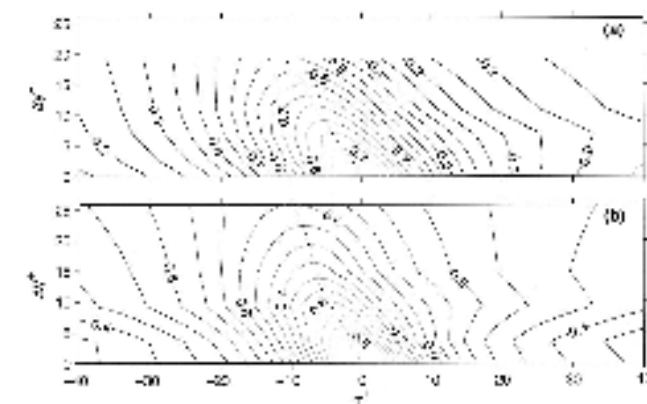


FIG. 15. Space-time autocorrelations of u . Dotted lines denote the locus of maximum correlation. Reference locations are identical to those used in Fig. 11. (a) $R_\theta = 2 \times 10^3$. (b) $R_\theta = 5 \times 10^6$.

Metzger & Klewicki (2001) Phys. Fl. 13

$$\begin{aligned} \bar{\varepsilon}/v &= 2 \left(\overline{\left(\frac{\partial u}{\partial x} \right)^2} \right)_I + \left(\overline{\left(\frac{\partial u}{\partial y} \right)^2} \right)_{II} + \left(\overline{\left(\frac{\partial u}{\partial z} \right)^2} \right)_{III} + \left(\overline{\left(\frac{\partial v}{\partial x} \right)^2} \right)_{IV} \\ &+ 2 \left(\overline{\left(\frac{\partial v}{\partial y} \right)^2} \right)_V + \left(\overline{\left(\frac{\partial v}{\partial z} \right)^2} \right)_{VI} + \left(\overline{\left(\frac{\partial w}{\partial x} \right)^2} \right)_{VII} + \left(\overline{\left(\frac{\partial w}{\partial y} \right)^2} \right)_{VIII} \\ &+ 2 \left(\overline{\left(\frac{\partial w}{\partial z} \right)^2} \right)_{IX} + 2 \overline{\left(\frac{\partial u}{\partial y} \right) \left(\frac{\partial v}{\partial x} \right)}_{IX} + 2 \overline{\left(\frac{\partial u}{\partial z} \right) \left(\frac{\partial w}{\partial x} \right)}_{IX} \\ &+ 2 \overline{\left(\frac{\partial v}{\partial z} \right) \left(\frac{\partial w}{\partial y} \right)}_{XII} \end{aligned}$$

Folz & Wallace (2010) Physica D 239

Jeong, Hussain, Schoppa & Kim (1997) JFM 332

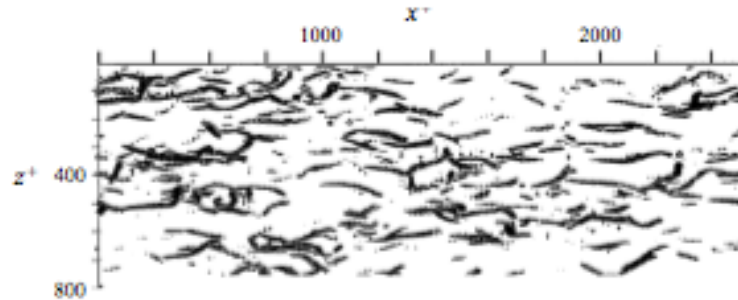


FIGURE 2. Top view of the isosurfaces of $\lambda_2 = -0.03$ in the range $0 < y^+ < 60$.

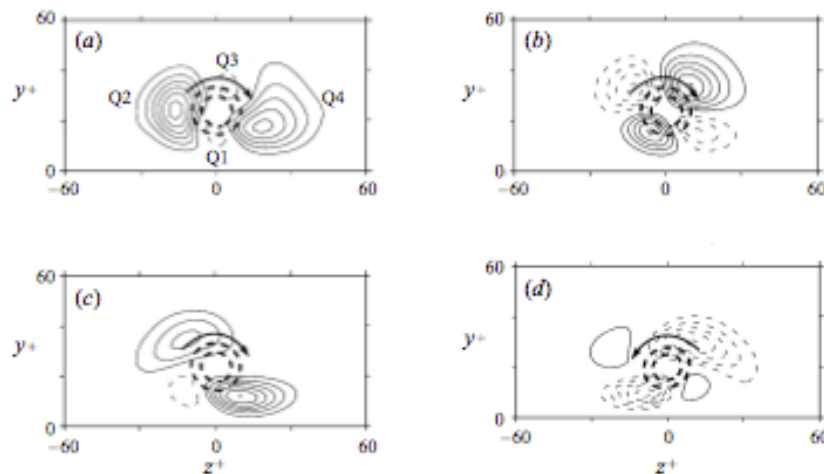


FIGURE 13. Coherent Reynolds stresses at $x = 0$ in E1: (a) $-(u - U)\langle v \rangle$ for SP, contour levels = $(0.3, -0.534, 1.94)$; (b) $-(v)\langle w \rangle$ for SP, contour levels = $(0.2, -0.868, 1.22)$; (c) $-(u - U)\langle w \rangle$ for SP, contour levels = $(0.7, -1.34, 4.23)$; (d) $-(u - U)\langle w \rangle$ for SN. Relative locations of Q1, Q2, Q3 and Q4 events with respect to the CS center are shown in (a).

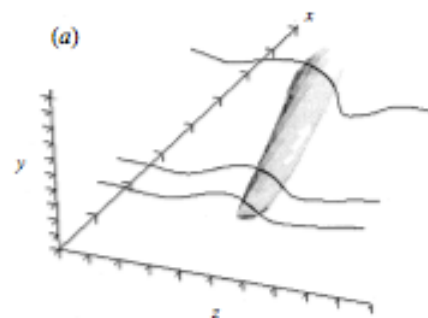


FIGURE 14. (a) Vortex lines traced outside CS

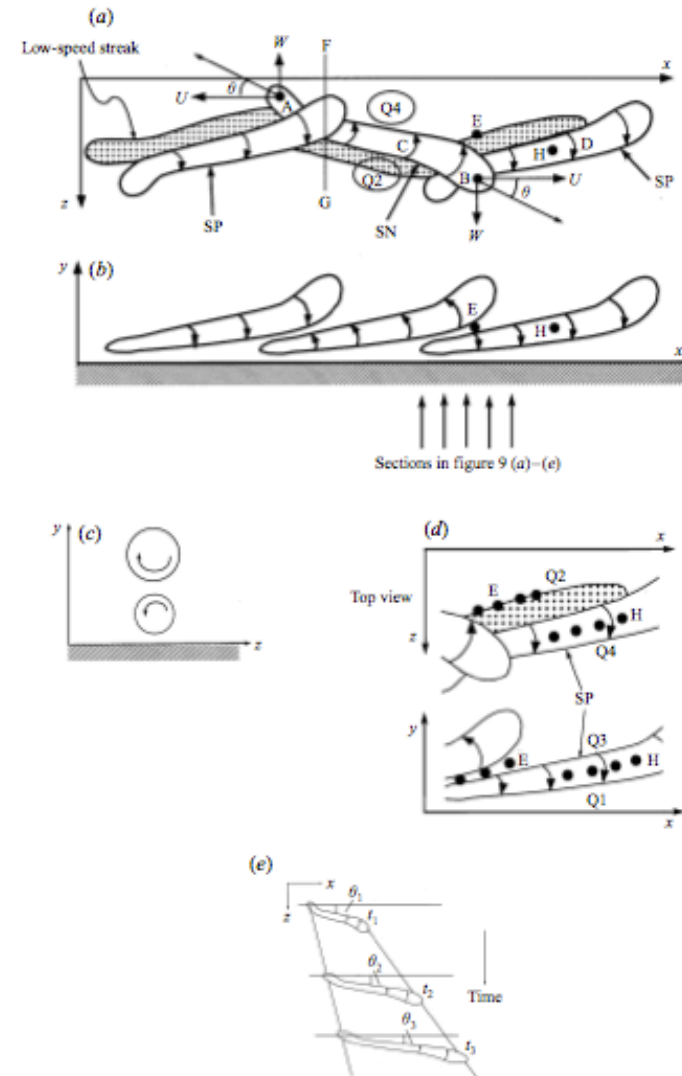


FIGURE 10. Conceptual model of an array of CS and their spatial relationship with experimentally observed events discussed in the text: (a) top view; (b) side view; (c) structures at cross-section FG in (a); (d) expanded views of structures C and D in (a,b), showing the relative locations of Q1, Q2, Q3, Q4, E and H. A schematic demonstrating the counteracting precession of SN in the (x, z) -plane due to background shear is shown in (e). The arrows in (b) denote the sections of figure 9(a-e).

Schoppa & Hussain (2002) JFM 453

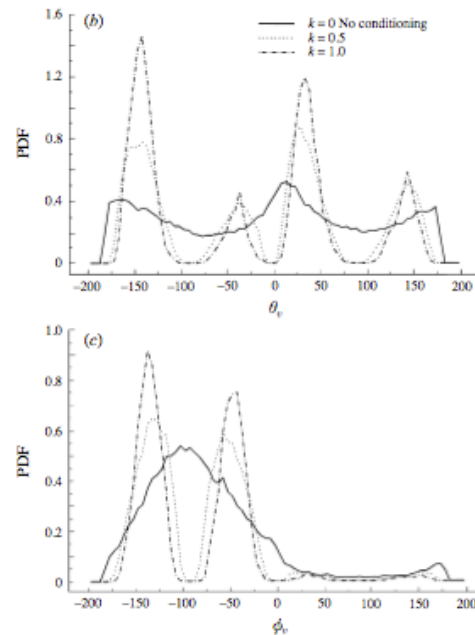
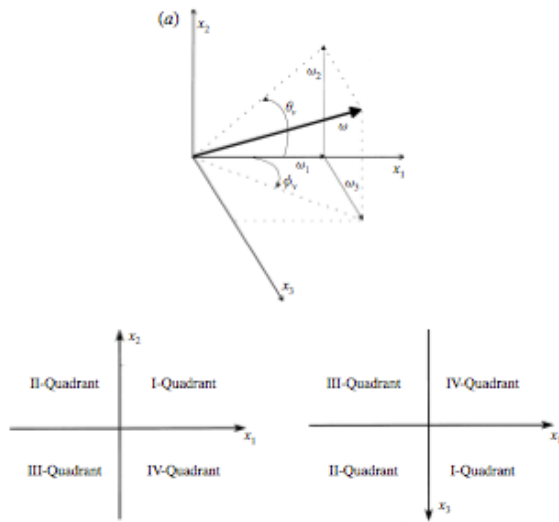


FIGURE 30. (a). Angular orientation of vorticity vector and definition of quadrants on vertical and horizontal planes. (b) Probability density function of vorticity vector orientation angle θ_1 in the (x_1, x_2) -plane at $x_3^+ = 12.5$, for threshold levels 0, 0.5 and 1. r.m.s. of ω_1 and for ω_2 . (c) Probability density function of vorticity vector orientation angle ϕ_e in the (x_1, x_2) -plane at $x_3^+ = 12.5$, for threshold levels 0, 0.5 and 1 r.m.s. of ω_1 and ω_2 .

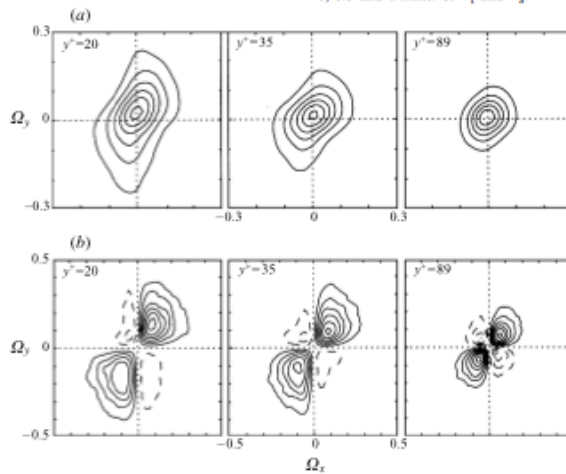


FIGURE 11. (a) JPDFs and (b) covariance integrands of Ω_x and Ω_y , non-dimensionalized by v/u_τ^2 . All vorticity and velocity gradients are normalized by this time scale here and in the following figures. Contour increments (for $y^+ = 20, 35$ and 89 , respectively) are (a) 3.3, 4.5, 9.0 and (b) 3.4×10^{-6} , 2.9×10^{-6} , 1.4×10^{-6} . The outer contours are one increment above zero.

$$\overline{\Omega_x \Omega_y} = \iint_{-\infty}^{\infty} \Omega_x \Omega_y P(\Omega_x, \Omega_y) d\Omega_x d\Omega_y$$

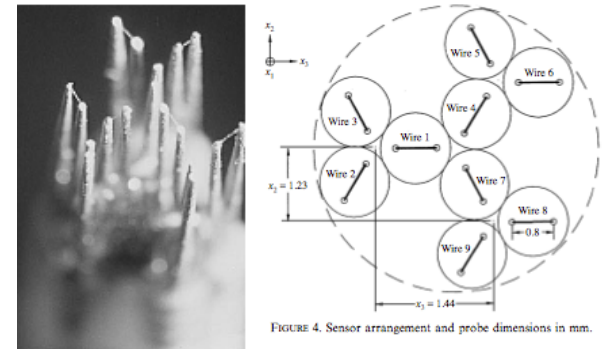


FIGURE 4. Sensor arrangement and probe dimensions in mm.

Honkan & Andreopolous (1997)
JFM 350

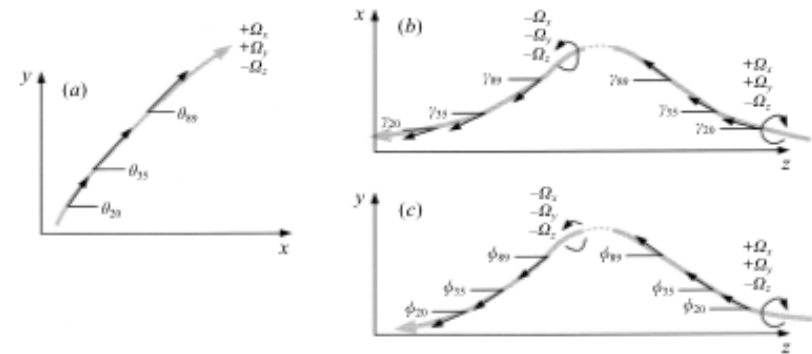
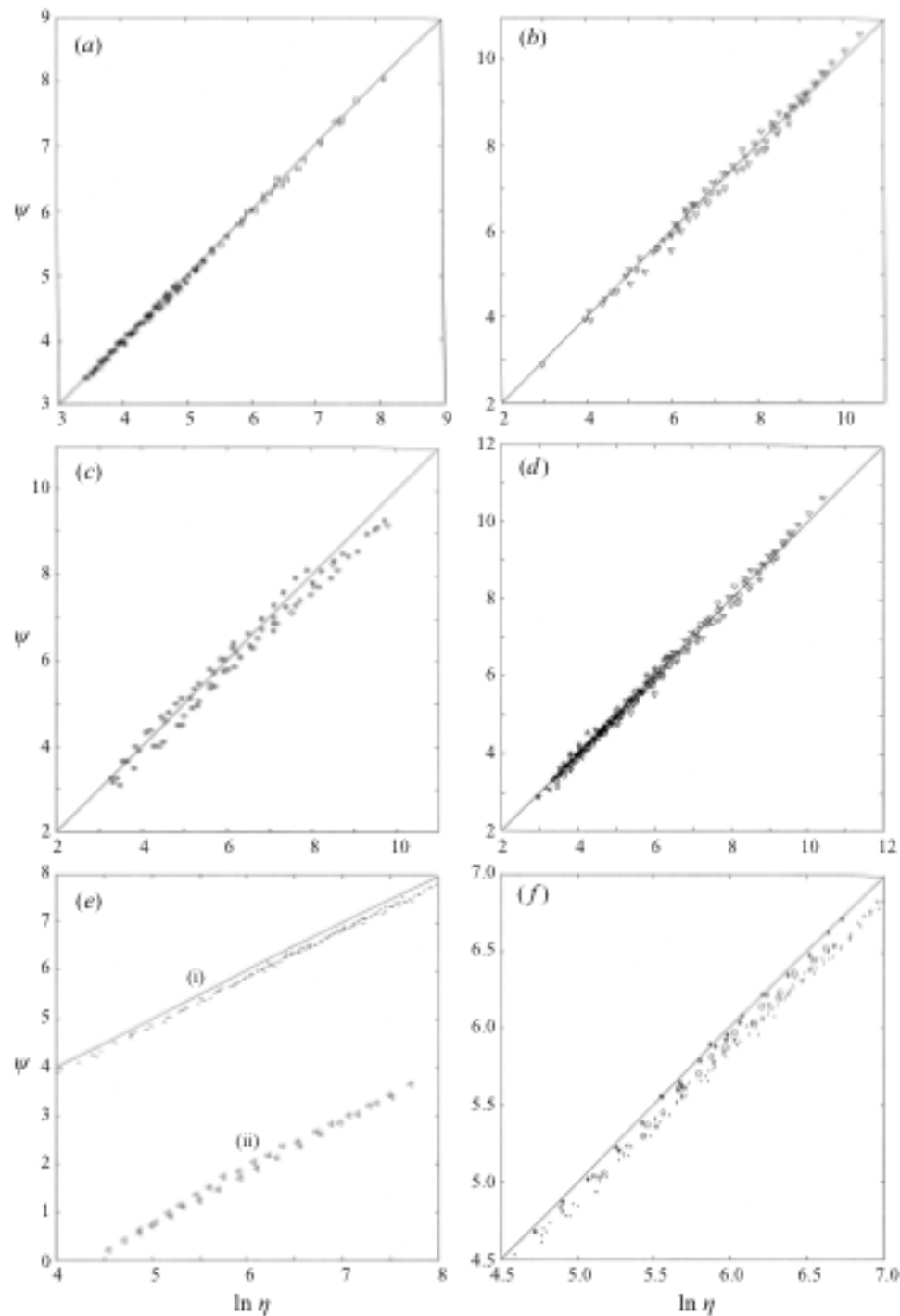


FIGURE 15. Projections of vorticity filament segments making the largest contributions to $\overline{\Omega_x \Omega_y}$, $\overline{\Omega_y \Omega_z}$ and $\overline{\Omega_x \Omega_z}$ at $y^+ = 20, 35$ and 89 . (a) Projection on (x, y) -plane where $\theta = \tan^{-1}(\Omega_y/\Omega_x)$: $\theta_{20} \approx 58^\circ$ (or -118°) at $y^+ = 20$, $\theta_{35} \approx 48^\circ$ (or -136°) at $y^+ = 35$ and $\theta_{89} \approx 48^\circ$ (or -137°) at $y^+ = 89$. (b) Projection on (x, z) -plane where $\gamma = \tan^{-1}(\Omega_z/\Omega_x)$: $\gamma_{20} \approx \pm 16^\circ$, $\gamma_{35} \approx \pm 27^\circ$ and $\gamma_{89} \approx \pm 42^\circ$. (c) Projection on (y, z) -plane where $\phi = \tan^{-1}(\Omega_z/\Omega_y)$: $\phi_{20} \approx \pm 27^\circ$, $\phi_{35} \approx \pm 35^\circ$ and $\phi_{89} \approx \pm 37^\circ$.

Ong & Wallace (1998) JFM 367



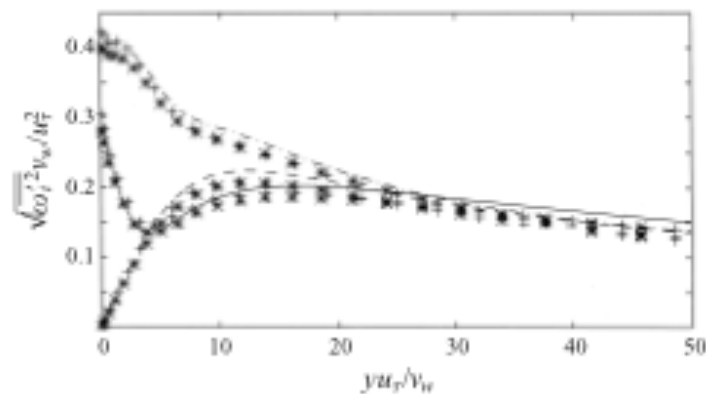
$$\eta = u_* y / \nu$$

$$\phi = \frac{u}{u_*} = \left(\frac{1}{\sqrt{3}} \ln Re + \frac{5}{2} \right) \eta^{3/2 \ln Re}$$

$$\psi = \frac{1}{\alpha} \ln \left(\frac{2\alpha\phi}{\sqrt{3} + 5\alpha} \right) = \ln \eta, \quad \alpha = \frac{3}{2 \ln Re}$$

Barenblatt, Chorin & Prostokishin (2000) JFM 410

FIGURE 16. (a) The experiments of: *, Erm & Joubert (1991); □, Smith (1994); ◁, Krogstad & Antonia (1998); and ▷, Petrie *et al.* (1990). (b) ▽, The data of Winter & Gaudet (1973). (c) *, The data of Bruns *et al.* (1973) and Fernholz *et al.* (1995). (d) The data of all experiments except of those by Naguib (1992) and Nagib & Hites (1995), Bruns *et al.* (1992) and Fernholz *et al.* (1995): ○, Collins *et al.* (1978); ▷, Petrie *et al.* (1990); +, Erm (1988); ◇, Patell *et al.* (1981); *, Djenidi & Antonia (1993); ×, Warnack (1994); ◁, Krogstad & Antonia (1998); ▽, Winter & Gaudet (1973). All the data in (a–d) collapse on the bisectrix of the first quadrant in accordance with the universal form (14) of the scaling law (5). (e) (i) The data of Naguib (1992) and Nagib & Hites (1995) show a systematic deviation from the bisectrix of the first quadrant. (ii) The data of Krogstad & Antonia (1998) related to rough walls: the experimental points lie much lower than bisectrix. For the evaluation of ψ the value $\alpha = 3/2 \ln Re_1$ was taken. (f) The data of Hancock & Bradshaw (1989) show the parallel shift from the bisectrix of the same order as in the experiments by Nagib & Hites: ●, Nagib & Hites; *, Hancock & Bradshaw, $u'/U = 0.0003, 0.024, 0.026$; ×, Hancock & Bradshaw, $u'/U = 0.040, 0.041$; ○, Hancock & Bradshaw, $u'/U = 0.058$.



$Re_\theta = 1577$
 $Mach = 2.5$

FIGURE 8. RMS of vorticity fluctuations. Lines correspond to the compressible simulation: —, $\overline{\omega_1^2}$; ---, $\overline{\omega_2^2}$; — — —, $\overline{\omega_3^2}$; +, Spalart ($Re_\theta = 1410$); *, Spalart ($Re_\theta = 670$).

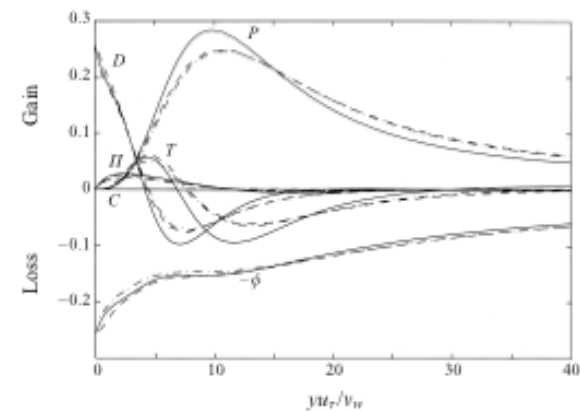


FIGURE 22. Turbulent kinetic energy budget: —, simulation data; ----, Spalart's data $Re_\theta = 1410$; — — —, Spalart's data $Re_\theta = 670$. Symbols are: C, Convective term; P, Generation term; T, Turbulent transport; II, Pressure terms; D, Viscous transport; $-\phi$, Viscous dissipation.

Guarini, Moser, Shariff & Wray (2000) JFM 414

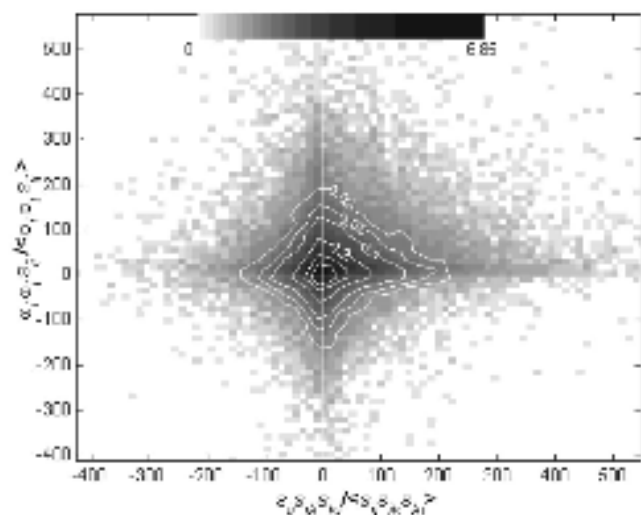


FIG. 2. Joint PDF/scatter plot of enstrophy production, $\omega_i \omega_j x_{ij}$, versus the production of strain $-(4/3)s_{ij}s_{ji}s_{kl}$. The density of the image corresponds to $\lg$ number of events.

$R_\lambda \sim 10^4$

Kholmyanshy, Tsinober & Yorish (2001) Phys. Fl. 13

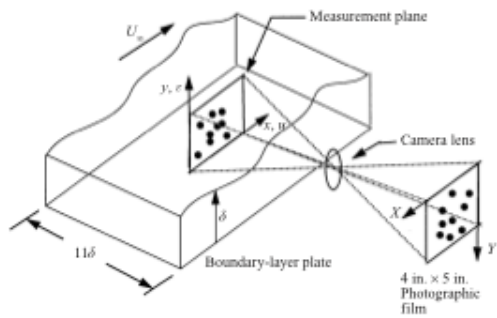


FIGURE 1. Schematic of PIV photographic recording system. The streamwise-wall-normal plane of a zero-pressure-gradient boundary layer is illuminated by a vertical laser light sheet and imaged by a side-viewing 4 in. x 5 in. photographic camera.

PIV

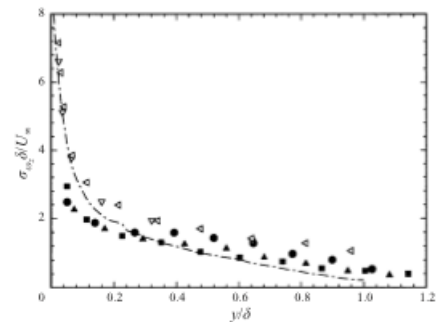


FIGURE 7. Root-mean-square spanwise vorticity scaled and plotted with outer variables ■, $Re_0 = 930$; ▲, 2370; ●, 6845; ▽, Bahint *et al.* (1991); ◄, Klewicki (1989) $Re_0 = 2870$; - - -, Spalart (1988) $Re_0 = 1410$.

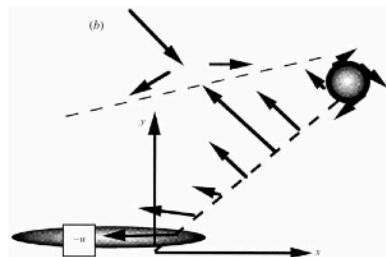
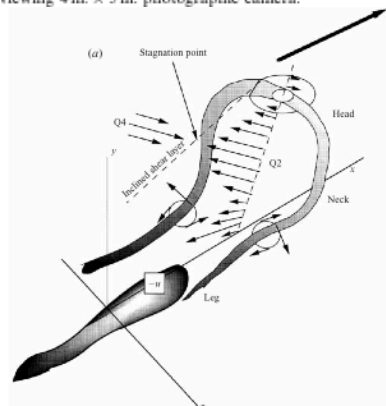


FIGURE 10. (a) Schematic of a hairpin vortex attached to the wall and the induced motion. (b) Signature of the hairpin vortex in the streamwise-wall-normal plane. The to the spanwise location of the plane, until it intersects the concentrated core of the hairpin.

Adrian (2007) Phys. Fl. 19

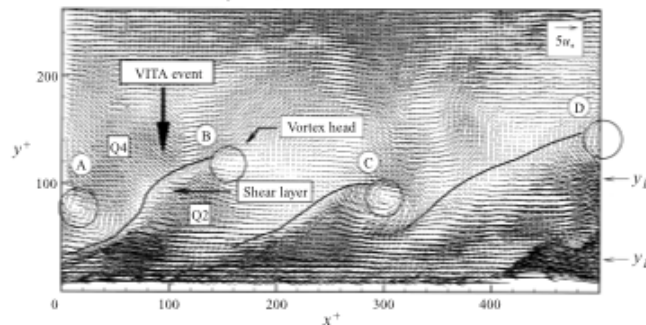
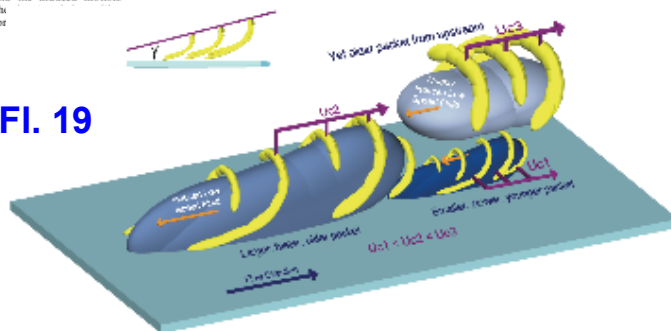


FIGURE 11. Near-wall realization at $Re_0 = 930$ showing four hairpin vortex signatures aligned in the streamwise direction. Instantaneous velocity vectors are viewed in a frame-of-reference moving at $U_c = 0.8 U_\infty$ and scaled with inner variables. Vortex heads and inclined shear layers are indicated schematically, along with the elements triggering a VITA event.

Adrian, Meinhart & Tompkins (2000) JFM 422

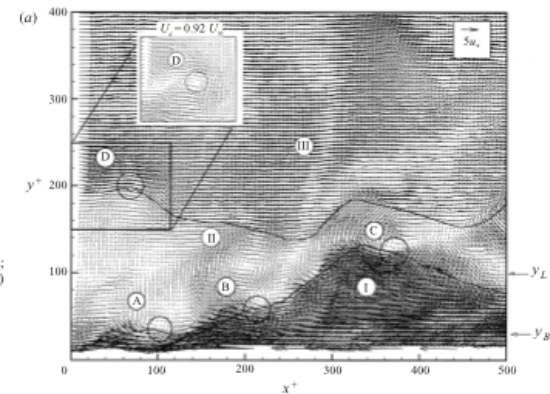
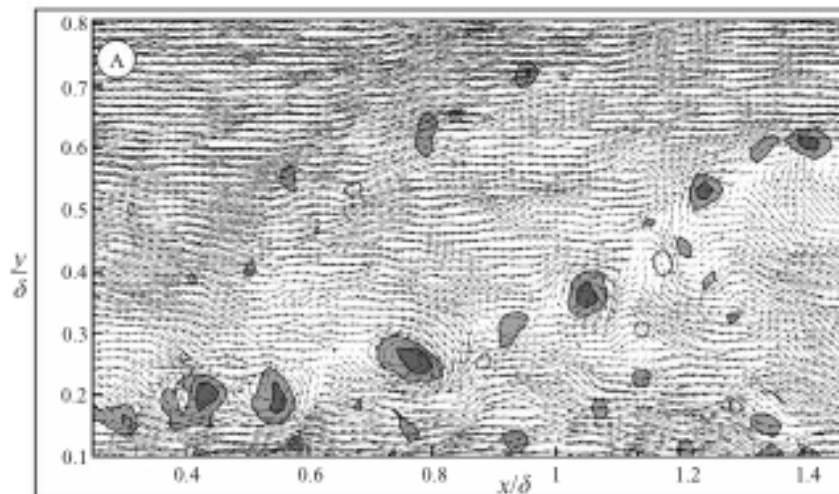


FIGURE 14. Realization of the $Re_0 = 930$ boundary layer showing hairpin vortex heads along the boundaries separating regions of uniform-momentum fluid. The black lines separate the flow field into zones, labelled I, II and III, in which the streamwise momentum is nearly uniform: (a) instantaneous velocity vector map viewed in a convecting frame of reference $U_c = 0.8 U_\infty$ and scaled with inner variables, (b) contours of constant u -momentum.



hairpin "packet"

$$A_{ij} = \partial U_i / \partial x_j$$

$$\lambda^3 + P\lambda^2 + Q\lambda + R = 0,$$

$$P = -A_{ii},$$

$$Q = \frac{1}{2}P^2 - \frac{1}{2}A_{ik}A_{ki},$$

$$R = -\frac{1}{3}P^3 + PQ - \frac{1}{3}A_{ik}A_{kl}A_{li},$$

$$D = \frac{2}{3}R^2 + Q^3$$

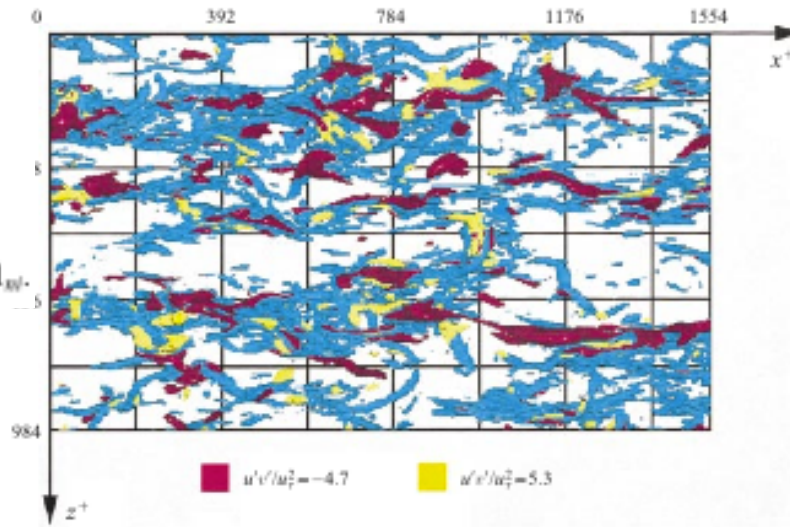


FIGURE 5. Top view of the computational domain showing regions of positive discriminant and their spatial association with Reynolds stress events ($u'v'$).

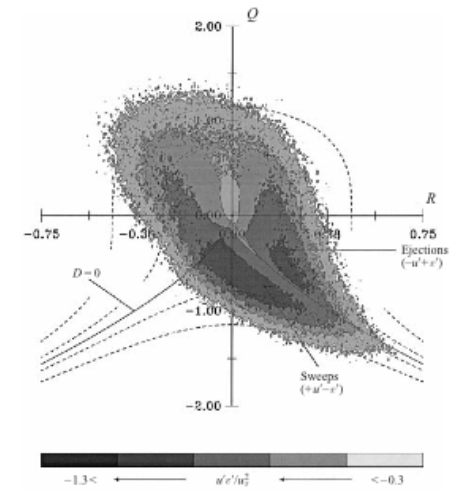


FIGURE 7. Time-averaged Reynolds-shear-stress ($u'v'$) generating events associated with the four incompressible flow patterns. Data taken from the entire boundary layer.

Chacin & Cantwell (2000) JFM 404

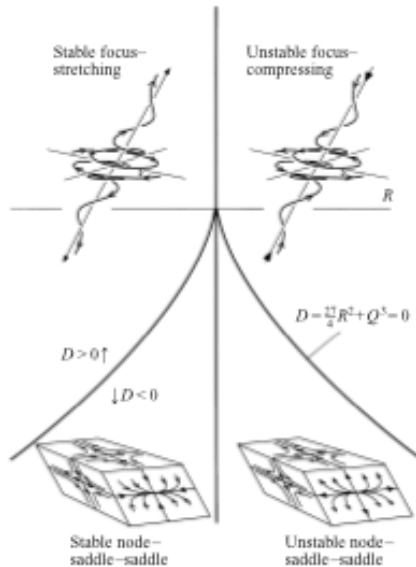


FIGURE 1. Summary of three-dimensional, incompressible flow patterns (from Soria *et al.* 1994).

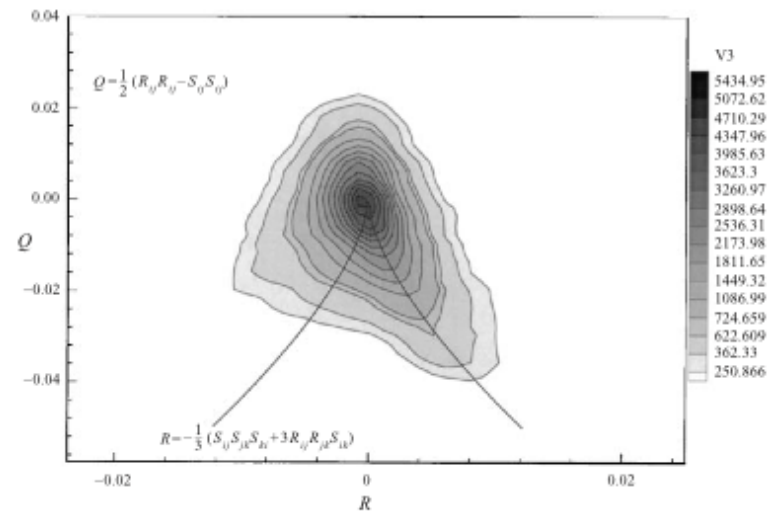


FIGURE 19. Joint probability density function of the Q and R invariants of velocity gradient tensor at $x_2^+ = 12.5$.

Andreopolous & Honkan(2001) JFM 439

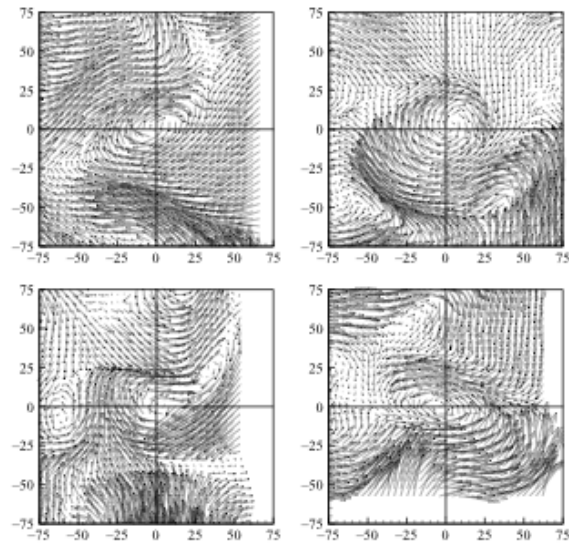


FIGURE 22. Examples of accepted eddy structures in the (e_z, e_y) -plane at $R_\theta = 7500$.

R_θ	(e_z, e_y)		(e_z, e_x)		(e_z, e_y)		(e_z, e_d)	
	V_-	V_+	V_-	V_+	V_-	V_+	V_-	V_+
7500	3613	1726	2386	2393	10979	10871	800	822
10 500	—	—	2096	2123	—	—	586	639
13 500	—	—	2423	2408	—	—	852	832
19 000	—	—	2303	2342	—	—	756	769

TABLE 6. Number of eddy structures detected.

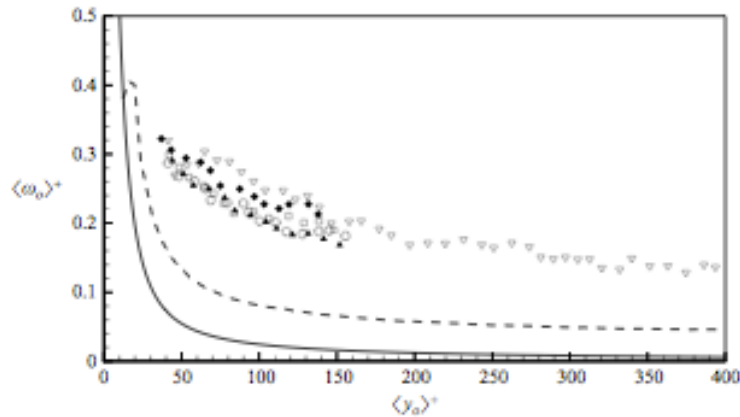


FIGURE 30. Mean vorticity profiles of eddy structures: ∇ , (e_z, e_y) -plane and $R_\theta = 7500$; $\blacklozenge$, (e_z, e_y) -plane and $R_\theta = 7500$; $\square$, (e_z, e_x) -plane and $R_\theta = 10\,500$; $\blacktriangle$, (e_z, e_x) -plane and $R_\theta = 13\,500$; $\circ$, (e_z, e_x) -plane and $R_\theta = 19\,000$; $---$, r.m.s. spanwise vorticity; $---$, Van Driest profile.

Carlier & Stanislas (2005) JFM 535

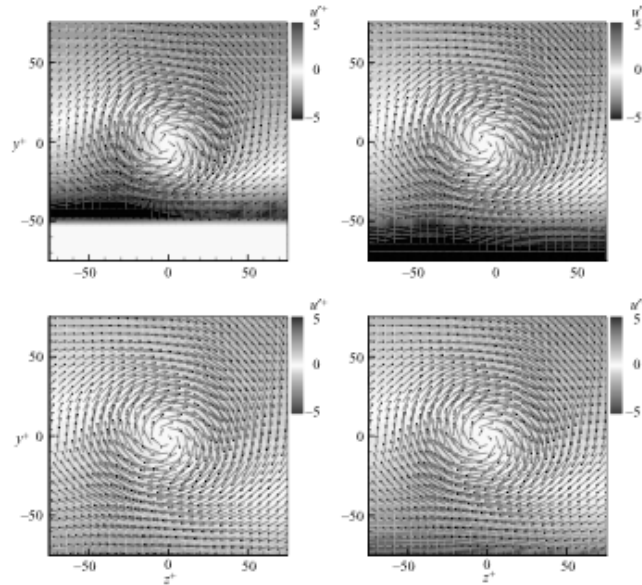


FIGURE 25. Averaged eddy structures in the (e_z, e_y) normal to the wall plane at $R_{y^+} = 50, 75, 100$ and 125 (clockwise from the top left-hand side). The grey scale out-of-plane component.

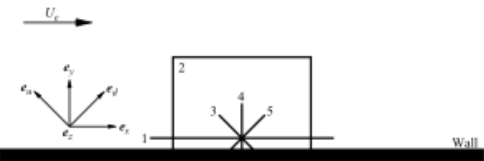


FIGURE 10. Orientations of the various planes used in the two series of PIV measurements: 1, (e_z, e_x) ; 2, (e_z, e_y) ; 3, (e_z, e_x) ; 4, (e_z, e_y) ; 5, (e_z, e_d) .

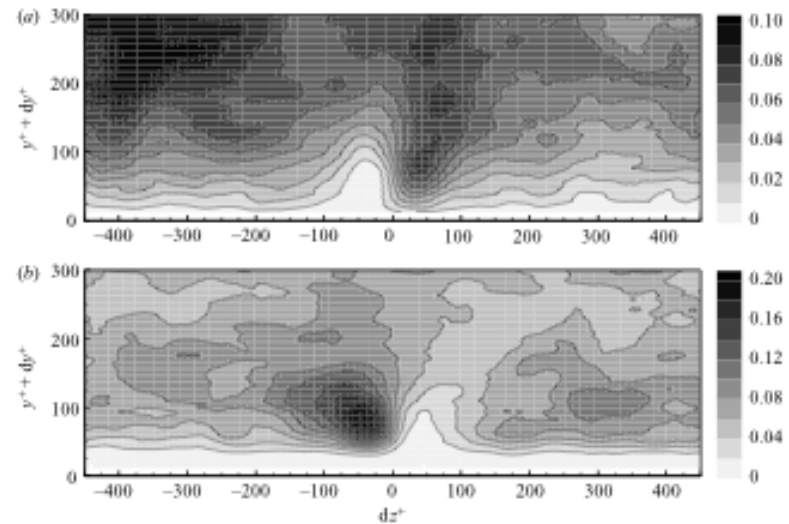


FIGURE 34. Probability map of the location of ejection compared to positive eddy structure and positive eddy structure compared to ejection at $y^+ = 50$ and $R_\theta = 7500$ in the (e_z, e_y) -plane. (a) Fixed point positive eddy structure; moving point, ejection. (b) Fixed point, ejection; moving point, positive eddy structure.

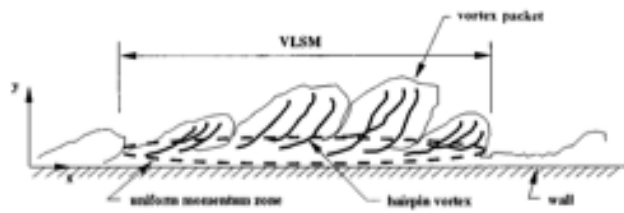


FIG. 7. The conceptual model of the process that creates very large-scale motions. Hairpins align coherently in groups to form long packets, and packets align coherently to form very large-scale motions.

Kim & Adrian (1999) Phys. Fl. 11

VLSMs

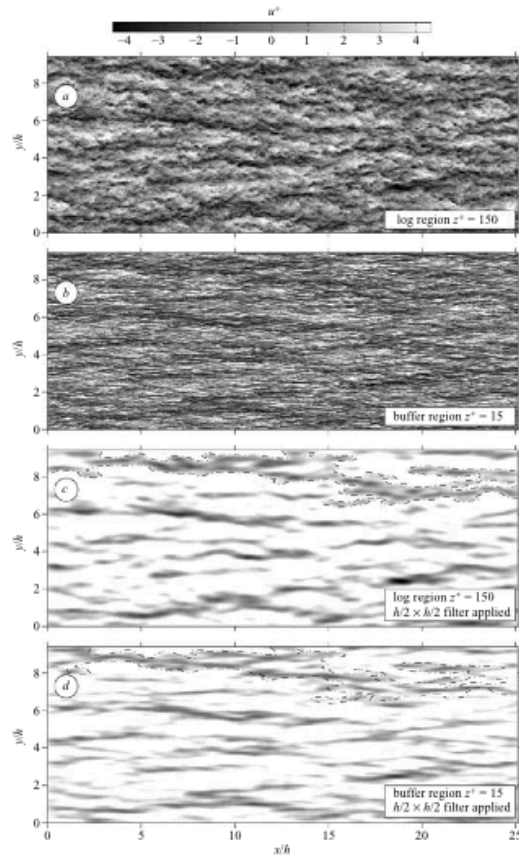


FIGURE 7. Instantaneous flow fields from $Re_\tau = 934$ channel simulations (del Álamo *et al.* 2004). Shading shows u fluctuations (a) at $z^+ = 150$; (b) at $z^+ = 15$ (see upper grey-scale). Plots (c) and (d) show the filtered data at the same respective heights (shading shows negative u fluctuations, grey-scale as figure 4).

Del Alamo, Jimenez,
Zandonade & Moser (2004) JFM 500

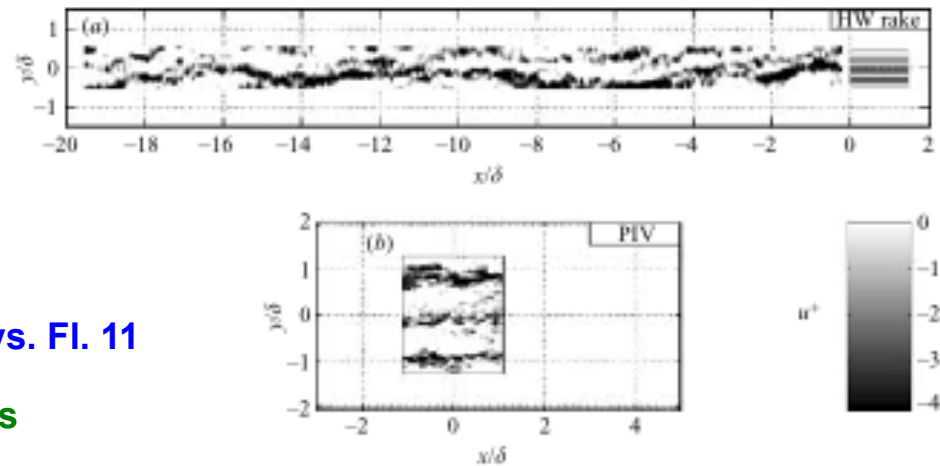
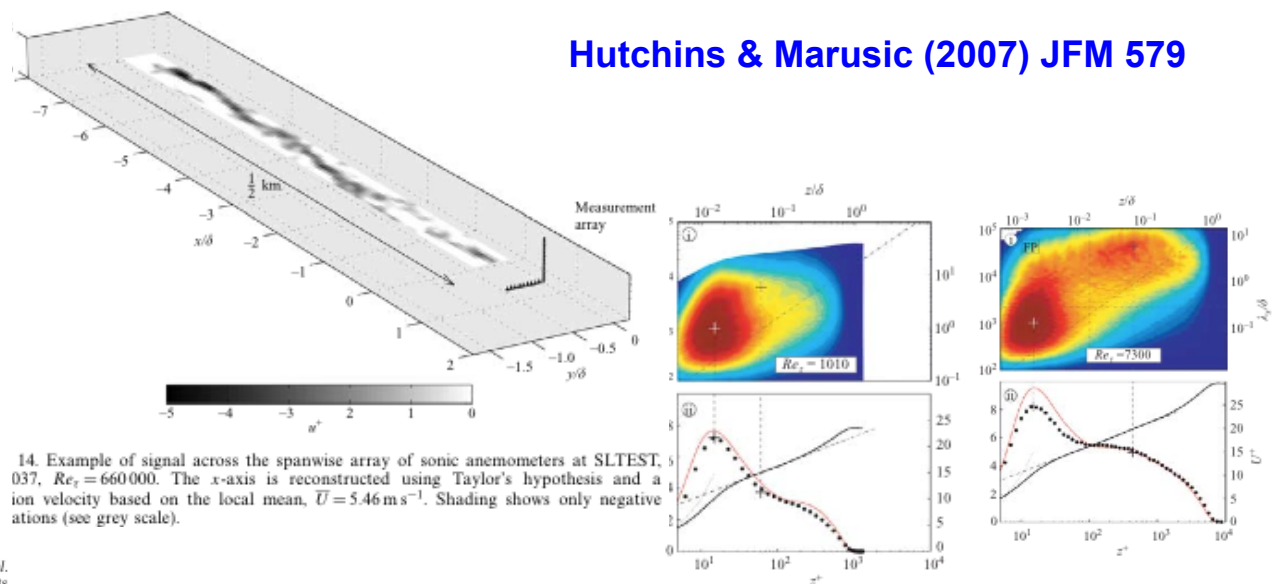


FIGURE 4. (a) Example of rake signal at $z/\delta = 0.15$ for $Re_\tau = 14\,380$. The x -axis is reconstructed using Taylor's hypothesis and a convection velocity based on the local mean, $\bar{U} = 15.9 \text{ m s}^{-1}$. (b) Typical PIV frame for comparison at $Re_\tau = 1100$, $z/\delta = 0.087$. Shading shows only negative u fluctuations (see grey-scale).

Hutchins & Marusic (2007) JFM 579



14. Example of signal across the spanwise array of sonic anemometers at SLTEST, 037, $Re_\tau = 660\,000$. The x -axis is reconstructed using Taylor's hypothesis and a convection velocity based on the local mean, $\bar{U} = 5.46 \text{ m s}^{-1}$. Shading shows only negative u fluctuations (see grey scale).

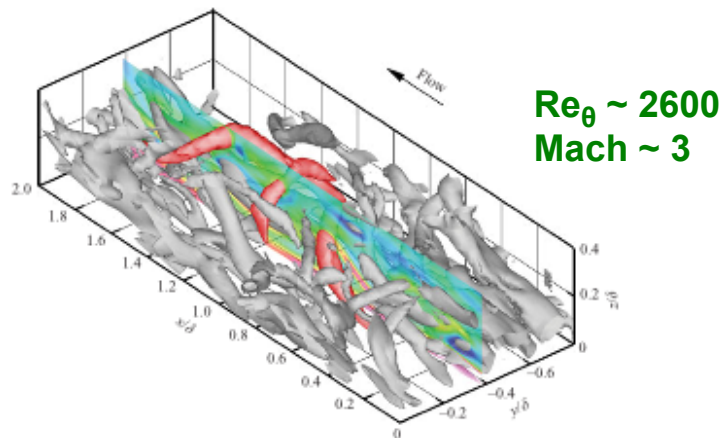


FIGURE 5. Hairpin packet from figure 4 visualized using an iso-surface of $\lambda_{ci} = 3.5\overline{\lambda_{ci}}$. The (x, z) -plane data of figure 4 are included at 50% transparency for reference. Portions of the packet hairpins not obscured by the reference plane have been coloured red.

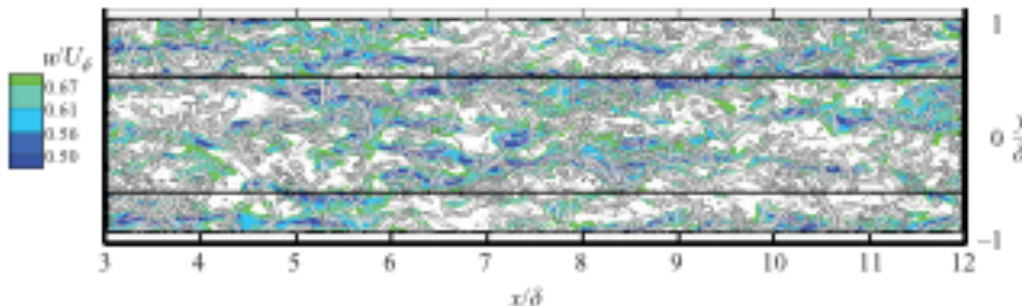


FIGURE 7. Instantaneous visualization connecting the large-scale low-speed regions with hairpin packets; see text for description.

Ringuette, Wu & Martin (2008) JFM 594

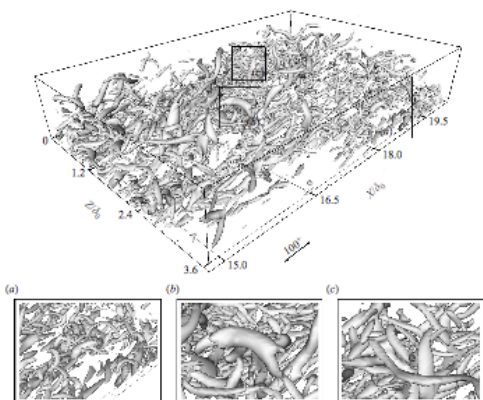


FIGURE 3. Perspective view of coherent structures in the boundary layer ($\lambda_{ci}^2 = 5u_{ci}^2/\delta_{ci}^2$). (a-c) Enlargements of corresponding parts in the main figure.

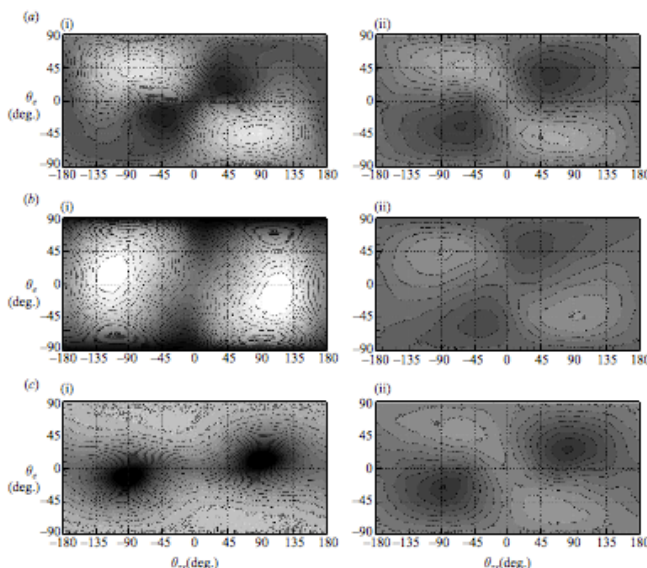


FIGURE 7. Scaled joint p.d.f. of vortex orientation ($\tilde{P}(\theta_x, \theta_y)$) for various vortex orientation criteria. (a) $\tilde{\omega}$ -criterion; (b) $\tilde{\omega}_{ci}$ -criterion; (c) $\tilde{\omega}_v$ -criterion. Twenty-four equally spaced contour levels from 10^{-6} to 10^{-4} (grey shades indicate larger values). (i) Viscous + buffer layer ($y^+ \leq 40$). (ii) Log-layer + wake ($y^+ \geq 40$).

$Re_\theta = 950 - 1350$
 $Mach = 2$

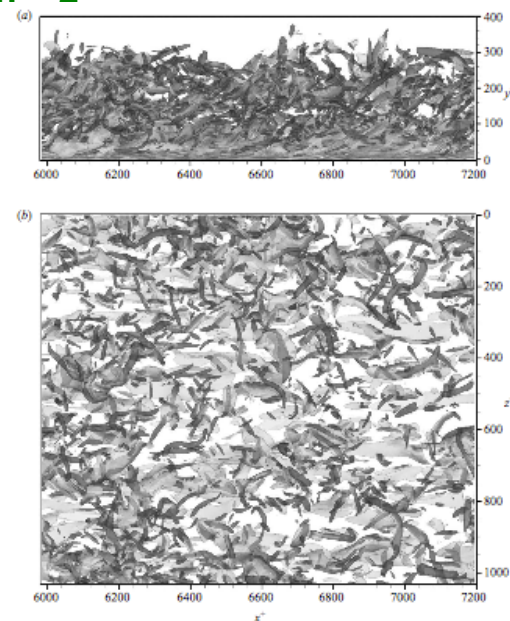
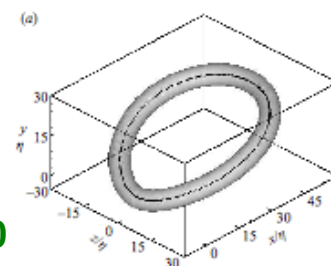


FIGURE 3. Iso-surfaces of tubes strength ($\omega_t/\omega' = 2$, dark grey) and sheets strength ($\omega_s/\omega' = 2$, light grey) projected onto the x - y and x - z planes.

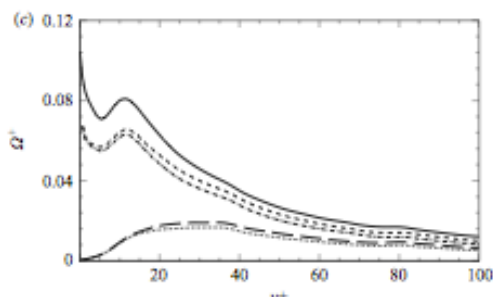


FIGURE 12. Distribution of turbulence kinetic energy (a), turbulent shear stress (b) and enstrophy (c) as a function of wall distance in wall units: DNS (—); strong vorticity events (---); vortex sheets (· · · · ·); vortex tubes (— · — ·); 'roll-up' events (· · · · ·).

Pirozzoli, Bernadini & Grasso (2008) JFM 613
(2010) JFM 648a

T

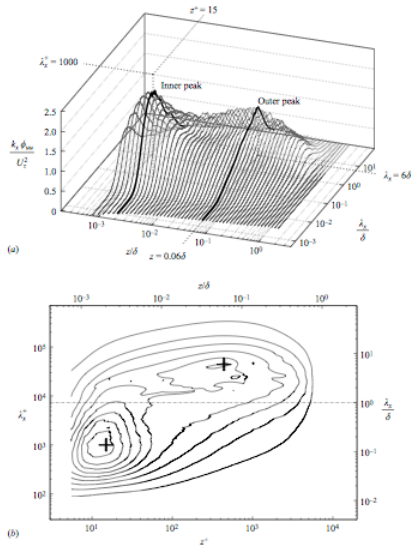


FIGURE 1. Pre-multiplied energy spectra of streamwise velocity fluctuation $k_x \phi_{u_{rms}} / U_\tau^2$ ($Re_\tau = 7300$). (a) Three dimensional surface plot for all wall-normal locations and (b) isocontour representation in which levels are from 0.2 to 1.8 in steps of 0.2; the '+' symbols mark the inner ($z^+ = 15$, $\lambda_x^+ = 1000$) and outer ($z/\delta = 0.06$, $\lambda_x/\delta = 6$) peaks. The horizontal dot-dashed line in (b) shows the location of the spectral filter ($\lambda_x = \delta$).

Mathis, Hutchins & Marusic (2009) JFM 628

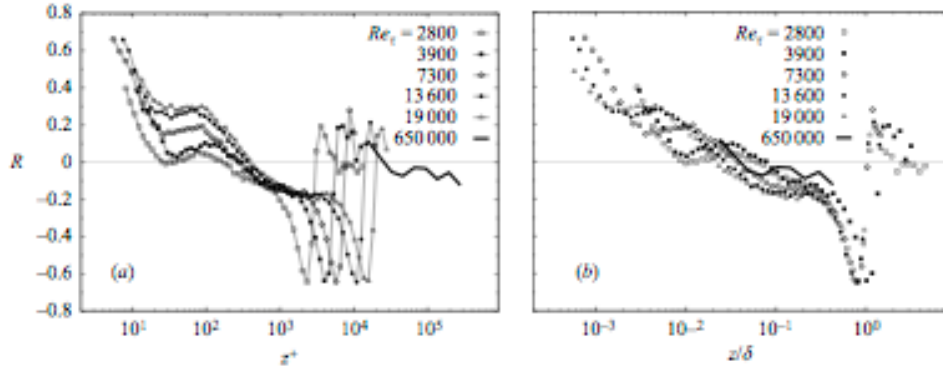


FIGURE 13. Comparison of correlation coefficient between the large-scale component and the filtered envelope of the small-scale component: (a) R plotted in inner-scale z^+ unit; (b) R plotted in outer-scale z/δ unit.

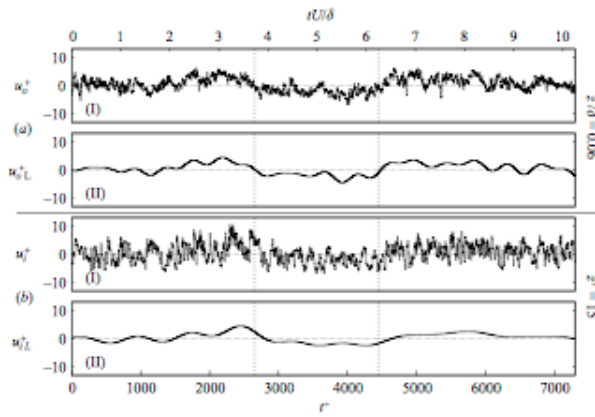


FIGURE 5. Example of large-scale decomposition on the fluctuating u velocity signal: (a) inner-peak location $z^+ = 15$; (b) outer-peak location $z/\delta = 0.06$; (I) raw signals, with 37 % of correlation; (II) large-scale components, with 72 % of correlation. Dashed vertical lines show region of negative large-scale u_{0L}^+ fluctuation.

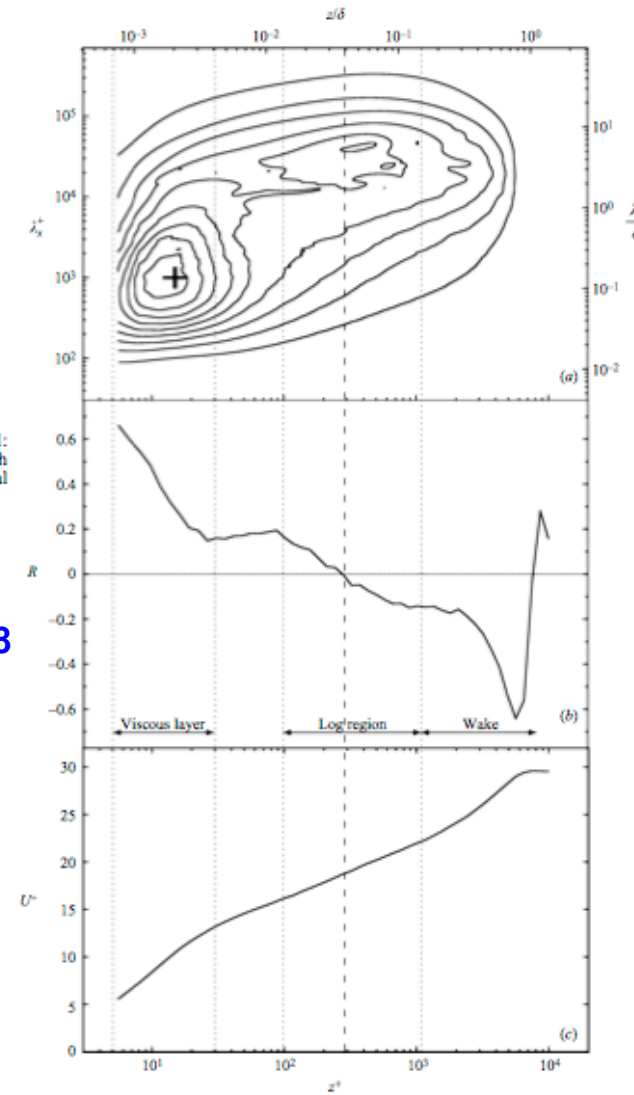
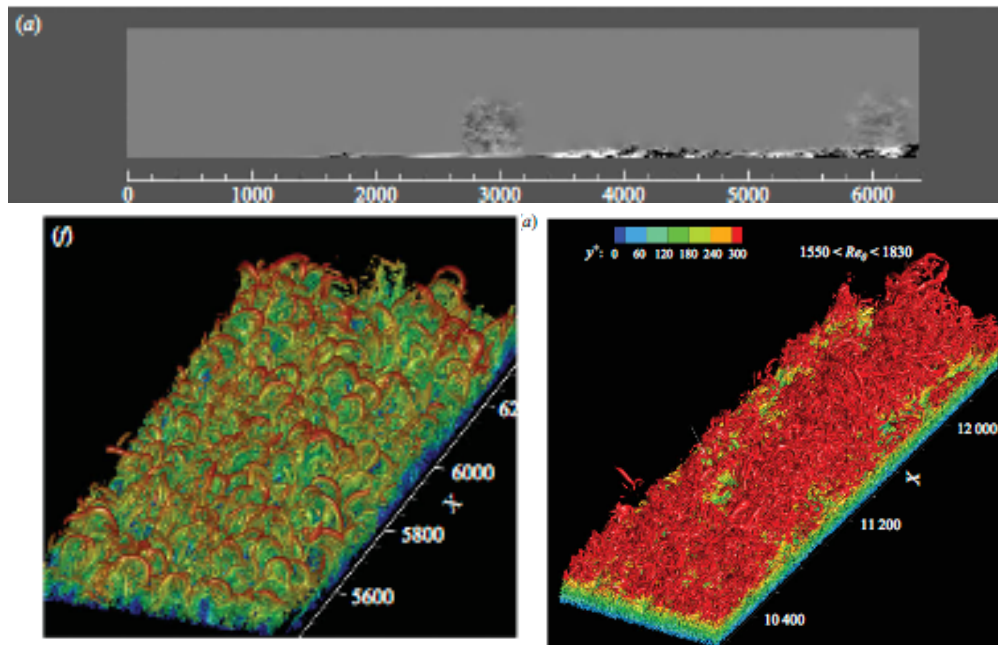


FIGURE 8. Wall-normal evolution of the degree of amplitude modulation: (a) pre-multiplied energy spectra of the streamwise velocity fluctuation $k_x \phi_{u_{rms}} / U_\tau^2$; (b) correlation coefficient $R(z^+)$ between the large-scale component and the filtered envelope of the small-scale component; (c) mean velocity profile; $Re_\tau = 7300$.



Wu & Moin (2009) JFM 630

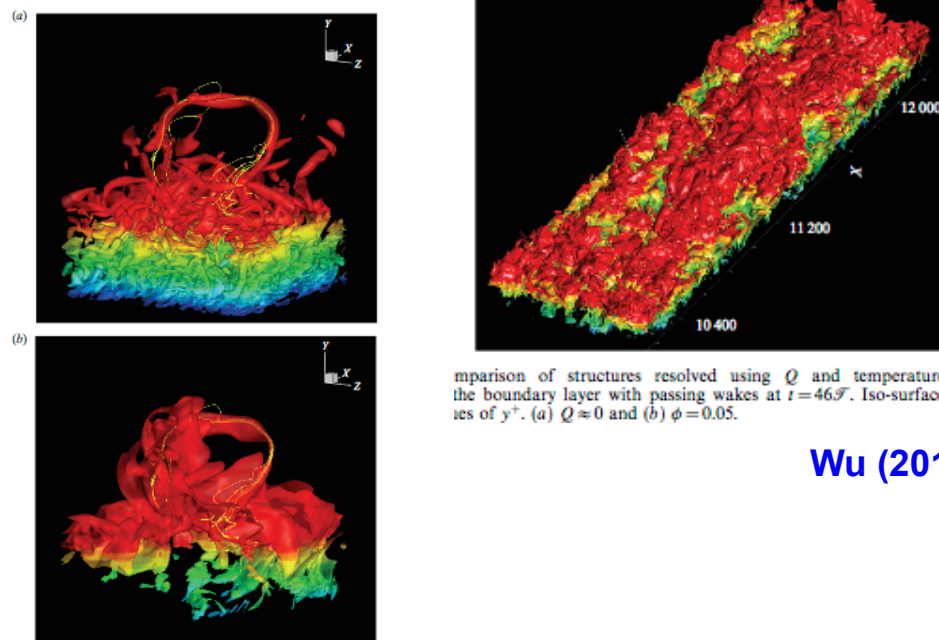


FIGURE 15. Zoomed view of the highlighted hairpin structure in figure 14 overlaid with local instantaneous vortex lines. (a) $Q \approx 0$ and (b) $\phi = 0.05$.

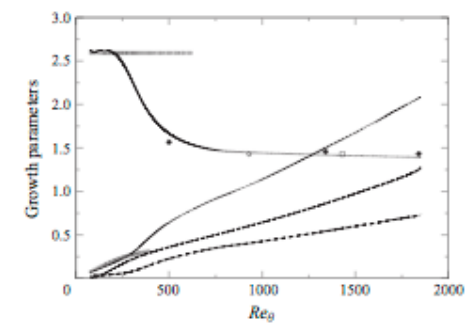
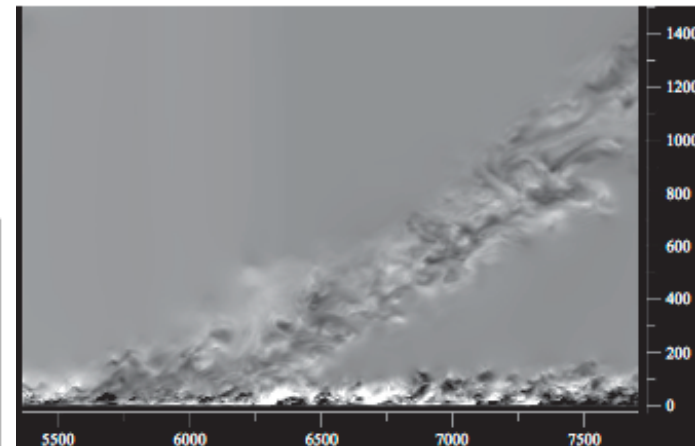


FIGURE 18. Growth parameters of the present boundary layer with free-stream passing wakes. The curves are DNS results. Dotted, $10^{-2}\delta/\theta_0$; dashed, $10^{-4}x/\theta_0$; solid, H ; dash-dotted, $10^{-3}Re_\tau$. Symbols: $\times$, Blasius solutions; diamond, Purtell, Klebanoff & Buckley (1981); circle, Adrian *et al.* (2000); square, DeGraaff & Eaton (2000).

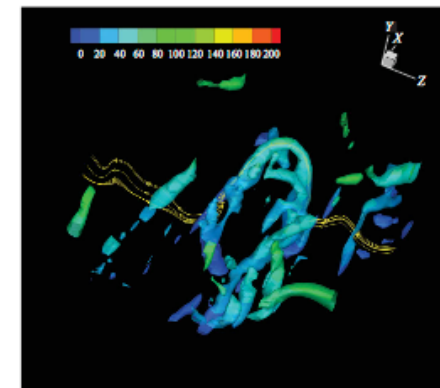


FIGURE 17. Zoomed view of the highlighted near-wall small structure in figure 16 overlaid with local instantaneous vortex lines. Iso-surfaces are coloured using y^+ .

Wu (2010) JFM 664

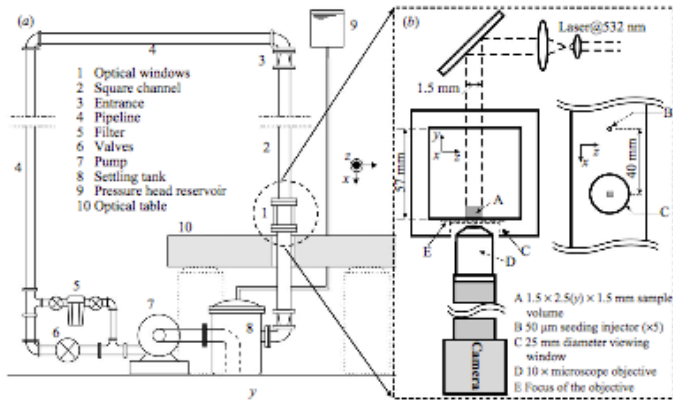


FIGURE 1. Test facility and DHM set-up.

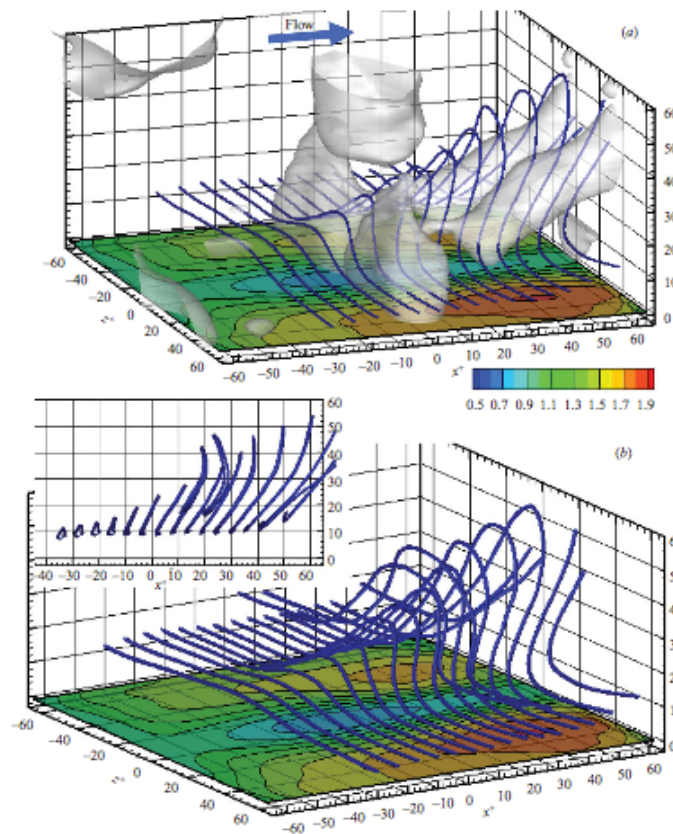


FIGURE 7. Conditionally averaged three-dimensional flow structure and wall stress based on a local stress minimum, $\tau_{xy} < 0.6(\tau_{xy})$, at $x^+ = z^+ = 0$. (a) Isosurface of $\lambda_2 = -350$, selected (blue) vortex lines and distribution of $\lambda_2^{\min}(\Delta x, 0, \Delta z)/(\tau_{xy})$. (b) Conditionally averaged near-wall vortex lines and distribution of $\lambda_2^{\min}(\Delta x, 0, \Delta z)/(\tau_{xy})$. Insert: x - y projection of the vortex lines.

Sheng, Malkiel & Katz (2009) JFM 633

$$Re_\tau = 1470$$

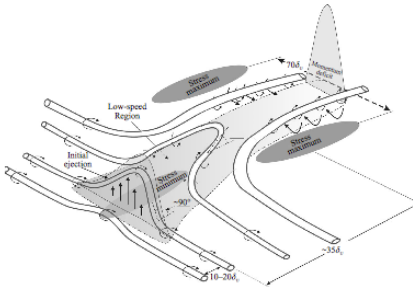


FIGURE 21. A conceptual model illustrating the process of spanwise vortex lifting and the resulting formation of a counter-rotating vortex pair, regions with wall stress extremes and low-momentum region.

Digital Holography

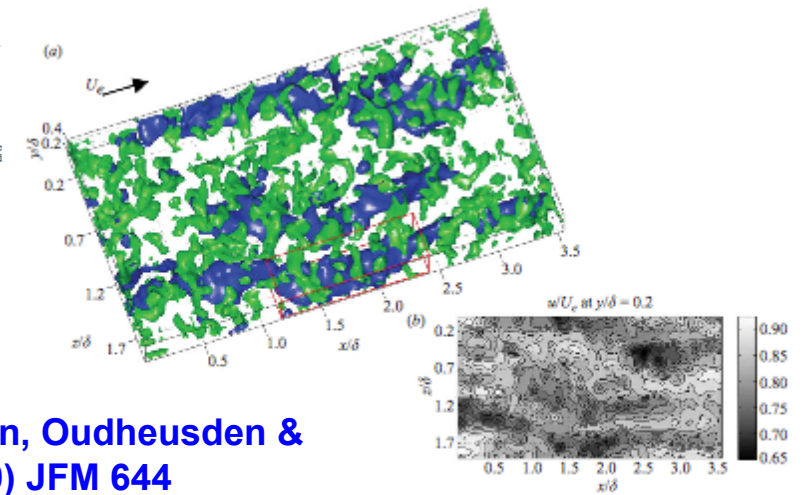


FIGURE 2. (a) Instantaneous vortex distribution detected by the Q criterion (green) and low-speed zones (blue, $u < 0.80U_e$) for $0.15 < y/\delta < 0.47$. (b) A contour plot of the u component of velocity at $y/\delta = 0.20$.

Elsinga, Adrian, Oudheusden & Scarano (2010) JFM 644

Tomographic PIV

$$Re_\theta = 34,000$$

$$Mach = 2$$

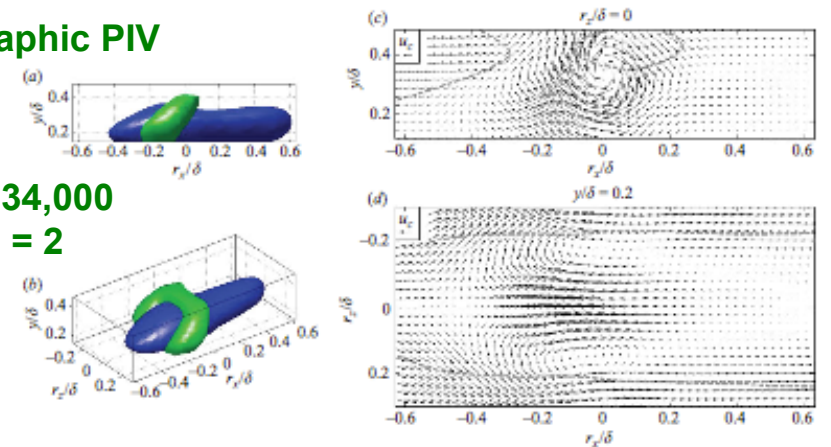
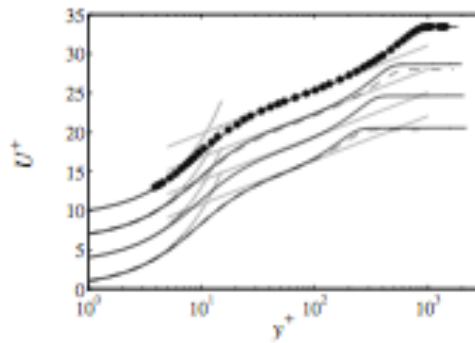


FIGURE 6. Conditional eddy (a,b) given a negative spanwise swirling event at $y/\delta = 0.35$ visualized using the Q vortex detection criterion (green) and low velocity region (blue, $u' < u'_c$) with corresponding velocity vector plot in the x, y plane at $r_z = 0$ and x, z cross-sections at $y/\delta = 0.2$ (c,d). The velocity vectors are relative to the eddy convective velocity u'_c at $y/\delta = 0.35$ indicated in the upper left corner of each plot. The dashed lines indicate $u' = 0$.



$Re_\theta \sim 2500$

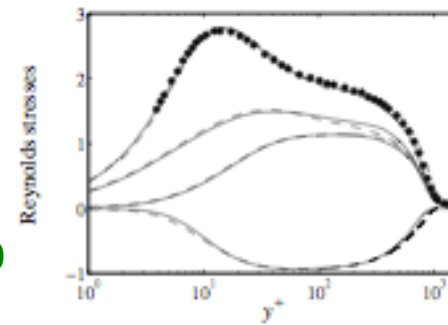
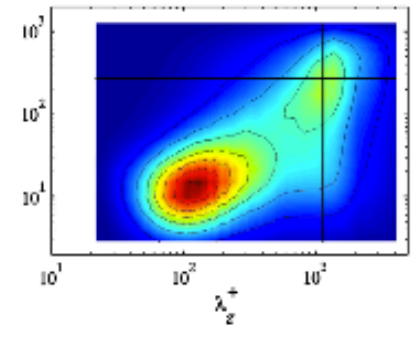
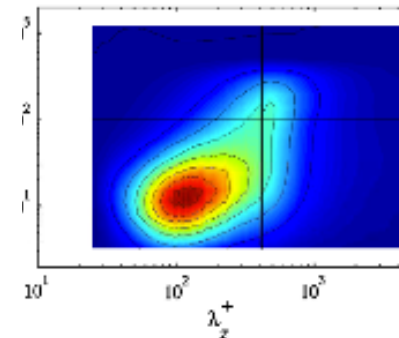
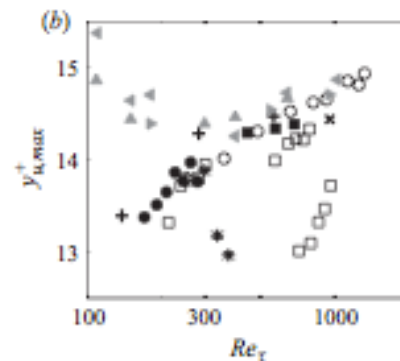
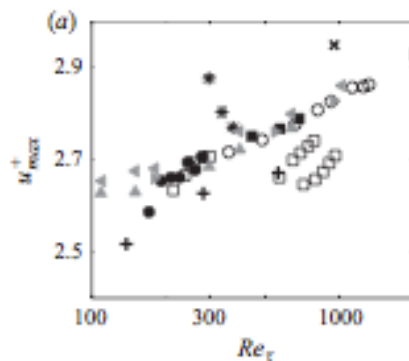


FIG. 2. Mean velocity profile U^+ in viscous units for (—) present DNS at $Re_\theta=671, 1000, 1412, 2512$, (●) present measurements at $Re_\theta=2541$. (---) DNS by Spalart (Ref. 4) at $Re_\theta=670, 1410$. The profiles are shifted by $U^+=3$ for increasing Re_θ . The linear and logarithmic regions are indicated by a thin line, using $1/\kappa \log y^+ + B$ with $\kappa=0.41$ and $B=5.2$.

FIG. 3. Turbulent fluctuations u'_{rms} , w'_{rms} , v'_{rms} , and shear stress $\langle u'v' \rangle^+$ (from top). (—) Present DNS at $Re_\theta=2512$, (●) experiments at $Re_\theta=2541$. (---) Correlations based on the attached-eddy hypothesis (Refs. 14–16).

Schlatter, Örlü, Li, Brethouwer, Fransson, Johansson, Alfredsson, & Henningson (2009) Phys. Fl. 21



$Re_\theta = 1400 \text{ \& } 4300$

FIGURE 4. Near-wall behaviour of inner-scaled streamwise velocity fluctuation. (a) Value and (b) wall-normal position of maximum. Corresponding channel-flow DNS values are depicted in filled grey symbols (see figure 3b for references). as function of the friction Reynolds number. Best fit to data by Komminaho & Skote (2002), Simens *et al.* (2009), Schlatter *et al.* (2009a): $\tau_{w,rms}^+ = 0.298 + 0.018 \ln Re_\tau$. Channel-flow DNS data (filled grey symbols): (◄) (Kawamura *et al.* 1999; Abe *et al.* 2004; Tsukahara *et al.* 2005), (▲) (Iwamoto *et al.* 2002) and (►) (del Álamo & Jiménez 2003; del Álamo *et al.* 2004; Hoyas & Jiménez 2006).

Schlatter, Li, Brethouwer, Johansson & Henningson (2009)
Int. Jour. Heat & Fluid Flow 31

Schlatter & Örlü (2010) JFM 659

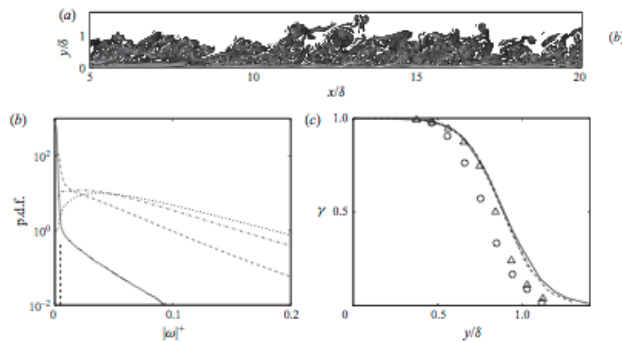


FIGURE 3. (a) Typical section of $|\omega|$ in the boundary layer, showing intermittent potential flow deep into the vortical region. $Re_\delta \approx 700$ –900. (b) Probability density functions of the vorticity magnitude in section BLS2, showing the development away from the wall of the irrotational delta at $|\omega| \approx 0$. $\cdots$, $y/\delta_{99} = 0.44$; $\cdots$, 0.59 ; $\cdots$, 0.88 ; $\cdots$, 1.31 . The dashed vertical line is the limit used to define irrotational flow, slightly larger than a single histogram bin. (c) Intermittency factor. $\cdots$, BLS1 in the present simulation; $\cdots$, BLS2; $\cdots$, BLS3; $\circ$, from experimental velocity measurements at $Re_\delta = 3000$ (Kovaszny, Kibens & Blackwelder 1970); $\triangle$, from temperature measurements at $Re_\delta = 1100$ –4800 (Murlis, Tsai & Bradshaw 1982).

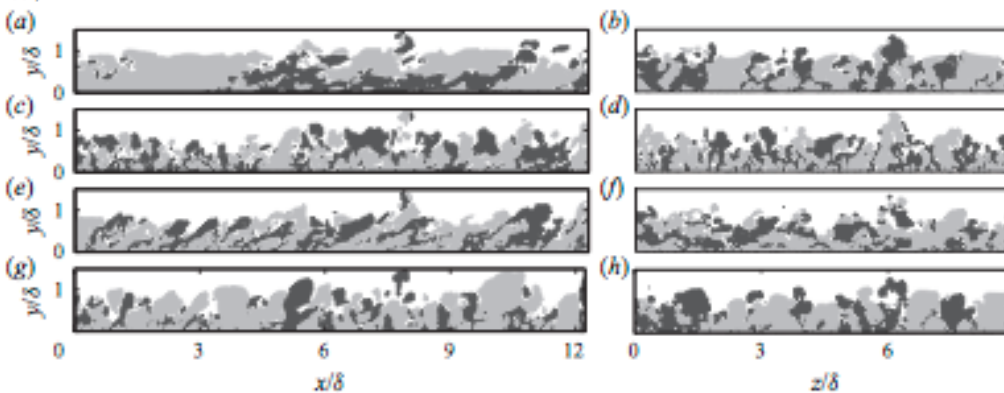


FIGURE 9. Instantaneous sections of the fluctuations in the boundary layer: u (a, b), v (c, d), w (e, f), p (g, h). (a, c, e, g) The x - y sections, in $Re_\delta = 1670$ –2000, and (b, d, f, h) the z - y sections at $Re_\delta = 1670$. All the fluctuations are normalized with the x -dependent friction velocity, and the coordinates are normalized with δ_{99} at $Re_\delta = 1670$. In all the sections the dark areas are below -0.5 wall units, and the lighter ones above $+0.5$.

Jimenez, Hoyas, Simens and Mizuno (2010) JFM 657

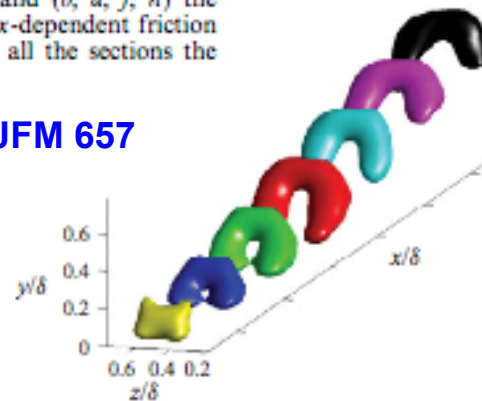


FIGURE 16. (Colour online) Conditionally averaged swirling

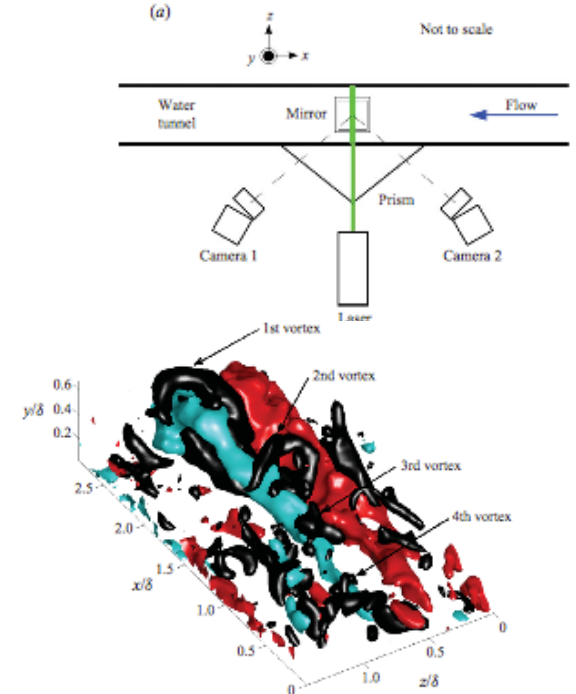
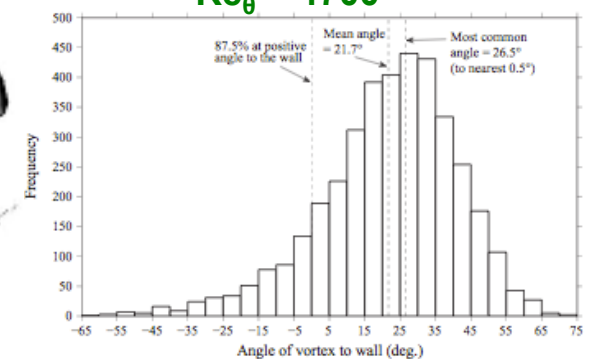


FIGURE 6. (Colour online) Visualisation of vortices with high- and low-speed structures. Black iso-surface: $|\lambda_{ci}|_{iso} = 0.18|\lambda_{ci}|_{max}$. Blue iso-surface: $u_{iso} = -0.1U$. Red iso-surface: $u_{iso} = 0.1U$.

Dennis & Nickels (2011) JFM 673

Stereo PIV
 $Re_\theta \sim 4700$



RE 23. Histogram showing the number of vortices binned according to their angle to the wall. Sample size of 3821.

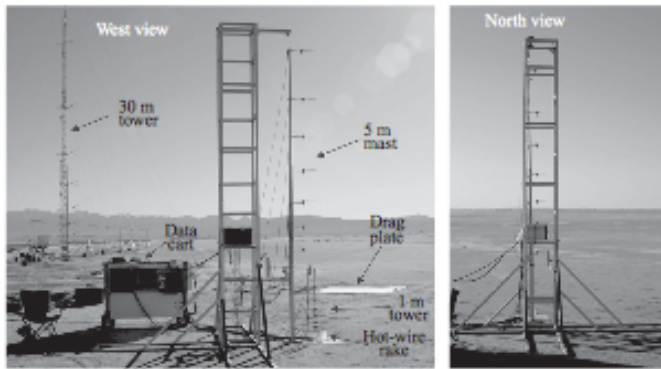


FIGURE 1. Experimental set-up, showing the hot-wire array in the foreground with the 30 m tower and sonic anemometers in the background.

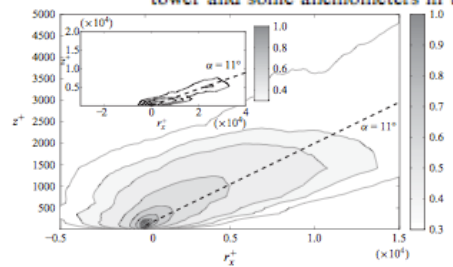


FIGURE 7. Isocontours of the two-point correlation function $\rho_{uu}(r_x^+, z^+, z_{ref}^+)$ at $z_{ref}^+ = 120$. The same contours are plotted in the inset to compare with ρ_{uu} at $z_{ref}^+ = 4032$ plotted in figure 8.

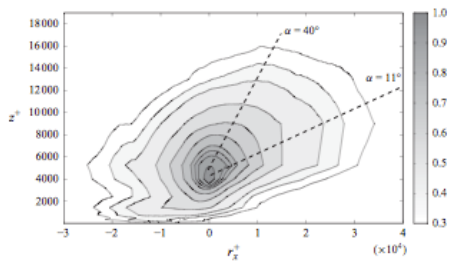


FIGURE 8. Isocontours of the two-point correlation function $\rho_{uu}(r_x^+, z^+, z_{ref}^+)$ at $z_{ref}^+ = 4032$.

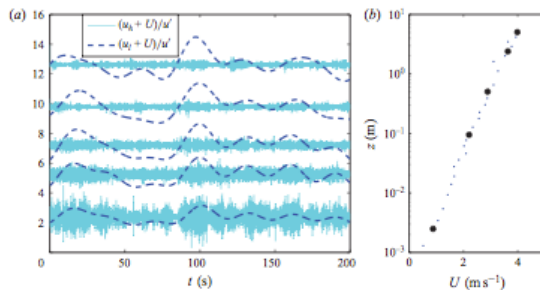
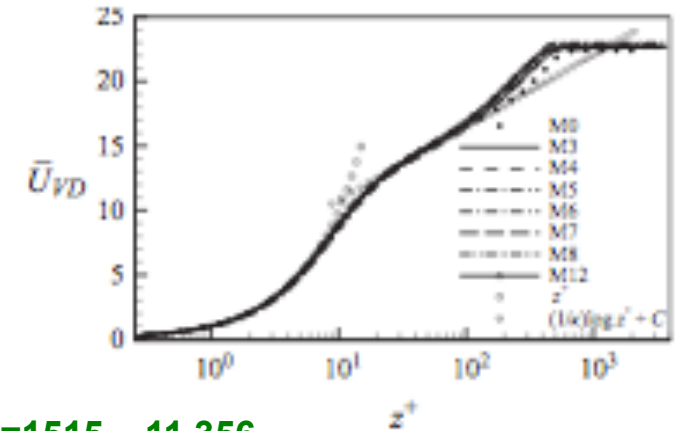


FIGURE 14. (Colour online) (a) Wall-normal variation of the low- (f_L) and high- (f_H) pass fluctuating velocities normalized with the r.m.s. velocity, $(u_a + U)/u'$ and $(u_i + U)/u'$ respectively, at $z^+ = 20, 762, 4033, 19,296$ and $40,547$. (b) Actual wall-normal locations and local mean velocities for the selected wires (•) and other hot-wire probes (◊).



$Re_\theta = 1515 - 11,356$
 $Mach = 0.3 - 11.9$

Duan, Beekman & Martin (2011) JFM 672

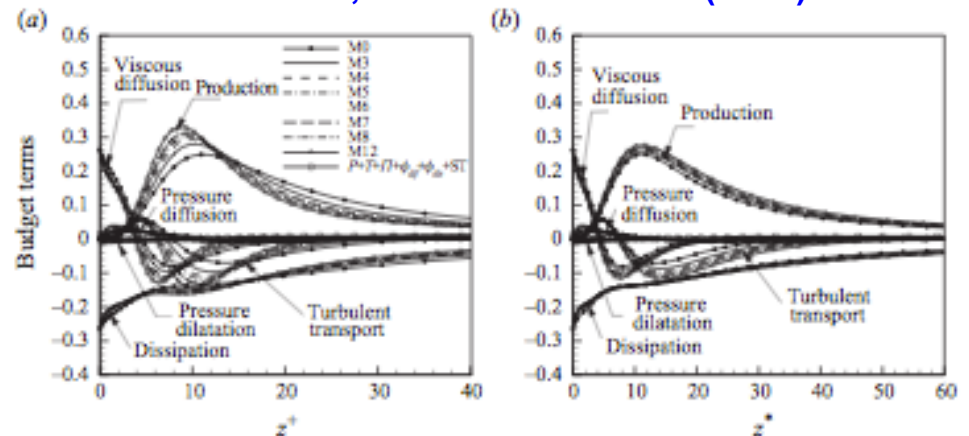


FIGURE 13. TKE budget for cases with different free-stream Mach numbers, non-dimensionalized with (a) wall units and (b) semi-local units, respectively. Variables in wall units are normalized by $\bar{\rho}_w u_\tau^3 / z_\tau$ and $z^+ = z / z_\tau$, and variables in semi-local units are normalized by $\bar{\rho} u_\tau^3 / z_\tau^*$ and $z^* = z / z_\tau^*$.

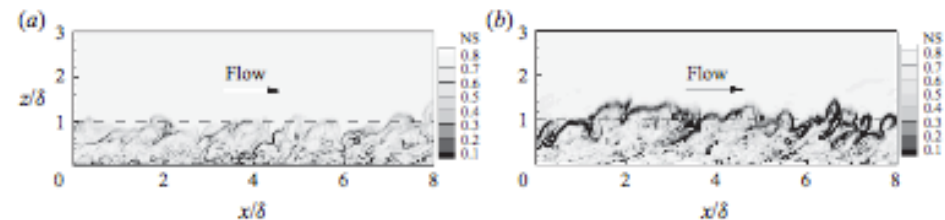


FIGURE 21. (a, b) Numerical Schlieren visualization in a (x, z) plane for Mach 3 and Mach 12.

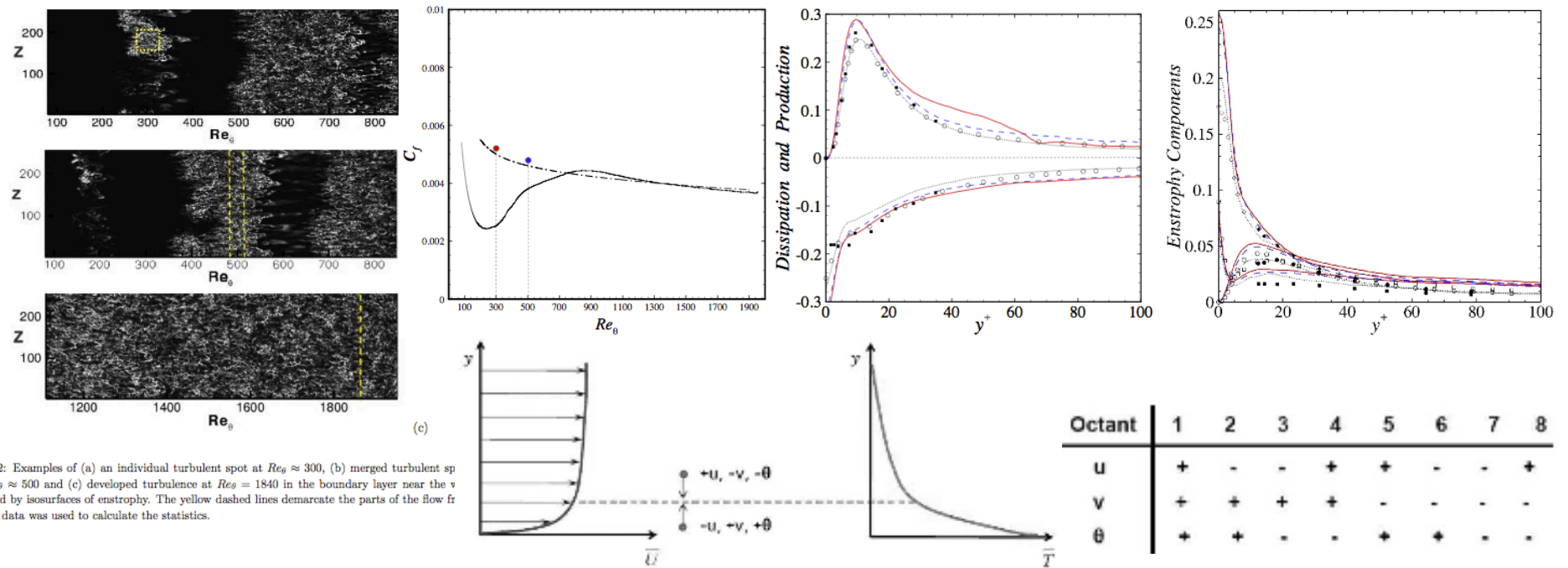
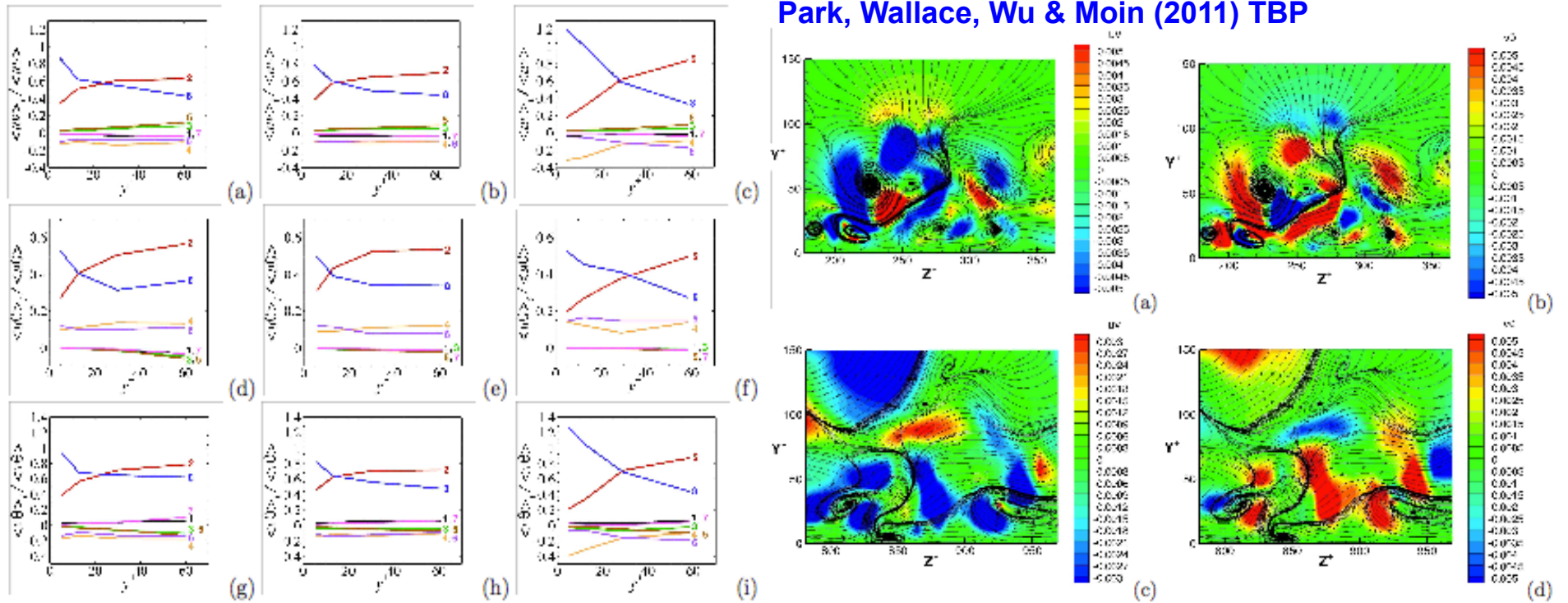


FIG. 2: Examples of (a) an individual turbulent spot at $Re_\theta \approx 300$, (b) merged turbulent spot at $Re_\theta \approx 500$ and (c) developed turbulence at $Re_\theta = 1840$ in the boundary layer near the v marked by isosurfaces of enstrophy. The yellow dashed lines demarcate the parts of the flow for which data was used to calculate the statistics.

Park, Wallace, Wu & Moin (2011) TBP



Summary

- ❑ There has been remarkable progress in turbulent boundary layer research in the past 50 years, particularly in understanding the structural organization of the flow. Consensus exists that vortices drive momentum transport but not about the exact form of the vortices or how they are created and sustained.
- ❑ This progress has been fueled by developments in experimental instrumentation (multi-sensor hot-wire anemometry and PIV) but most of all with the advent of DNS in the 1980s and its subsequent advances.
- ❑ Further progress has been made by the development of high Reynolds number laboratory facilities and the use of field sites to study the very high Reynolds number atmospheric surface layer under near neutral stability conditions.
- ❑ Challenges for the future:
 - Incorporating the knowledge of the structure of turbulent boundary layers into models, including RANS and subgrid scale LES models.
 - Further extending the knowledge gained for zero pressure gradient, smooth wall boundary layers to the complexities of accelerating and decelerating boundary layers and flows with rough walls.
 - Continuing to develop and implement methods to control turbulent boundary layers that occur in real engineering applications.

Highlights of Fifty Years of Turbulent Boundary Layer Research

Pre – 1961

SLIDE 1

Title

SLIDE 2

Summary of periods and highlights by decades

SLIDE 3

Early hot-wire measurements. Some done in Delft by Burgers and co-workers even earlier in the 20s.

SLIDE 4

Similarity laws for “overlap” and “wake” regions.

Millikan: “Law of the wall”

Coles: “Law of the wake”

SLIDE 5

Townsend: RMS distributions of velocity fluctuations and estimate of the TKE balance from hot-wire measurements.

Corrsin & Kistler: “Superlayer” properties and intermittency function in TBL

Klebanoff: TKE production and dissipation rate estimates. All the determinations of the dissipation rate from this period were crudely estimated as the residue of the other terms.

SLIDE 6

Favre et al: Space-time isocorrelation contours with optimum time delay. Probes were separated in both the streamwise and wall normal directions. Fixed probe at about $y^+ = 40$. Note high aspect ratio of correlation in x-y plane compared to y-z plane. Note also that a small correlation remains all the way out to $y = 0.3\delta$.

Grant: Spatial correlation tensor components at several locations of the fixed probe in the boundary layer. He inferred structure from these correlations.

SLIDE 7

Willmarth & Wooldridge: Wall pressure space-time correlation function with two probes of varying separation in the streamwise direction. One horizontal axis is time and the other is downstream distance. The vertical axis is the correlation level. The ridge flowing out to the lower right of the figure shows the cumulative effect of

eddies of different scale on the wall pressure with increasing time and distance. The decay in correlation is interpreted as the increasing loss of the effect of smaller eddies.

Bakewell & Lumley: Streamlines in the cross-stream plane of a pipe flow of glycerin as revealed by proper orthogonal decomposition of hot-film data and their suggested eddy structure.

SLIDE 8

Visual experiments that excited the research community about organized coherent motions in wall bounded flows.

Kline et al.: Low-speed streaks revealed by hydrogen bubbles and their “bursting”.

Corino & Brodkey: “Ejection” and “sweep” coherent events revealed by particle motion near the wall in a pipe flow viewed in a moving frame of reference.

1970 – 1986: Conditional Processing of Measurements & Further Visualization

SLIDE 9

Kovaszny et al.: Intermittency function, point averages of “fronts” and “backs” of potential flow bulges and a sketch of them.

SLIDE 10

Wallace et al.: Quadrant analysis of the Reynolds shear stress in a channel flow. Plot of covariance integrand, uv dudv, by quadrant and as function of distance from wall.

Willmarth and Lu: Quadrant analysis for boundary layer with “hole” of constant Re Stress to accentuate large amplitude events.

SLIDE 11

Several hundred small holes covered with a mirrored silicone rubber foil. Using interferometry and a high speed movie camera, the instantaneous fringes on each element were used to determine local wall pressure after calibration.

Figure shows pressure pulses being convected downstream over one row of transducers. Patterns persist for more than 1100 viscous length scales ($1\frac{1}{2}$ the boundary layer thickness). Convection velocities are about $\frac{3}{4}$ of the freestream velocity.

SLIDE 12

Blackwelder and Kaplan: Intention was to detect turbulent “bursts” using Variable Integral Time Averages (VITA) of conditionally sampled data. Condition was that the local square of the streamwise velocity fluctuation minus the square of the local mean be larger than some chosen threshold. This detected events with large du/dt .

The double peaks in the conditional averaged Re stress are roughly related to the Q2 and Q4 quadrants. Simultaneous rake measurements show that these events have great coherence in the wall normal direction.

Chen & Blackwelder: Passively heated wall and a rake of X-array hot-wires. Highly coherent ramps in the temperature fluctuations were observed. Conditioning on these ramps, conditional velocity fluctuation averages were obtained that show the outward motion of warmer, lower momentum fluid downstream of the front followed by inward motion of cooler, higher momentum flow upstream.

Antonia et al.: Similar study using heat as a passive scalar marker. Fig. shows conditional averages of u , v and θ and the momentum and heat fluxes in the inner layer of the TBL.

SLIDE 13

Head & Bandyopadhyay: Smoke visualization of boundary layer structure viewed in inclined planes and interpreted as hairpin vortices.

Balint et al.: A similar study with wall layer and potential flow separately marked by smoke and the tripping of the boundary layer varied. Photo shows the evolution and growth of wall layer structures which eventually penetrate the potential flow. The potential flow is also ingested deeply into the turbulent boundary layer.

Townsend: Proposed the attached eddy model

Perry et al.: Used this conceptual model of attached hairpin eddies, rolling up and lifting up out of near wall sheets of vorticity, to construct a theoretical model that attempts to explain many of the statistical features of the boundary layer, including the log layer.

1986 – 2011: DNS, Multi-Sensor Hot-Wire Probes & PIV Measurement

SLIDE 14

Kim & Moin: Vorticity (vortex lines) showing hairpin and Ω -like shapes in a turbulent channel flow DNS. Cross-stream plane cut through the leg of the vorticity line bundle in the upper right figure shows that this is truly a vortex as revealed by the velocity vector projections on this plane.

SLIDE 15

Kim Moin & Moser: Their DNS was accepted by experimental researchers in part because of the flow visualization they did of simulated hydrogen bubbles that revealed the same structure as in physical experiments.

In this paper, they showed the first DNS distribution of the rms vorticity components and other statistics of the vorticity field.

Balint et al.: We published our rms vorticity component distributions and other vorticity field statistics, experimentally measured with our miniature 9-sensor probe, that year in the Proceedings of the 1st European Turbulence Conference.

SLIDE 16

Spalart: A year later, in 1988, he published the first DNS of a turbulent boundary layer where he employed the so-called “fringe” method to rescale the flow allowing him to employ periodic boundary conditions in the streamwise direction. The figures are of the TKE budget and contours of vorticity projected onto streamwise and cross-stream inclined planes of the flow.

Balint et al.: Experimental values of the turbulent production and dissipation rates are compared to Spalart’s DNS values and the Kim, Moin and Moser DNS channel flow values in the figure on the right.

SLIDE 1

Balint et al.: Vorticity fluctuation component spectra compared to Spalart’s DNS.

Distribution of the terms of the transport of total enstrophy equation.

SLIDE 18

Aubry et al.: Expansion of the wall region using POD to obtain low-dimensional sets of ODEs. Streamwise rolls are revealed that have intermittent Reynolds stress “burst” characteristics. This was one of the first applications of low-dimensional chaotic dynamical systems theory to realistic turbulent open flows.

Antonia et al.: A rake made up of an array of 8 X-array hot-wires was used to construct sectional streamlines and contours of the large-scale vorticity in streamwise planes at several Reynolds numbers. Large-scale vortices (foci) and saddle points of high strainrate are evident in this frame of reference traveling to the left at 0.8 of the freestream velocity. Variation with Reynolds number is seen in the figure in the lower right.

SLIDE 19

Bernard et al.: Lagrangian analysis of the Reynolds shear stress that decomposes it exactly into (1) the correlation of u at the terminal point, a , with v at the set of initial points, b , (2) a “displacement transport” term and (3) an “acceleration transport” term. For large enough mixing times, this $u_a v_b$ correlation goes to zero, as seen in the distribution on the right. The displacement transport term is simply a sort of mixing length/ mean gradient type effect. The acceleration transport term produces a significant fraction of the Reynolds stress, having a positive or negative contribution depending on position relative to the wall.

The upper right figure shows the pdfs of the particle displacements sorted by the quadrants of quadrant analysis as a function of y^+ .

Their group also identified quasi-streamwise vortices with a recognition algorithm and studied particle displacements and Reynolds stress creation in relation to these vortices as seen in the middle lower figure.

SLIDE 20

Spina et al.: Studied the structure of supersonic turbulent boundary layers adopting methods used in subsonic, low Reynolds number flows such as the VITA technique and quadrant analysis.

SLIDE 21

Robinson: Analyzed the Spalart DNS to study the structure of the flow. Low pressure was used as a criterion to detect vortices. Few complete hairpins were observed, but this could have been a result of the threshold values set. The relation of low-speed streaks and Q2 and Q4 Reynolds stress to the vortices is clearly seen. Robinson believed that hairpin-shaped vorticity lines are simply a result of their distortion by quasi-streamwise vortices, and that they do not necessarily, themselves, indicate the presence of true hairpins.

SLIDE 22

Tsinober et al.: Use of a 12-sensor hot-wire probe to demonstrate, experimentally, the most probable alignment of the vorticity vector with the intermediate eigenvector of the rate of strain tensor. This had previously been seen in DNS of both isotropic and shear flow turbulence and is now known to be a general characteristic of all turbulent flows.

Durbin: Tensorially consistent 2nd order closure modelling of the Reynolds stress transport equation. Applied to channel and boundary layer turbulent flows with and without pressure gradients and to flows around 90 deg. bends. Figures show model values of turbulence intensities and friction coefficient distributions compared to experimental values.

SLIDE 23

Choi et al.: Active control for drag reduction using (1) v control at the surface with suction and blowing based on detection in the flow of sweep and ejection events, (2) w control at the surface, (3) combinations of the two types of control, etc. The figures show the effects of control compared to no control on TKE production and dissipation rates and on the vorticity component rms distributions.

SLIDE 24

Saddoughi & Veeravalli: Performed a highly regarded experiment in the NASA AMES huge wind tunnel with its 80' x 120' test section to examine indicators of local isotropy in turbulent boundary layers. They documented the effects of Reynolds number and proximity to the wall. The figures here show examples of (1) compensated streamwise and cross-stream spectra rather far from the wall and at a

rather high Reynolds number ($Re_\lambda = 1450$) and (2) compensated second-order structure functions for streamwise and cross-stream velocity fluctuations. Both plots provide evidence of local isotropy under these conditions.

Wallace & Ong: We were kindly allowed to piggyback on their experiment to use our 12-sensor probe to examine local isotropy of the vorticity field. The figure shows evidence of it in the inertial subrange as seen in the ratio of the two cross-stream vorticity components computed from the streamwise component under isotropic assumptions to their measured values. This ratio should be unity for isotropic flow, and it is in the inertial subrange. Experimental error takes over in the dissipation range of this figure.

Mestayer had carried out an earlier and similar study in the high Reynolds number IMST Air-Sea Interaction Simulation tunnel at $Re_\lambda = 616$ in the dissipative range but not in the inertial subrange.

Slide 25

Nagano & Tagawa: Trajectory analysis based on uv plane quadrants illustrated in upper left. In lower right the number of types of trajectories are shown as a function of the Willmarth & Lu “hole” size. The figure on the right shows autoregressive (AR) model predictions of time series of temperature for various trajectory patterns.

SLIDE 26

Klewicki et al.: Developed field site southwest of Salt Lake City, Utah, on the Salt Flats, where measurements in the atmospheric surface layer could be carried out. At sundown, neutral stability occurs giving conditions similar to those in a laboratory boundary layer but at the very high Reynolds numbers, Re_θ , of $O(10^6)$. The figures show: (1) the histogram of spanwise low-speed stream spacing obtained from flow visualization, (2) distribution of the rms streamwise velocity distribution showing how the peak increases with Reynolds number, (3) the joint pdf of the u and v fluctuations at low and high Reynolds numbers and (4) the space-time autocorrelation of u at low and high Reynolds number.

Folz & Wallace: They have invited many research groups to work there over the years. We were there the first year, and, among other things, measured the contributions of all the terms to the dissipation rate.

SLIDE 27

Jeong et al.: Used method of detecting vortices with $-\lambda_2$, the second invariant of the velocity gradient tensor which indicates dominance of rotation over strain. Found quasi-streamwise vortices that are not in the form of hairpins. Vortices, of opposite sign, slightly inclined to the wall and skewed in the x-z plane, exist in staggered overlapping arrays. They state that a phase difference in space accounts for nearly

all of the Q2 and Q4 Reynolds stress as well as counter-gradient Q1 and Q3 Reynolds stress.

Schoopa & Hussain: Carried out a transient growth stability analysis to show how the vortices emerge out of instabilities of low-speed streaks under certain conditions.

SLIDE 28

Honkan & Andreopolous: Used a 12-sensor probe to obtain the angular orientation of the projection of the vorticity vector near the wall in wall normal and wall parallel planes of the flow.

Ong & Wallace: Obtained these orientations for the vorticity filaments that most contribute to the vorticity covariances from weighted vorticity component joint pdfs (covariance integrand plots).

SLIDE 29

Barenblatt et al.: Proposed a Reynolds number dependent power law alternative to the log law to describe the mean velocity in the overlap region. The figure shows many different data sets plotted as evidence to support this theory. The debate about the veracity of this partial similarity law compared to the complete similarity log law still continues.

SLIDE 30

Guarini et al.: Carried out a supersonic Mach 2.5 DNS that showed very little difference from subsonic turbulent boundary layer statistics. The figures show the distributions of the rms vorticity components and the TKE budget.

Kholmyanshy et al.: Carried out a study using a 20-sensor probe to measure both velocity and velocity gradient as well as temperature fluctuations. The measured many different properties of these fields including the joint pdf of the enstrophy production vs. production of strain shown in the figure.

SLIDE 31

Adrian et al.: Used planar PIV in numerous studies to reveal many features of the structure of turbulent boundary layers. Fig. in upper center compares rms spanwise vorticity to DNS and hot-wire values. The figures in the center and on the right show large scale zones of coherent momentum, high shear in ramps inclined to the wall and vortices that are interpreted as “heads” of hairpins. Their hairpin model, like those of others, accounts for Q2 and Q4 Reynolds stress. They also describe the hairpins as occurring in “packets” and account for the creation of new hairpins.

SLIDE 32

Chacin & Cantwell: Used critical point theory, primarily developed by Perry and Chong, to analyse the Spalart turbulent boundary layer DNS. The top middle figure shows regions of positive discriminant in association with Reynolds stress events.

The top right figure shows the characteristic “tear drop” shape of the Q-R plane joint pdf with superimposed regions of Q2 and Q4 Reynolds stress. The regions in this plane with respect to the Villefosse line of zero discriminant are described by the flow categories in the figure to the lower left.

Andreopolous & Honkan: Obtained this teardrop shape jpdf from 12-sensor hot-wire measurements in the buffer layer of their experimental turbulent boundary layer. It is now believed to be a universal feature of turbulence.

SLIDE 33

Carrier & Stanislas: Used planar PIV to investigate structure in various planes, including planes tilted upstream and downstream across the flow, to study the eddy structure in the boundary layer at $Re_\theta = 7,500$. They used a pattern recognition technique that involved convolving a model vortex with the 2D flow field to educt the actual vortices. Instantaneous and average vortices are shown in the figures in the upper right. They studied Q2 and Q4 events in spatial relationship to these vortices.

SLIDE 34

Kim & Adrian: Observed very large scale motions (VLSMs) in a turbulent pipe flow that were 12 – 14 times as long as the pipe radius.

Del Alamo et al: Also observed these VLSMs in their channel flow DNS.

Hutchins & Maurusic: Observed VLSMs as long as 20δ in the log and lower wake regions in their experiment in the Utah desert, and studied how they affect premultiplied 1D spectra of the streamwise velocity fluctuations. The rising plateau in the rms distribution further from the wall is related to the second peak in the spectrum coming from these VLSMs.

SLIDE 35

Ringuette et al.: Carried out a DNS at $Re_\theta \sim 2600$ and $Mach \sim 3$ in which they observed most of the same types of structures as in subsonic flow.

Pirozzoli et al.: Also carried out a supersonic DNS at $Mach = 2$ and $Re_\theta = 950 - 1350$. They studied the statistical properties of quasi-streamwise vortices near the wall and of hairpins and hairpin packets further from the wall. In the outer layer they state that these statistical properties are consistent with noninteracting closed loop vortices. In their later study they conclude that sheet-like structures have a greater influence on the statistical properties of the TBL than the vortices.

SLIDE 36

Mathis et al.: Studied the modulating effect that large scale motions in the outer flow have on the fluctuations in the inner region of the flow. They did this by filtering the streamwise velocity signals and correlating them. They examine how the degree of correlation depends on wall normal distance and how it is related to the 1D spectra.

SLIDE 37

Wu & Moin: Carried out a spatially developing DNS of the TBL which goes through bypass transition to turbulence. It exhibits a forest of hairpins. When the wall is passively heated, the temperature field also exhibits hairpins.

SLIDE 38

Sheng et al.: Used digital holography to study the wall layer structure in a square duct at $Re_\tau = 1470$ and obtained conditionally averaged hairpin structures that emerge from the spanwise vorticity sheets near the wall and are related to high wall shear stress occurrences.

Elsinga et al.: Found hairpin packets using tomographic PIV at $Re_\theta = 34,000$ and $Mach = 2$

SLIDE 39

Schlatter et al.: Carried out boundary layer DNS up to $Re_\theta \sim 4,300$. They carefully studied statistical properties, and have also compared the consistency of various DNS studies. They don't observe hairpins in their highest Reynolds number DNS.

SLIDE 40

Jimenez et al.: Carried out a TBL DNS up to $Re_\theta = 2100$. They don't observe hairpins, but they do observe the large scale coherent momentum events.

SLIDE 41

Guala et al.: Observations in the atmospheric surface layer quantifying interactions between the VLSMs and the turbulence from the energy containing to the dissipative scales.

Duan et al.: DNS of TBL up to hypersonic cases. Flow structure doesn't change much.

SLIDE 42

Park et al. : Showed that statistics, including those of the fine scale properties, enstrophy and dissipation rate, are very similar in transitional turbulence spots and in developed turbulence. This implies that the structure is likely to be similar. Octant analysis showed that motions consistent with mean gradient transport of momentum and heat are the dominant contributors to the fluxes for both transitional spots and developed turbulence. The transport of momentum and heat is strongly associated with vortices as shown in the cross-stream cuts through the instantaneous fields for the transition and developed cases.

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Summary

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(send additions to wallace@umd.edu)

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